

Vector Autoregression (VAR) of Longitudinal Sleep and Self-report Mood Data

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Editor: Could use one

Abstract

Self-tracking is one of many behaviors involved in the long-term self-management of chronic illnesses. As consumer-grade wearable sensors have made the collection of health-related behaviors commonplace, the quality, volume, and availability of such data has dramatically improved. This exploratory longitudinal N-of-1 study quantitatively assesses four years of sleep data captured via the Oura Ring, a consumer-grade sleep tracking device, along with self-reported mood data logged using eMood Tracker for iOS. After assessing the data for stationarity and computing the appropriate lag-length selection, a vector autoregressive (VAR) model was fit along with Granger causality tests to assess causal mechanisms within this multivariate time series. Oura's nightly sleep quality score shown to Granger-cause self-reported presence of depressed mood using a VAR(3) model.

1 Introduction

Long-term self-management of chronic illnesses such as bipolar disorder require persistent awareness of illness state over long periods of time and at varying time scales (Murnane et al., 2016; Morton et al., 2018; Majid et al., 2022). Remaining consistently aware of key indicators signalling the onset of a chronic condition allow individuals a chance at early intervention to reduce the severity of a given episode. For example, an individual may modify behavior, engage their health practitioners, or adjust medication dosage. However nuanced, bipolar disorder is an illness that often degrades an individual's self-awareness and capacity for self-monitoring during symptomatic periods.

In the context of this specific illness, a volume of prior work has demonstrated the vital role of sleep in order to promote mood stability and prevent symptomatic episodes (Harvey et al., 2009; Murray and Harvey, 2010; Gruber et al., 2011). Although the particulars of this topic fall beyond the scope of this paper, these nuanced relationships may in fact be self-reinforcing and bidirectional — poor sleep may lead to episodic onset, which may also lead to worsening (or shortening) sleep bouts.

Given the importance of sleep in the ongoing management of this illness, accurate consumer-grade alternatives to polysomnography (considered the gold standard of sleep tracking) have emerged over the last few years. Indeed, comparatively inexpensive sleep tracking technologies like the Oura Ring have dramatically improved the quality of information that can be used to augment and inform these self-monitoring activities. Objective sensor-based tracking technology can be complemented with subjective self-report measures in order to form a more complete picture of physical and mental health across time. Given the aforementioned interplay of sleep and mood, this combination of subjective and objective tracking creates the possibility of longitudinal analysis — and potentially deepens one's capacity for self-awareness.

Following four years of consistent sleep and mood tracking, I sought to more formally interpret the data I had collected to quantify what I had previously intuited: that certain mood states could be understood (and potentially even predicted) by recent sleep trends. Indeed, this intuition has been demonstrated quantitatively in existing literature (Bose et al., 2017; Moshe et al., 2021; Jafarlou

et al., 2023). As this work also demonstrates, combining data from consumer wearable technology and subjective self-report logs allows for a more comprehensive picture of health.

I will first describe the vector autoregression (VAR) method and subsequent tests, namely the Granger causality test and an impulse response analysis, that were performed to achieve these goals.

First, I will describe the methods used to achieve these goals, providing an overview of vector autoregression, Granger causality, and impulse response functions. Next, I will detail the findings of these methods on the dataset. This work concludes with a discussion of the methods and their potential applications in future work.

2 Problem setup

A multivariate time series analysis was performed using a vector autoregressive (VAR) model fit using ordinary least squares. An optimal lag order was first obtained using a combination of Akaike Information Criterion (AIC), Bayesian Information Criterion (BIC), Hannan-Quinn Information Criterion (HQIC), and final prediction error (FPE). After fitting a VAR(2) model on the multiple time series data (outlined below), a Granger causality test was performed in order to assess the predictive relationships between variables. Finally, an impulse response analysis was plotted to further explore the temporal relationships between variables, specifically between sleep, heartrate variability, and self-reported mood. I will outline these analysis steps in greater detail in the sections that follow.

2.1 Vector Autoregression

(Lütkepohl, 2005)

A VAR(p) model for a multivariate time series is a regression model for outcomes at time t and time lagged predictors, with p indicating the lag. Given $p = 1$, the model would be concerned with one observation prior to t . As noted by Seabold and Perktold (2010), a $T \times K$ multivariate time series (where T is the number of observations and K is the number of variables) can be modeled using a p -lag VAR model, notated as

$$Y_t = \nu + A_1 Y_{t-1} + \dots + A_p Y_{t-p} + u_t$$

$$u_t \sim \text{Normal}(0, \Sigma_u)$$
(1)

where A_i is a $K \times K$ coefficient matrix.

The vector autoregressive (VAR) model is a flexible method for the analysis of causality in this setting.

