HASKELL SYNTAX AND STATIC SEMANTICS WRITTEN IN K-FRAMEWORK

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BY

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THESIS

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ABSTRACT

Haskell Context Free Syntax, Preprocessing, Context Sensitive Checks, and Type Inferencing in K.

Subject Keywords: at least one subject keyword here; separate keywords with semicolons

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To my parents, for their love and support.

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INTRODUCTION

In the first progress report, I will detail what I learned about K and the motivation for specifying languages in K, along with Haskell and the goal of my project. A current problem with engineered systems is that the design of the system is not proven to be working. The system could be non-functional at design time. The designer may not fully understand the system environment or may have not considered the behavior of the system in rare circumstances. Then once the design is made, there may be bugs introduced by implementing the design incorrectly. The current way that programs are created is by making a design or a formal specification of the program, implementing it, and testing the program against unit tests or verifying the behavior of the program after the fact. Formal methods are ways to mathematically prove correctness of a system. Without formal methods, the only way to reason about a system is by testing it against different edge cases. Within the context of a programming language, one way a programming language can be formally specified is by defining a syntax and semantics for that language. The operational semantics of a programming language can be thought of as a transition system upon an abstract syntax tree, which is the program itself written in the language, and a state, which is a function from the variables in the tree to the current values of those variables. This way, real and complex programs written in natural looking programming languages can be interpreted as strings written in formal languages. Once a programming language is defined in this way, certain properties and behavior of the language and programs written in the language can be proven. K is a framework for creating the formal specification of a programming language. It then can interpret programs written in the language by running only the rules of the formal operational semantics of the programming language. This allows programs to be ran and analyzed formally. This way the formal specification of the complex programming language can be tested and analyzed with the use of a machine. A K-configuration defines the memory structure of the programming language, made up of cells. The program state can be thought of as the current values of the K-configuration at a certain point in time. Grammar can be written in K using the constructor syntax, and a semantic rule can be written in K using the constructor rule. Haskell is a purely functional programming language with strong static typing. Purely functional means that the language only allows the user to make functions whose output is only dependant on the function input. Strong static typing means that before a program is run, a type inference algorithm checks the program and ensures that all functions and function applications are allowed with regards to the types of the inputs and outputs. Static refers to the fact that type inference is performed before the code is ran, and will not run during the runtime of the code. Strong typing refers to the fact that the compiler will not allow the user to perform workarounds like typecasting. My goal for this project is to write the syntax of Haskell and the type system of Haskell in K.

CONTEXT FREE SYNTAX

The Haskell 2010 report is the current official specification of the Haskell language. The grammar specified in section 10.5 of the Haskell 2010 report is a specification of the expanded syntax of haskell. As specified in section 2.7, the expanded syntax of haskell specifies haskell programs when written using semicolons and braces. However, these can be omitted in a real haskell program. The compiler will then utilize layout rules for certain grammar structures instead. These are specified in section 10.3 The parser that I have written in K does not implement these layout rules and instead only can parse the expanded, layout insensitive syntax of haskell. It would require another script to convert a program written using the layout sensitive syntax into the expanded syntax in order to parse the program. Haskell has a context free grammar. Section 10.1 specifies the notation used in the grammar. The notation of 10.1 are always in bold in the grammar. So

```
qvarid \rightarrow [\mod id . ] varid
```

Means that modid . is optional, and the brackets [] are not part of the haskell code, but the period . is part of the haskell code. Any symbol that is not in bold needs to be written in the program in order to parse correctly. There are a lot of parts of the grammar that were tricky for me to implement in K. For instance, a sort definition with an optional part could be just written using a — in the K syntax. So

```
qvarid -> [ modid . ] varid
```

Is written in my K syntax as

```
syntax \ \ QVarId \ ::= \ \ VarId \ \ | \ \ ModId \ \ "." \ \ VarId \ \ [ \ klabel ( \ 'qVarIdCon ) ]
```

However, an issue arises when you have something written like

```
data [context =>] simpletype [= constrs] [deriving]
```

As an option for the definition of the topdecl sort. What I did was, for each optional part, replace the optional part with a new sort. For instance,

I replaced [context $= \[\vdots \]$] with a new sort called OptContext. Then I just specified

I ran into another issue where a program with a variable called size did not parse. I found out that this is because size is a k keyword. So I just specified that a variable could be a variable token, or size.

I ran into an issue where floats and integers did not parse correctly. They caused parsing errors due to ambiguity of parsing. For example the number 123.45 had ambiguity where the parser did not know if 1, 12, or 123 where integers, and if 5 was an integer, or if the entire thing was one float. Normally in K, different tokens are separated with whitespaces. However, for some reason the parser had difficulty here. Initially, I added a workaround by requiring parentheses around each integer and floating point. f y z (2) This fixed the issue.

```
syntax Literal ::= IntFloat | CusChar | CusString
syntax TyCon ::= ConId
syntax ModId ::= ConId | ConId "." ModId [klabel('conModId)]
syntax QTyCon ::= TyCon | ModId "." TyCon [klabel('conTyCon)]
syntax QVarId ::= VarId | ModId "." VarId [klabel('qVarIdcon)]
syntax QVarSym ::= VarSym | ModId "." VarSym [klabel('qVarSymCon)]
syntax QConSym ::= ConSym | ModId "." ConSym [klabel('qConSymCon)]

** syntax QTyCls ::= QTyCon
syntax TyCls ::= ConId
```

```
syntax TyVars ::= List{TyVar, ""} [klabel('typeVars)] //used in SimpleType syntax
syntax TyVar ::= VarId
\mathtt{syntax} \ \mathtt{TyVarTuple} \ ::= \ \mathtt{TyVar} \ \mathtt{"} \ \mathtt{,"} \ \mathtt{TyVar}
                                                   [klabel('twoTypeVarTuple)]
                       TyVar "," TyVarTuple [klabel('typeVarTupleCon)]
syntax QVar::= QVarId | "(" QConSym ")" [klabel('qVarBracket)]
syntax QCon ::= QTyCon | "(" GConSym ")" [klabel('gConBracket)]
syntax QConOp ::= GConSym | "'" QTyCon "'"
                                                      [klabel('qTyConQuote)]
\operatorname{syntax} \ \operatorname{QVarOp} \ ::= \ \operatorname{QVarSym} \ | \ \ " \cdot " \ \ \operatorname{QVarId} \ " \cdot "
                                                      [klabel('qVarIdQuote)]
syntax VarOp ::= VarSym | " " VarId " " syntax ConOp ::= ConSym | " " ConId " "
                                                       [klabel('varIdQuote)]
                                                      [klabel('conIdQuote)]
syntax GConSym ::= ":" | QConSym
syntax Vars ::= Var
                | Var "," Vars [klabel('varCon)]
syntax VarsType ::= Vars "::" Type [klabel('varAssign)]
\operatorname{syntax} Ops ::= Op
| Op "," Ops [klabel('opCon)]
syntax Fixity ::= "infixl" | "infixr" | "infix"
\mathtt{syntax}\ \mathrm{Op}\ ::=\ \mathrm{VarOp}\ |\ \mathrm{ConOp}
syntax CQName ::= Var | Con | QVar
/* syntax QConId ::= ConId | ModId "." ConId */
syntax QOp ::= QVarOp | QConOp
syntax ModuleName ::= "module" ModId [klabel('moduleName)]
syntax Module ::= ModuleName "where" Body
                                                             [klabel ('module)]
                   | ModuleName Exports "where" Body [klabel('moduleExp)]
                                                             [klabel ('moduleBody)]
syntax Body ::= "{" ImpDecls ";" TopDecls "}" [klabel('bodyimpandtop)]
                | "{" ImpDecls "}" [klabel('bodyimpdecls)]
                 | "{" TopDecls "}" [klabel('bodytopdecls)]
syntax ImpDecls ::= List{ImpDecl, ";"} [klabel('impDecls)]
```

The sort that contains all the other sorts is a module. A module represents one complete Haskell program. It can have either a name and a body, a name and a body with exports, or just a body.

```
module Foo where
{import Bar
}
```

This example program has a Module with only ImpDecls. It has one ImpDecl.

import Bar

This example program has a Module with no name and only ImpDecls. It has one ImpDecl.

```
"(" CQList ")" [klabel('cqListBracket)]
                       //Liyi: a check needs to place in preprocessing to check
                       //\operatorname{if} the CQList is a cname list or a quar list.
                    [\ \ ""\ [\ onlyLabel\ ,\ \ klabel\ (\ 'emptyOptCNameList\ )\ ]
syntax CQList ::= List{CQName, ","}
syntax ImpDecl ::= "import" OptQualified ModId OptAsModId OptImpSpec [klabel('impDecl)]
                  | "" [onlyLabel, klabel('emptyImpDecl)]
syntax OptQualified ::= "qualified"
                      "" [onlyLabel, klabel('emptyQualified)]
\mathtt{syntax} \;\; \mathsf{OptAsModId} \;\; ::= \;\; \mathtt{"as"} \;\; \mathsf{ModId}
                    ,, ,,
                             [onlyLabel, klabel('emptyOptAsModId)]
{\tt syntax} \ {\tt OptImpSpec} \ ::= \ {\tt ImpSpec}
                    | ""
                              [onlyLabel, klabel('emptyOptImpSpec)]
syntax ImpSpecKey ::= "(" ImportList OptComma ")"
syntax ImpSpec ::= ImpSpecKey
                 | "hiding" ImpSpecKey
syntax ImportList ::= List {Import, ","}
syntax Import ::= Var
               | TyCon CQList
syntax TopDecls ::= List{TopDecl, ";"} [klabel('topdeclslist)]
syntax TopDecl ::= Decl [klabel('topdecldecl)]
                 > "type" SimpleType "=" Type [klabel('type)]
                  "data" OptContext SimpleType OptConstrs OptDeriving [klabel('data)]
                    "newtype" OptContext SimpleType "=" NewConstr OptDeriving [klabel('newtype)]
                  "class" OptContext ConId TyVar OptCDecls [klabel('class)]
                    "instance" OptContext QTyCon Inst OptIDecls [klabel('instance)]
                    "default" Types [klabel('default)]
                  | "foreign" FDecl [klabel('foreign)]
```

The main types of expressions in Haskell are TopDecls - Top Declarations. A top declaration can either be a type, a data, a newtype, a class, an instance,