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2.2 Granger Causality

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2.3 Impulse Response Analysis

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3 Experimental Results

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3.1 Dataset Description

The sleep score dataset was created using the second- and third-generation Oura Ring. The proprietary Oura sleep score is on a scale of 1 to 100 and incorporates a variety of sensor-based measures (i.e., heartrate variability, resting heartrate, body temperature) across time. Although the specifics of this algorithm are not public, the Oura Ring has been found to produce accurate measures of sleep timing and heartrate variability when compared against polysomnography (de Zambotti et al., 2019). As detailed in Table 1, my use of the Oura Ring was consistent across time. The dataset contains 1,455 nights of sleep bout data occurring between February, 2019 and March, 2023.

Each day at 4:30pm I received a notification prompting me to log my subjective state in eMood Tracker, a mobile application for iOS. eMood Tracker is "recommended by psychologists, therapists, and social workers" and is intended to "track symptom data relating to Bipolar I and II disorders" (eMo, 2023). The version used through this period contains preset mood categories (depressed, irritable, anxious, and elevated) and allow users to log the presence and intensity on a scale of 0 to

	Value
Total nights	1455
Missing nights	1
Mean	73.82
SD	12.36
Max	97.00
Min	30.00

Table 1: Descriptive statistics of Oura Ring sleep score data

EMA Categories	Count
irritable	100
anxious	88
depressed	103
elevated	48

Table 2: Count of days where EMA item contains a non-zero value

3, where 0 is "not present" and 3 is "severe". The resulting dataset contains the most severe mood state per day. The contents of this dataset are outlined in Table 2.

3.2 Data Analysis

All analysis were performed in Python version 3.11.0 (Pyt) using Pandas 1.5.3 (The pandas development team, 2020) for data preprocessing and statsmodels 0.13.5 (Seabold and Perktold, 2010) for modeling.

3.3 Stationarity, Decomposition, and Autocorrelation

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3.4 Lag Order Selection

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SLEEP AND MOOD

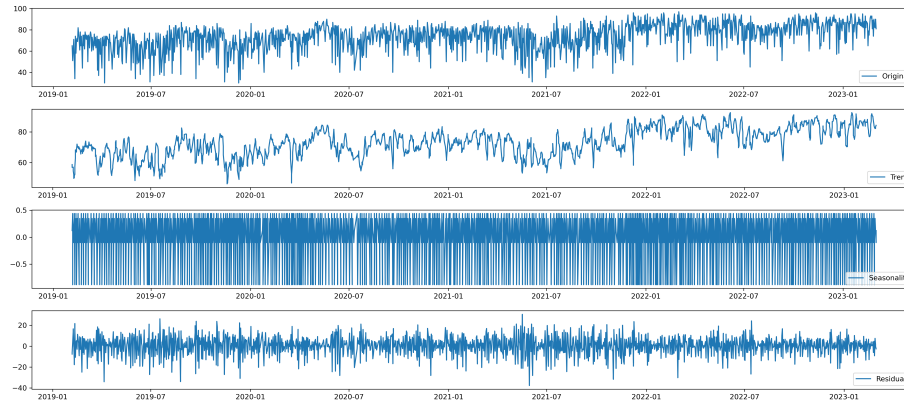


Figure 1: Decomposition of sleep time series

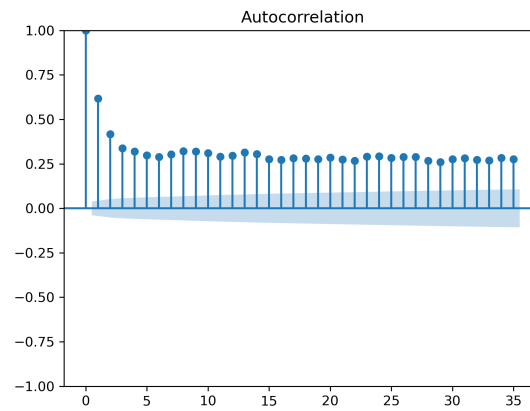


Figure 2: Autocorrelation of sleep time series

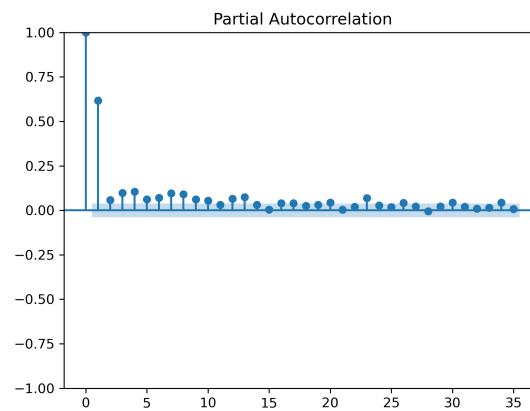


Figure 3: Partial autocorrelation of sleep time series

	AIC	BIC	FPE	HQIC
0	1.688	1.708	5.408	1.695
1	-0.02482	0.09412*	0.9755	0.01979*
2	-0.03545*	0.1826	0.9652*	0.04635
3	-0.03417	0.2830	0.9664	0.08481
4	-0.02907	0.3872	0.9714	0.1271
5	-0.02537	0.4900	0.9750	0.1680
6	-0.01701	0.5975	0.9832	0.2135
7	-0.01940	0.6943	0.9809	0.2483
8	-0.01014	0.8026	0.9900	0.2948
9	-0.0008049	0.9111	0.9993	0.3413
10	0.01201	1.023	1.012	0.3913
11	0.02510	1.135	1.026	0.4415
12	0.03723	1.246	1.038	0.4909
13	0.04867	1.357	1.050	0.5395
14	0.06022	1.468	1.063	0.5882
15	0.07076	1.577	1.074	0.6359