a default, a foreign, or an arbitrary declaration.

```
syntax FDecl ::= "import" CallConv CusString Var "::" FType
                | "import" CallConv Safety CusString Var "::" FType
                | "export" CallConv Safety CusString Var "::" FType
//Liyi: fdecl needs to use special function in preprocessing
// to get the actually elements from the impent and expent from the CusString
//did string analysis
syntax Safety ::= "unsafe" | "safe"
syntax CallConv ::= "ccall" | "stdcall" | "cplusplus" | "jvm" | "dotnet"
\mathtt{syntax} \ \mathtt{FType} \ ::= \ \mathtt{FrType}
                | FaType "->" FType // unsure about this one syntax is ambiguous UNFINISHED
\operatorname{syntax} \operatorname{FrType} ::= \operatorname{FaType}
                | "()"
syntax FaType ::= QTyCon ATypeList
//define declaration.
syntax OptDecls ::= "where" Decls | "" [onlyLabel, klabel('emptyOptDecls)]
syntax Decls ::= "{" DeclsList "}" [klabel('decls)]
syntax DeclsList ::= List{Decl, ";"} [klabel('declsList)]
syntax Decl ::= GenDecl
               | FunLhs Rhs [klabel('declFunLhsRhs)]
               | Pat Rhs [klabel('declPatRhs)]
syntax OptCDecls ::= "where" CDecls | "" [onlyLabel, klabel('emptyOptCDecls)]
syntax CDecls ::= "{" CDeclsList "}"
syntax CDeclsList ::= List{CDecl, ";"}
```

```
syntax CDecl ::= GenDecl
                | FunLhs Rhs
                | Var Rhs
syntax OptIDecls ::= "where" IDecls | "" [onlyLabel, klabel('emptyOptIDecls)]
syntax IDecls ::= "{" IDeclsList "}"
syntax IDeclsList ::= List{IDecl, ";"} [klabel('ideclslist)]
syntax IDecl ::= FunLhs Rhs [klabel('cdeclFunLhsRhs)]
                | Var Rhs [klabel('cdeclVarRhs)]
                "" [onlyLabel, klabel('emptyIDecl)]
svntax GenDecl ::= VarsType
                  | Vars "::" Context "=>" Type [klabel('genAssignContext)]
                  | Fixity Ops
                  | Fixity Integer Ops
                  "" [onlyLabel, klabel('emptyGenDecl)]
//three optional data type for the TopDecl data operator.
//deriving data type
syntax OptDeriving ::= Deriving | "" [onlyLabel, klabel('emptyDeriving)]
syntax Deriving ::= "deriving" DClass | "deriving" "(" DClassList ")"
syntax DClassList ::= List{DClass, ","}
syntax DClass ::= QTyCon
syntax FunLhs ::= Var APatList [klabel('varApatList)]
                | Pat VarOp Pat [klabel('patVarOpPat)]
                 "(" FunLhs ")" APatList [klabel('funlhsApatList)]
syntax Rhs ::= "=" Exp OptDecls [klabel('eqExpOptDecls)]
             | GdRhs OptDecls [klabel('gdRhsOptDecls)]
syntax GdRhs ::= Guards "=" Exp
               | Guards "=" Exp GdRhs
syntax Guards ::= "|" GuardList
syntax GuardList ::= Guard | Guard "," GuardList [klabel('guardListCon)]
syntax Guard ::= Pat "<-" InfixExp
               | "let" Decls
                | InfixExp
//definition of exp
syntax Exp ::= InfixExp
             > InfixExp "::" Type [klabel('expAssign)]
              | InfixExp "::" Context "=>" Type [klabel('expAssignContext)]
syntax InfixExp ::= LExp
                   > "-" InfixExp [klabel('minusInfix)]
                   > LExp QOp InfixExp
\operatorname{syntax} LExp ::= AExp
              > "\" APatList "->" Exp [klabel('lambdaFun)]
| "let" Decls "in" Exp [klabel('letIn)]
               | "if" Exp OptSemicolon "then" Exp OptSemicolon "else" Exp [klabel('ifThenElse)]
               "case" Exp "of" "{" Alts "}" [klabel('caseOf)]
| "do" "{" Stmts "}" [klabel('doBlock)]
               //| FExp
//syntax FExp ::= AExp | FExp AExp
syntax OptSemicolon ::= ";" | "" [onlyLabel, klabel('emptySemicolon)]
syntax OptComma ::= "," | "" [onlyLabel, klabel('emptyComma)]
 syntax OptWhereDecls ::= "where" Decls | ""
syntax AExp ::= QVar [klabel('aexpQVar)]
               | GCon [klabel('aexpGCon)]
               | Literal [klabel('aexpLiteral)]
              > AExp AExp [left , klabel('funApp)]
              > QCon "{" FBindList "}"
               | AExp "{" FBindList "}" //aexp cannot be qcon UNFINISHED
                       //Liyi: first, does not understand the syntax, it is the Qcon {FBindlist}
                        //or QCon? Second, place a check in preprosssing.
```

```
//and also check the Fbindlist here must be at least one argument
             > "(" Exp ")"
                                  [bracket]
              | "(" ExpTuple ")"
               "[" ExpList "]"
               "[" Exp OptExpComma ".." OptExp "]"
              "[" Exp "|" Quals "]"
              "(" InfixExp QOp ")"
              | "(" QOp InfixExp ")" //{\rm qop} cannot be - (minus) UNFINISHED
                       //Livi: place a check here to check if QOp is a minus
{\tt syntax\ OptExpComma\ ::=\ ","\ Exp\ |\ ""\ [onlyLabel,\ klabel('emptyExpComma)]}
syntax OptExp ::= Exp | "" [onlyLabel, klabel('emptyExp)]
syntax ExpList ::= Exp | Exp "," ExpList [right]
                                           [right, klabel('twoExpTuple)]
syntax ExpTuple ::= Exp "," Exp
                 | Exp "," ExpTuple
                                          [right, klabel('expTupleCon)]
//constr datatypes
syntax OptConstrs ::= "=" Constrs [klabel('nonemptyConstrs)] | "" [onlyLabel, klabel('emptyConstrs)]
                   ::= Constr [klabel('singleConstr)] | Constr "|" Constrs [klabel('multConstr)]
syntax Constrs
                   ::= Con OptBangATypes [klabel('constrCon)] // (arity con = k, k 0) UNFINISHED
syntax Constr
                    | SubConstr ConOp SubConstr
                     | Con "{" FieldDeclList "}"
\mathtt{syntax} \ \ \mathsf{NewConstr} \qquad ::= \ \ \mathsf{Con} \ \ \mathsf{AType} \ \ [ \ \mathtt{klabel} \ ( \ \ \mathsf{newConstrCon} \, ) \, ]
                    | Con "{" Var "::" Type "}"
syntax SubConstr ::= BType | "!" AType
syntax FieldDeclList ::= List{FieldDecl, ","}
syntax FieldDecl ::= VarsType
                   | Vars "::" "!" AType
syntax OptBangATypes ::= List{OptBangAType, ""} [klabel('optBangATypes)]
syntax \ OptBangAType ::= \ OptBang \ AType \ [\ klabel('optBangAType')]
syntax \ OptBang ::= "!" \ | \ "" \ [onlyLabel, \ klabel('emptyBang)]
syntax OptContext ::= Context "=>" | "" [onlyLabel, klabel('emptyContext)]
syntax Context ::= Class
                 | "(" Classes ")"
syntax Classes ::= List{Class, ","}
syntax SimpleClass ::= QTyCon TyVar [klabel('classCon)]
syntax Class
                   ::= SimpleClass
                     | QTyCon "(" TyVar ATypeList ")"
                          //Liyi: a check in preprossing to check if the Atype list is empty
                          //it must have at least one item
//define type and simple type
syntax SimpleType ::= TyCon TyVars [klabel('simpleTypeCon)]
syntax Type ::= BType
             | BType "->" Type [klabel('typeArrow)]
syntax BType ::= AType
              | BType AType [klabel('baTypeCon)]
syntax ATypeList ::= List{AType, ""} [klabel('atypeList)]
syntax AType ::= GTyCon
                                             [klabel('atypeGTyCon)]
                                             [klabel('atypeTyVar)]
                 TyVar
                 "(" TypeTuple ")"
                                             [klabel('atypeTuple)]
               | "[" Type "]"
| "(" Type ")"
                                             [klabel('tyList)]
                                             [bracket]
syntax TypeTuple ::= Type "," Type
                                            [right, klabel('twoTypeTuple)]
                  | Type "," TypeTuple
                                             [klabel('typeTupleCon)]
syntax Types ::= List{Type, ","}
syntax GTyCon ::= QTyCon
                | GConCommon
                | "(->)"
```

```
syntax GCon ::= GConCommon
               | QCon
//inst definition
\mathtt{syntax} \ \mathtt{Inst} \ ::= \ \mathtt{GTyCon}
                | "(" GTyCon TyVars ")" //TyVars must be distinct UNFINISHED
| "(" TyVarTuple ")" //TyVars must be distinct
                | "[" TyVar "]" [klabel('tyVarList)]
| "(" TyVar "->" TyVar ")" //TyVars must be distinct
//pat definition
syntax Pat ::= LPat QConOp Pat
             | LPat
syntax LPat ::= APat
              "-" IntFloat
                                    [klabel('minusPat)]
                GCon APatList [klabel('lpatCon)]//arity gcon = k UNFINISHED
syntax APatList ::= APat | APat APatList [klabel('apatCon)]
syntax APat ::= Var [klabel('apatVar)]
                | Var "@" APat
                | GCon
                | QCon "{" FPats "}"
                | Literal [klabel('apatLiteral)]
                | "(" Pat ")" [bracket]
| "(" PatTuple ")"
                | "[" PatList "]"
| "~" APat
syntax PatTuple ::= Pat "," Pat [klabel('twoPatTuple)] | Pat "," PatTuple [klabel('patTupleCon)]
syntax PatList ::= Pat
                  | Pat "," PatList
                                            [klabel('patListCon)]
syntax FPats ::= List{FPat, ","}
syntax FPat ::= QVar "=" Pat
//definition of quals
syntax Quals ::= Qual | Qual "," Quals [klabel('qualCon)]
syntax Qual ::= Pat "<-" Exp
              | "let" Decls
               | Exp
//definition of alts
syntax Alts ::= Alt | Alt ";" Alts
syntax Alt ::= Pat "->" Exp [klabel('altArrow)]
             | Pat "->" Exp "where" Decls
              "" [onlyLabel, klabel('emptyAlt)]
//definition of stmts
syntax Stmts ::= StmtList Exp OptSemicolon
syntax StmtList ::= List{Stmt, ""}
syntax Stmt ::= Exp ";"
               | Pat "<-" Exp ";"
               l "let" Decls ";"
//definition of fbind
syntax FBindList ::= List {FBind, ","}
syntax FBind ::= QVar "=" Exp
```

CONFIGURATION

```
requires "haskell-syntax.k"
module HASKELL-CONFIGURATION
   imports HASKELL-SYNTAX
   syntax KItem ::= "startImportRecursion"
   syntax KItem ::= callInit(K)
   //syntax KItem ::= initPreModule(K) [function]
   //\operatorname{syntax} KItem ::= tChecker(K) [function]
   configuration
       <T>
           <k> $PGM: ModuleList ~> startImportRecursion </k>
           <tempModule> .K </tempModule>
           <tempCode> .K </tempCode>
           <typeIterator> 1 </typeIterator>
           <tempAlpha> .K </tempAlpha>
           <tempAlphaMap> .Map </tempAlphaMap>
           <tempBeta> .Map </tempBeta>
           <tempT> .K </tempT>
           <tempDelta> .Map </tempDelta>
           <tempAlphaStar> .K </tempAlphaStar>
           <tempBetaStar> .K </tempBetaStar>
           <importTree> .List </importTree>
           <recurImportTree> .List </recurImportTree>
           <impTreeVMap> .Map </impTreeVMap>
           <modules> //static information about a module
               <module multiplicity = "*">
                   <moduleName> .K </moduleName>
                   <moduleAlphaStar> .K </moduleAlphaStar>
                   <moduleBetaStar> .K </moduleBetaStar>
                   <moduleImpAlphas> . List </moduleImpAlphas>
                   <moduleTempCode> .K </moduleTempCode>
                   <imports> . Set </imports>
                   <classes> //static information about a module
                       <class multiplicity="*">
                          <className> .K </className>
                       </class>
                   </classes>
               </module>
           </modules>
       </T>
```

endmodule

CONTEXT SENSITIVE CHECKS

I also placed the user defined types into data structures in order to perform several checks to make sure that the user did not have errors when creating types. Then the data structures will be transformed into a form that will be used for type inferencing. Section 4 of the Haskell 2010 report specifies the haskell type system. In the topdecl sort, there are three typecons that are used to create user defined datatypes. Data, type, and newtype. The end goal is to put the user defined types into a data structure which I can use to perform type inferencing. These three typecons are used to create user defined types. The first one is type, type simpletype = type This is used in a haskell program to declare a new type as a single type. In effect, it renames the type where both names now can be used to refer to the type. type Username = String Is one such example usage of type, it creates a new type Username, which is defined as just a string. Now the programmer can refer to Username or String to make a string. The second one is data,

```
data [context =>] simpletype [= constrs] [deriving]
```

This allows a user to declare a new type that may include many fields, and polymorphic types. For instance: data Date = Date Int Int Int This is a new type that includes the typecon Date followed by three integers. data Poly a = Number a This is a new polymorphic type with polymorphic parameter a, that has the typecon Number. The third one is newtype,

```
newtype [context =>] simpletype = newconstr [deriving]
```

This is very similar to data except it only parses when the newtype has only one typecon and one field.

I perform several checks here, 1. The programmer should not be able to make two user defined datatypes with the same name, even if one is created using data and another is created using type for instance. 2. The programmer should not be able to use the same typecons when making different options for their types or use the same typecons for different types. 3. There should

be no cycles in type renaming using type, and the type renaming chains using type should terminate with a type defined with data or newtype. 4. The argument sorts for types defined using data or newtype should be types that exist. 5. The polymorphic parameters that appear on the right hand side of a data declaration need to appear on the left hand side as well. 6. The polymorphic parameters that appear on the left hand side of a data declaration need to be unique. I implemented a map, called alpha, of new type names as the keys and their declared types as the entries. I then collected all appearances of the typecon type in the program, and put simpletype -; type in the alpha map. However, one of the things I needed to check for in the program was whether a user declared multiple definitions with type, so I could not use a map in K because they only allow unique keys with unique entries. So I initially used a set of tuples, and then changed it to a map after checking for multiple type declarations.

The second data structure I made is called T. T holds the user defined types created using data and newtype.

```
\label{eq:syntax} \begin{array}{lll} \text{Syntax} & \text{KItem} & ::= & \text{TList}(K) \\ \text{$//$ list} & \text{of $T$ objects for every new type introduced by data and newtype} \\ & \text{syntax} & \text{KItem} & ::= & \text{TObject}(K,K,K) \\ \text{$//$ (type name, entire list of poly type vars, list of inner $T$ pieces)} \\ & \text{syntax} & \text{KItem} & ::= & \text{InnerTPiece}(K,K,K,K,K) \\ \text{$//$ (type constructor, poly type vars, argument sorts, entire constr block, type name)} \end{array}
```

T is a list of TObjects, each TObject represents a single user defined datatype. It holds the name, the list of polymorphic parameters, and a list of inner T pieces. An inner T piece represents an option of what a type could be. It consists of a type constructor, a list of polymorphic parameters required for this option, the fields for this option, the entire subtree of the AST for this option unedited, and the type name again. I then used these data structures to perform these checks, and afterwards will transform them into a new data structure to perform type inferencing.

```
//
requires "haskell-syntax.k"
requires "haskell-configuration.k"

module HASKELL-PREPROCESSING
   imports HASKELL-SYNTAX
   imports HASKELL-CONFIGURATION

   //USER DEFINED LIST
   //definition of ElemList

   //syntax KItem ::= ElemList
   syntax ElemList ::= List{Element,","} [strict]

// syntax Int ::= lengthOfList(ElemList) [function]

// rule lengthOfList(.ElemList) => 0

// rule lengthOfList(val(K:K),L:ElemList) => 1 +Int lengthOfList(L)
```

```
rule lengthOfList(valValue(K:K),L:ElemList) => 1 +Int lengthOfList(L)
          \mathtt{syntax} \ \mathtt{Element} \ ::= \ \mathtt{val} \, (\mathtt{K}) \ [\, \mathtt{strict} \, ]
          syntax ElementResult ::= valValue(K)
          syntax Element ::= ElementResult
          syntax KResult ::= ElementResult
          rule val(K: KResult) => valValue(K) [structural]
          //form ElemList
               \mathtt{syntax} \ \mathtt{ElemList} \ ::= \ \mathtt{formElemList}(K) \ [\, \mathtt{function} \, ]
          //CONVERT ~> TO List
          //list convert
               syntax List ::= convertToList(K) [function]
               \texttt{rule convertToList}\,(\,.K) \;\Longrightarrow\; .\; L\, i\, s\, t
               rule convertToList(A:KItem ~> B:K) => ListItem(A) convertToList(B)
          syntax KItem ::= dealWithImports(K,K)
          \texttt{rule} \  \, <\texttt{k} > \  \, \texttt{'modListSingle} \, (\, \texttt{'module} \, (\texttt{A} : \texttt{K}, \, , \, \, \texttt{B} : \texttt{K})) \  \, = > \  \, \texttt{dealWithImports} \, (\texttt{A}, \texttt{B}) \, \, \ldots < / \, \texttt{k} > \, \, \texttt{(A,B)} \, \, \ldots < / \, \texttt{k} > \, \, \texttt{(A,B)} \, \, \ldots < / \, \texttt{k} > \, \, \texttt{(A,B)} \, \, \ldots < / \, \texttt{(A,B)} \, \ldots < / \, \texttt{(A,B)} \, \, \ldots < / \, \texttt{(A,B)
          (.Bag =>
                                                         //DOT DOT DOT MEANS OVERWRITE ONLY SOME OF THE DEFAULTS
                         <module>...
                               <moduleName> A </moduleName>
                  \dots < / \text{module} >
          (.Bag =>
                                                         //DOT DOT DOT MEANS OVERWRITE ONLY SOME OF THE DEFAULTS
                         <module > ...
                               <moduleName> A </moduleName>
                  ... < / module>
//
              rule dealWithImports(Mod:K, A:K) => callInit(A)
               \texttt{rule} \  \, <\!\! k\!\! > \  \, \texttt{dealWithImports}\left(\texttt{Mod:K}, \  \, A\!:\!K\right) \  \, =\!\!\! > \  \, \texttt{callInit}\left(A\right) \  \, \ldots <\!\! / \, k\!\! >
          \texttt{rule} \  \, <\!\! k\!\! > \  \, \texttt{dealWithImports}\left(\texttt{Mod}\!:\!K, \quad \!\!\! \text{'bodyimpandtop}\left(A\!:\!K, \,, \quad B\!:\!K\right)\right) \  \, =\!\!\!\!> \  \, .K \ \ldots <\!\!/\,k\!\!>
                    <importTree> L: List => L importListConvert(Mod, A) </importTree>
                    <moduleName> Mod </moduleName>
                    < imports > S : Set \ (.Set \implies SetItem (A)) < / imports >
                    <moduleTempCode> OldTemp:K => B </moduleTempCode>
          rule < k > dealWithImports(Mod:K, 'bodyimpdecls(A:K)) => .K ... < /k >
                    <importTree> L: List => L importListConvert(Mod, A) </importTree>
                    <recurImportTree> L:List => L importListConvert(Mod, A) </recurImportTree>
                    <moduleName> Mod </moduleName>
                    <imports> S:Set (.Set => SetItem(A)) </imports>
               rule <k> dealWithImports(Mod:K, 'bodytopdecls(A:K)) => callInit(A) ... </k>
          \texttt{rule} \  \, <\!\! k\!\!> \  \, \texttt{dealWithImports}\left(\texttt{Mod}\!:\!K, \quad \text{'bodytopdecls}\left(B\!:\!K\right)\right) \  \, =\!\!\!> \  \, .K \  \, \ldots <\!\! \, / \, k\!\!>
                    <moduleName> Mod </moduleName>
                    //importlist convert
          syntax List ::= importListConvert(K,K) [function]
          \mathtt{syntax} \ \mathsf{KItem} \ ::= \ \mathsf{impObject}\left(\mathsf{K}, \mathsf{K}\right)
          rule importListConvert(Name:K, 'impDecls(A:K,, Rest:K)) => importListConvert(Name, A) importListConvert(Name,
          rule \ importListConvert (\ 'moduleName (Name : K) \ , \ \ 'impDecl (A : K, \ , \ Modid : K, \ , \ C : K, \ , \ D : K)) \ => \ ListItem (impObject (Name \ , \ Modid : K, \ , \ C : K, \ , \ D : K))
          rule importListConvert(Name:K, .ImpDecls) => .List
```