Table 3: VAR Order Selection (* highlights the minimum)

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3.5 Vector Autoregression Model

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	coefficient	std. error	t-stat	prob
L1.score	0.633262	0.027574	22.966	0.000
L1.anxious	0.153275	0.446110	0.344	0.731
L1.depressed	0.477164	0.409130	1.166	0.243
L1.irritable	-0.282988	0.412509	-0.686	0.493
L1.elevated	-0.220198	0.655784	-0.336	0.737
L2.score	-0.003080	0.027452	-0.112	0.911
L2.anxious	0.353528	0.445359	0.794	0.427
L2.depressed	1.241873	0.409667	3.031	0.002
L2.irritable	-0.080069	0.412341	-0.194	0.846
L2.elevated	-0.499540	0.657230	-0.760	0.447

Table 4: VAR results for equation score

Causal Variable	Variable	Test statistic	Critical value	p-value	df
sleepscore	depressed	5.384	2.997	0.005	(2, 6535)
sleepscore	anxious	3.294	2.997	0.037	(2, 6535)
sleepscore	irritable	1.347	2.997	0.260	(2, 6535)
sleepscore	elevated	1.203	2.997	0.500	(2, 6535)

Table 5: Granger Causality Test for Sleep Score

3.6 Granger Causality

3.7 Impulse Response Analysis

4 Discussion

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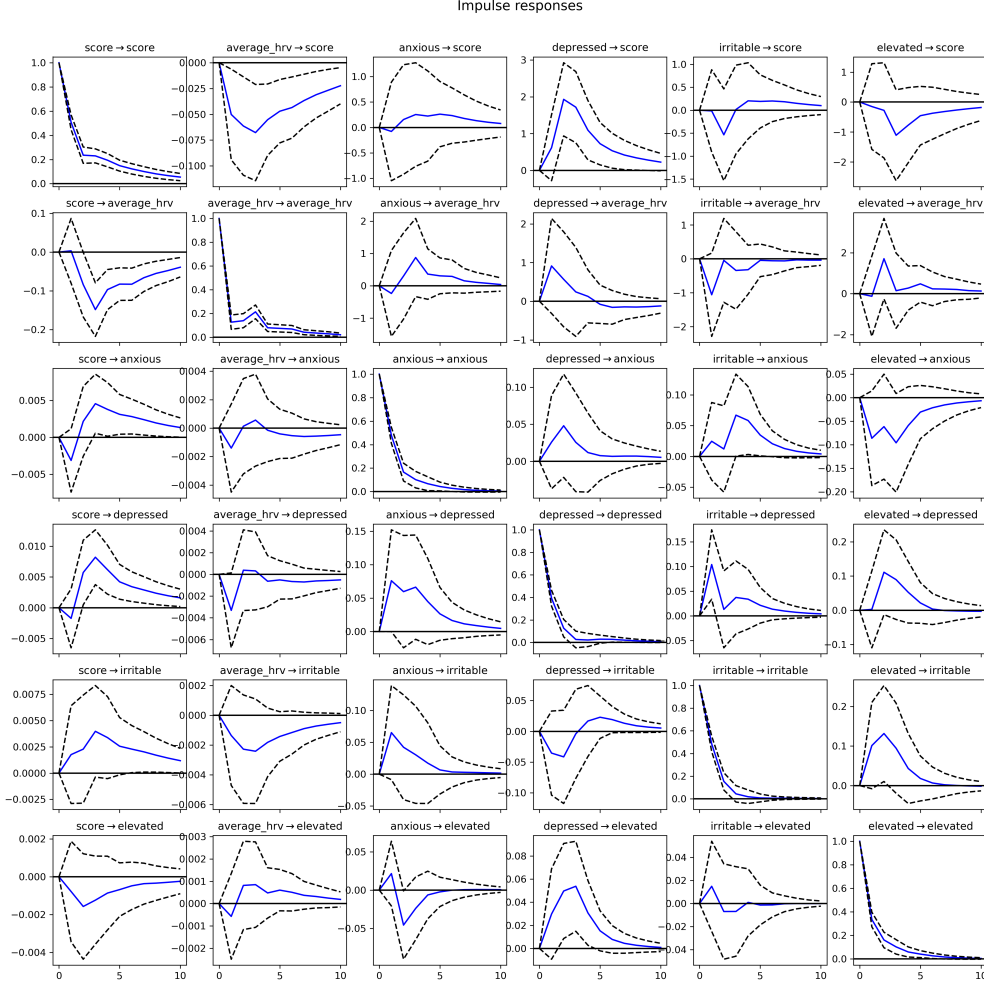


Figure 4: Plot of Impulse Response Function, Lag 0 to 10

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