/*NEW TODO ALGORITHM

1. Construct tree for module inclusion

```
2. Check tree for cycles
3. Go to each leaf and recursively go up the tree and build alpha* and beta* for the types of the module and the c
(and specify scoping) (desugar the scope so that each type specifies the scope) */
        syntax KItem ::= "checkImportCycle"
        syntax KItem ::= "recurseImportTree"
            rule <k> performNextChecks
                           => checkUseVars
                                  ~> (checkLabelUses
                                  ~> (checkBlockAddress(.K)
                                 ~> (checkNoNormalBlocksHavingLandingpad(.K, TNS -Set TES)
                                 {\it `>~(checkAllExpBlocksHavingLandingpad\,(.K,~TES)}
                                  > (checkAllExpInFromInvoke(.K, TES)
                                 ~> (checkLandingpad
                                 ~> checkLandingDomResumes)))))) ... </k> */
        rule <k> startImportRecursion => checkImportCycle
                                                                               > (recurseImportTree)...</k>
        syntax \ KItem ::= \ cycleCheck(K, Map, List \ , List) \ [function] \ // current \ node, \ map \ of \ all \ nodes \ to \ visited \ or \ not \ , \ standard \ , \ standard \ )
        {\tt syntax \ Map ::= \ createVisitMap (List , Map) \ [function] \ //graph \,, \ visitmap}
        syntax KItem ::= getUnvisitedNode(K,K, Map) [function] //visitmap
        syntax \ List ::= \ getNodeNeighbors(K, List) \ [function] \ //visitmap
        rule <k> checkImportCycle
                          \Rightarrow cycleCheck (.K, createVisitMap(I, .Map), .List, I) ... </k>
                  <importTree> I:List </importTree>
                  <\!\!\operatorname{impTreeVMap}\!\!> \ \operatorname{.Map} \ =\!\!\!> \ \operatorname{createVisitMap}\left(\operatorname{I} \ , \ \ \operatorname{.Map}\right) \ <\!\!/\operatorname{impTreeVMap}\!\!>
        syntax KItem ::= "visited"
        syntax KItem ::= "unvisited"
        syntax KItem ::= "none"
        \texttt{rule} \quad \texttt{createVisitMap} \, (\, \texttt{ListItem} \, (\, \texttt{impObject} \, (A:K,B:K)) \,) \quad \texttt{Rest} : \texttt{List} \,\, , \,\, M:Map)
                           \Rightarrow createVisitMap(Rest, M[A <- unvisited][B <- unvisited])
        rule createVisitMap (.List, M:Map) => M
        \texttt{rule getUnvisitedNode}\left(.\,\text{K}, \ .\,\text{K}, \ .\,\text{Map}\right) \; \Longrightarrow \; \texttt{none}
        \texttt{rule getUnvisitedNode} (.K, .K, (A:K \mid -> B:K) \ M:Map)
                      => getUnvisitedNode(A, B, M)
        \texttt{rule getUnvisitedNode}(A\!:\!KItem\,,\ \texttt{unvisited}\,\,,\,\,M\!:\!Map) \implies A
        \verb"rule" getUnvisitedNode(A:KItem", visited", M:Map")
                        => getUnvisitedNode(.K, .K, M)
        rule getNodeNeighbors(Node:K,.List) => .List
        {\tt rule \ getNodeNeighbors}\,(\,.\,K,\,Rest\,{:}\,List\,) \;\Longrightarrow\;.\,List
        rule getNodeNeighbors(Node:KItem,ListItem(impObject(Node,B:KItem)) Rest:List) => getNodeNeighbors(Node, Rest)
        rule \ getNodeNeighbors(Node:KItem,ListItem(impObject(A:KItem,B:KItem)) \ Rest:List) \implies getNodeNeighbors(Node, \ Rest:List) \implies getNodeNeighbors(No
                   requires Node =/=K A
        \texttt{rule cycleCheck(none, M:Map, .List, L:List)} \; = \!\!\!> \; .K
        \texttt{rule cycleCheck} \ (.K, \ M: Map, \ ListItem \ (Node: K) \ S: List \ , \ I: List ) \ \Longrightarrow \ cycleCheck \ (Node \ , \ M, \ S, \ I)
        rule cycleCheck(Node:K, M:Map, S:List, I:List)
                                   => \ \operatorname{cycleCheck}\left(.\,\operatorname{K},\ \operatorname{M}[\operatorname{Node} <- \ \operatorname{visited}\ ]\,,\ \operatorname{getNodeNeighbors}\left(\operatorname{Node},\operatorname{I}\right)\ \operatorname{S},\ \operatorname{I}\right)
                   requires Node =/=K .K andBool Node =/=K none
        rule cycleCheck (.K, M:Map, ListItem (Node:K) S:List, I:K) => cycleCheck (Node, M, S, I)
                   requires S =/=K . List
        rule cycleCheck\left(A:K,.K,.K,I:K\right) \implies cycleCheck\left(A,createVisitMap\left(I,.Map\right),.List,I\right)
        rule cycleCheck(Node:K, M:Map, S:List, I:K) => cycleCheck(.K, M[Node <- visited], getNodeNeighbors(Node,I) S,
         rule cycleCheck (.K, M:Map, ListItem (Node:K) S:List, I:K) => cycleCheck (Node, M, S, I)
```

//rule cycleCheck(.K, M:Map, .K, ListItem(impObject(A:K,B:K)) Rest:List) => cycleCheck(ListItem(impObject(A:K,B:K))

```
//COPY IMPORT GRAPH, NEED SECOND GRAPH FOR RECURSING, ADDITIONAL GRAPH FOR SELECTING IMPORTS FOR ALPHA* AND BETA*
//DFS for leaf
//acquire alpha and beta for leaf
//merge alpha and beta with imports to produce alpha \ast and beta \ast
//perform checks
//perform inferencing
//insert alpha* and beta* into importing modules
//remove all edges pointing to leaf
       syntax KItem ::= "leafDFS"
       syntax KItem ::= "getAlphaAndBeta"
       syntax KItem ::= "getAlphaBetaStar"
       syntax KItem ::= "performIndividualChecks"
       syntax KItem ::= "performIndividualInferencing"
       syntax KItem ::= "insertAlphaBetaStar"
       syntax KItem ::= "removeAllEdges"
       syntax KItem ::= "seeIfFinished"
       rule <k> recurseImportTree => leafDFS
                                                              ~> (getAlphaAndBeta
                                                              //~> (getAlphaBetaStar
                                                              ~> (performIndividualInferencing))...</k>
//rule <k> dealWithImports(Mod:K, 'bodytopdecls(A:K)) => callInit(A) ... </k>
          rule <k> leaf
                          \Rightarrow cycleCheck (.K, createVisitMap(I, .Map), .List,I) ... </k>
                    <importTree> I:List </importTree>
syntax \ KItem ::= \ returnLeafDFS(K,List\,,Map) \ [function] \ // current \ node \,, \ map \ of \ all \ nodes \ to \ visited \ or \ not \,, \ stack \ function \ func
       syntax KItem ::= innerLeafDFS(K, List) [function]
       syntax KItem ::= loadModule(K)
       rule <k> leafDFS
                      \Rightarrow returnLeafDFS(.K,I,M) ... </k>
                <recurImportTree> I:List </recurImportTree>
                <\!\!\operatorname{impTreeVMap}\!\!> \, \operatorname{M:Map} \, <\!\!\operatorname{/impTreeVMap}\!\!>
       rule returnLeafDFS(.K, ListItem(impObject(Node:KItem,B:KItem)) I:List,M:Map) => returnLeafDFS(B,I,M)
       rule \ returnLeafDFS (Node: KItem \,, I: List \,, M: Map) \ => \ returnLeafDFS (innerLeafDFS (Node, I) \,, I \,, M)
                requires innerLeafDFS(Node, I) =/=K none
       rule returnLeafDFS(Node:KItem, I:List, M:Map) => loadModule(Node)
                \texttt{requires innerLeafDFS} \, (\, \texttt{Node} \, , \, \texttt{I} \, ) \, = \!\!\! - \!\!\! \texttt{K} \, \, \texttt{none}
       \texttt{rule innerLeafDFS}(\texttt{Node}:\texttt{KItem},\texttt{ListItem}(\texttt{impObject}(\texttt{Node},\texttt{B}:\texttt{KItem})) \quad \texttt{I}:\texttt{List}) \implies \texttt{B}
       rule \ innerLeafDFS (Node: KItem \,, ListItem \, (impObject \, (A: KItem \,, B: KItem \,)) \quad I: List \,) \ \Rightarrow \ innerLeafDFS \, (Node \,, I)
                requires Node =/=K A
       \verb"rule" innerLeafDFS(Node:KItem", . List) \implies \verb"none"
         returnLeafDFS(Node:KItem, ListItem(impObject(Node,B:KItem)) I:List,M:Map) => returnLeafDFS(B,I,M)
//call before Checker Code
          \texttt{rule} \  \, <\!\! k\!\! > \  \, \texttt{callInit}\left(S\!:\!K\right) \  \, =\!\!\! > \  \, \texttt{initPreModule}\left(S\right) \  \, \ldots <\!\! / \, k\!\! >
                    <tempModule> A:K => S </tempModule>
       rule \langle k \rangle loadModule(S:KItem) \Rightarrow .K ... \langle k \rangle
                <tempModule> A:K => S </tempModule>
       rule <k> getAlphaAndBeta => initPreModule(Code) ... </k>
                <tempModule> Mod:KItem </tempModule>
                <moduleName> 'moduleName(Mod) </moduleName>
                <moduleTempCode> Code:KItem </moduleTempCode>
```

```
//get alpha and beta
                         \mathtt{syntax} \ \mathsf{KItem} \ ::= \ \mathsf{Module} \left( \mathsf{K}, \ \mathsf{K} \right)
                         syntax KItem ::= preModule(K,K) //(alpha, T)
                         // STEP 1 CONSTRUCT T AND ALPHA
                         // alpha = type
                         // T = newtype and data, temporary data structure
                         \mathtt{syntax} \ \mathsf{KItem} \ ::= \ \mathsf{initPreModule}\left(\mathsf{K}\right) \ [\, \mathsf{function} \,]
                         syntax \hspace{0.1in} KItem \hspace{0.1in} ::= \hspace{0.1in} getPreModule\hspace{0.1in} (K, \hspace{0.1in} K) \hspace{0.1in} [\hspace{0.1in} function\hspace{0.1in}] \hspace{0.1in} //(\hspace{0.1in} Current \hspace{0.1in} term\hspace{0.1in}, \hspace{0.1in} premodule)
                         syntax KItem ::= makeT (K,K,K,K)
                         syntax KItem ::= fetchTypes (K,K,K,K)
                         syntax List ::= makeInnerT (K,K,K) [function] //LIST
                         \mathtt{syntax} \ \mathtt{List} \ ::= \ \mathtt{getTypeVars}(\mathtt{K}) \ [\, \mathtt{function} \, ] \ \ // \mathtt{LIST}
                         syntax KItem ::= getCon(K) [function]
                         syntax List ::= getArgSorts(K) [function] //LIST
                         syntax KItem ::= AList(K)
                         syntax KItem ::= AObject(K,K) //(1st -> 2nd) map without idempotency
                         \mathtt{syntax} \ \mathsf{KItem} \ ::= \ \mathsf{ModPlusType} (\mathsf{K}, \mathsf{K})
                         \operatorname{syntax} \ \operatorname{KItem} \ ::= \ \operatorname{TList}(K) \ // \operatorname{list} \ \operatorname{of} \ \operatorname{T} \ \operatorname{objects} \ \operatorname{for} \ \operatorname{every} \ \operatorname{new} \ \operatorname{type} \ \operatorname{introduced} \ \operatorname{by} \ \operatorname{data} \ \operatorname{and} \ \operatorname{newtype}
                         syntax \ KItem ::= TObject(K,K,K,K) \ //(module \ name, \ type \ name, \ entire \ list \ of \ poly \ type \ vars \, , \ list \ of \ inner \ T \ picks of 
                         syntax \ KItem ::= InnerTPiece (K,K,K,K,K) \ //(type \ constructor \, , \ poly \ type \ vars \, , \ argument \ sorts \, , \ entire \ constr \ block of the constructor \, , \ block of the c
                                     rule \ initPreModule (\ 'module (\ I : Module Name , \ , \ J : K)) \ \Rightarrow \ getPreModule (\ J , preModule (\ A List (\ . \ List ) , T List (\ . \ List )))
                                     rule \ initPreModule(\ 'moduleExp(I:ModuleName,\ ,\ L:K,\ ,\ J:K)) \ \Rightarrow \ getPreModule(\ J,\ preModule(\ AList(\ .\ List)\ ,\ TList(\ 
                                     rule \ initPreModule(\ 'moduleBody(\ J:Body)) \ \Rightarrow \ getPreModule(\ J, preModule(\ AList(\ .List), TList(\ .List)))
                         rule initPreModule(J:K) => getPreModule(J, preModule(AList(.List), TList(.List)))
                         \texttt{rule getPreModule('bodytopdecls(I:K), J:K)} \; \Rightarrow \; \texttt{getPreModule(I,J)}
                         rule getPreModule('topdeclslist('type(A:K,, B:K),, Rest:K),J:K) => fetchTypes(A,B,Rest,J) //constructalpha
                         rule \ getPreModule ('topdeclslist ('data (A:K, , B:K, , C:K, , D:K) , , Rest:K) , J:K) \implies makeT (B, C, Rest , J)
                         rule \ getPreModule (\ 'topdeclslist \ (\ 'newtype (A:K, , \ B:K, , \ C:K, , \ D:K) \ , , \ Rest:K) \ , J:K) \ \Longrightarrow \ makeT (B,C,Rest \ , J)
                         rule \ getPreModule (\ 'topdeclslist (\ 'topdecldecl (A:K) \ , \ Rest : K) \ , J : K) \ \Longrightarrow \ getPreModule (\ Rest \ , J)
                         rule \ getPreModule ('topdeclslist ('class (A:K, , B:K, , C:K, , D:K) , , \ Rest : K) , J:K) \ \Rightarrow \ getPreModule (Rest , J) \
                         rule \ getPreModule (\ 'topdeclslist (\ 'instance (A:K, , \ B:K, , \ C:K, , \ D:K) \ , , \ Rest : K) \ , \\ J:K) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \ , J) \ \Longrightarrow \ getPreModule (\ Rest \
                         rule \ getPreModule('topdeclslist('default(A:K,, B:K,, C:K,, D:K),, Rest:K), J:K) \Rightarrow getPreModule(Rest,J)
                         rule \ getPreModule ('topdeclslist ('foreign (A:K, , B:K, , C:K, , D:K) , , Rest:K) , J:K) \implies getPreModule (Rest, J) \implies g
                         rule getPreModule (.TopDecls, J:K) => J
                         //rule getPreModule('module(I:ModuleName,L:K, J:K)) => preModule(J)
                         rule <\!\!k\!\!> fetch Types ('simple TypeCon(I:TyCon,, H:TyVars), 'atypeG TyCon(C:K), Rest:K, preModule(AList(M:List), L:Lunder, M:List), L:Lunder, M:List(M:List), L:Lunder, M:List(M:List), L:Lunder, M:List(M:List), L:Lunder, M:List(M:List), L:Lunder, M:List(M:List), L:Lunder, M:Lunder, M:List(M:List), L:Lunder, M:List(M:List), M
                                                       <tempModule> ModName: KItem </tempModule>
                         rule <k> makeT('simpleTypeCon(I:TyCon,, H:TyVars), D:K, Rest:K, preModule(AList(M:List), TList(ListInside:List
                                                      <\!\!\operatorname{tempModule}\!\!> \operatorname{ModName}\!:\!\operatorname{KItem} \ <\!\!/\operatorname{tempModule}\!\!>
                         rule makeInnerT(A:K,B:K, 'nonemptyConstrs(C:K)) \implies makeInnerT(A,B,C)
                         rule \ \ makeInnerT(A:K,B:K,\ `multConstr(C:K,\ D:K)) \ \ \Rightarrow \ \ ListItem(InnerTPiece(getCon(C),getTypeVars(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C),getArgSorts(C)
                         \texttt{rule getTypeVars}\left(\,\,'\,\texttt{constrCon}\left(A\!:\!K,\,,\;\;B\!:\!K\right)\right) \;=\!>\; \texttt{getTypeVars}\left(B\right)
                         \verb|rule| | \verb|getTypeVars('optBangATypes(A:K,, Rest:K))| => \verb|getTypeVars(A)| | \\ \verb|getTypeVars(Rest)| |
                         \verb|rule| | \verb|getTypeVars('optBangAType('emptyBang(.KList),, | Rest:K))| => | \verb|getTypeVars(Rest)| |
                         rule getTypeVars('atypeGTyCon(A:K)) \Rightarrow .List
                         \texttt{rule getTypeVars('atypeTyVar(A:K))} \implies \texttt{ListItem(A)}
                         \verb"rule" getTypeVars(.OptBangATypes) => .List
                         //rule getCon('emptyConstrs()) => .K
                         //rule getCon('nonemptyConstrs(A:K)) => getCon(A)
                          rule getCon('constrCon(A:K,, B:K)) => A
```

```
//rule getArgSorts('constrCon(A:K,, B:K)) => B
        \texttt{rule getArgSorts('constrCon(A:K,, B:K))} \implies \texttt{getArgSorts(B)}
        \texttt{rule getArgSorts('optBangATypes(A:K,, Rest:K))} \implies \texttt{getArgSorts(A) getArgSorts(Rest)}
        \texttt{rule getArgSorts('optBangAType('emptyBang(.KList),, Rest:K))} \implies \texttt{getArgSorts(Rest)}
        rule getArgSorts('atypeGTyCon(A:K)) => ListItem(A)
        rule getArgSorts('atypeTyVar(A:K)) => .List
        rule getArgSorts(.OptBangATypes) \Rightarrow .List
rule <k> preModule(A:K,T:K) => startTTransform ... </k>
                  <tempAlpha> OldAlpha:K => A </tempAlpha>
                  <tempT> OldT:K \Rightarrow T </tempT>
// STEP 2 PERFORM CHECKS
        syntax KItem ::= "error"
        syntax KItem ::= "startChecks"
        syntax KItem ::= "checkNoSameKey"
               //Keys of alpha and keys of T should be unique
        \mathtt{syntax} \ \ \mathsf{KItem} \ ::= \ "\mathtt{checkTypeConsDontCollide}"
                //Make sure typeconstructors do not collide in T
        syntax KItem ::= "makeAlphaMap"
                //make map for alpha
        syntax KItem ::= "checkAlphaNoLoops"
                //alpha check for no loops
                //check alpha to make sure that everything points to a T
        syntax KItem ::= "checkArgSortsAreTargets"
                      //Make sure argument sorts [U] [W,V] are in the set of keys of alpha and targets of T, (keys of T)
        syntax KItem ::= "checkParUsed"
//NEED TO CHECK all the polymorphic parameters from right appear on left. RIGHT SIDE ONLY
//NEED TO CHECK UNIQUENESS FOR POLY PARAM ON LEFT SIDE ONLY
            rule \langle k \rangle preModule(A:K,T:K) => startChecks ... \langle /k \rangle
                      <tempAlpha> OldAlpha:K => A </tempAlpha>
//
//
                      <tempT> OldT:K \Rightarrow T </tempT>
            rule <k> performNextChecks
                           => checkUseVars
                                 ~> (checkBlockAddress(.K)
                                 {\it `>~(checkNoNormalBlocksHavingLandingpad\,(.K,~TNS~-Set~TES)}
                                  > (checkAllExpBlocksHavingLandingpad(.K, TES)
                                > (checkAllExpInFromInvoke(.K, TES)
                                 > (checkLandingpad
                                 \sim checkLandingDomResumes)))))) ... </k> */
        rule <k> startChecks
                           => checkNoSameKev
                                 ~> (checkTypeConsDontCollide
                                 ~> (makeAlphaMap
                                \sim (checkAlphaNoLoops
                                 \sim (checkArgSortsAreTargets
                                 ~> (checkParUsed))))) ... </k>
        rule <k> checkTypeConsDontCollide
                          => tyConCollCheck(T,.List,.Set) ... </k>
                  <tempT> T:K </tempT>
        //\operatorname{syntax} KItem ::= tChecker(K) [function]
        syntax \hspace{0.2cm} KItem \hspace{0.2cm} ::= \hspace{0.2cm} tyConCollCheck (K,K,K) \hspace{0.2cm} [\hspace{0.2cm} function \hspace{0.2cm}] \hspace{0.2cm} //(\hspace{0.2cm} TList \hspace{0.2cm}, List \hspace{0.2cm} of \hspace{0.2cm} Tycons \hspace{0.2cm}, Set \hspace{0.2cm} of \hspace{0.2cm} Tycons)
        syntax KItem ::= lengthCheck(K,K) [function]
        //\operatorname{syntax} \ KItem \ ::= \ \operatorname{tyConCollCheck}\left(K,K,K\right) \ [\, \operatorname{function}\, ]
        //syntax K ::= innerCollCheck(K) [function]
        // \, syntax \ K \ ::= \ tyConCollCheckPasser(K, \ K) \ [\, function \, ]
        //\text{rule } \text{ } \text{tChecker}(\text{preModule}(\text{Alpha}:\text{Map},\text{T}:\text{K},\text{Mod}:\text{K})) \\ \Rightarrow \text{tyConCollCheck}(\text{innerCollCheck}(\text{T}),\text{preModule}(\text{Alpha},\text{T},\text{Mod})) \\ = \text{tyConCollCheck}(\text{T}) \\ = \text
        //rule tyConCollCheck(.K, preModule(Alpha:Map,H:K,Mod:K)) => tyConCollCheck(innerCollCheck(H), preModule(Alpha,H
```

```
rule tyConCollCheck(TList(ListItem(TObject(ModName:K, A:K,B:K,ListItem(InnerTPiece(Ty:K,E:K,F:K,H:K,G:K)) Inne
                                                                                rule \ tyConCollCheck(TList(ListItem(TObject(ModName:K, A:K,B:K,. \ List)) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(TObject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(TObject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(TObject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(TObject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(TObject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(TObject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(Tobject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(Tobject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), J:List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(Tobject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), List, D:Set) = \\ rule \ tyConCollCheck(TList(ListItem(Tobject(ModName:K, A:K,B:K,. \ List))) \ Rest:List), List, List, List, List), List, List) = \\ rule \ tyConCollCheck(TList(ListItem(Tobject(ModName:K, A:K,B:K,B:K,. \ List))) \ Rest:List), List, List, List, List, List), List, List,
                                                                               tyConCollCheck(TList(Rest),J,D)
rule tyConCollCheck(TList(.List), J:List, D:Set) =>
                                                                              lengthCheck(size(J),size(D))
rule lengthCheck(A:Int, B:Int) => .K
                                                                                \texttt{requires} \ A == \!\!\!\! = \!\!\!\! \texttt{Int} \ B
rule lengthCheck(A:Int, B:Int) => error
                                                                               requires A =/=Int B
//\operatorname{rule} \ \operatorname{tyConCollCheck}(\operatorname{TList}(\operatorname{TObject}(A:K,B:K,C:K) \ \tilde{\ } > \operatorname{Rest}:K) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{innerCollCheck}(A:K,B:K,C:K) \ \tilde{\ } > \operatorname{Rest}:K) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ \tilde{\ } > \operatorname{Rest}:K) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ \tilde{\ } > \operatorname{Rest}:K) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ \tilde{\ } > \operatorname{Rest}:K) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{TList}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheck}(A:K,B:K,C:K) \ ) \ , J:K) \ \Rightarrow \ \operatorname{tyConCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerCollCheckPasser}(\operatorname{InnerColl
syntax KItem ::= keyCheck(K,K,K,K) [function] //(Alpha, T, List of names, Set of names)
rule <k> checkNoSameKey
                                           \Rightarrow keyCheck(A, T, .Set, .List) ... </k>
                       <tempAlpha> A:K </tempAlpha>
                       <\!\!\operatorname{tempT}\!\!> \, T\!:\!K \,<\!\!/\!\operatorname{tempT}\!\!>
//rule <k> checkAlphaNoSameKey
                                                     =>~akeyCheck\,(\,.\,K,~.\,Set\,)~\dots</\,k>
rule keyCheck(AList(ListItem(AObject(A:K,B:K)) C:List), T:K, D:Set, G:List) => keyCheck(AList(C), T, SetItem(A
rule keyCheck(AList(.List), TList(ListItem(TObject(ModName:K, A:K,B:K,C:K)) Rest:List), D:Set, G:List) => keyC
rule \;\; keyCheck(\;AList\;(\;.\;List\;)\;,\;\; TList\;(\;.\;List\;)\;,\;\; D:Set\;,\;\; G:List\;) \;\; \Rightarrow \;\; lengthCheck\;(\;size\;(G)\;,\; size\;(D)\;)
syntax KItem ::= makeAlphaM(K,K) [function] //(Alpha, AlphaMap)
\mathtt{syntax} \ \ \mathsf{KItem} \ ::= \ \mathsf{tAlphaMap}(\mathsf{K}) \ \ //(\,\mathsf{AlphaMap}) \ \ \mathsf{temp} \ \ \mathsf{alphamap}
\verb|rule| < k > makeAlphaMap|
                                           => makeAlphaM(A, .Map) ... < / k>
                       <tempAlpha> A:K </tempAlpha>
rule makeAlphaM(AList(ListItem(AObject(A:K,B:K)) C:List), M:Map) => makeAlphaM(AList(C), M[A <- B])
rule makeAlphaM(AList(.List), M:Map) => tAlphaMap(M)
rule < k > tAlphaMap(M:K) => .K ... < /k >
                       <tempAlphaMap> OldAlphaMap:K => M </tempAlphaMap>
        syntax KItem ::= tkeyCheck(K,K,K) [function] //(T,List of T,Set of T)
         rule <k> checkTNoSameKey
                                                      \Rightarrow tkeyCheck(T, .Set, T) ... </k>
                                  <tempT> T:K </tempT>
         rule tkeyCheck(TList(ListItem(TObject(A:K,B:K,C:K)) Rest:List), D:Set, G:K) => tkeyCheck(TList(Rest), SetItem
          \texttt{rule tkeyCheck}(\texttt{TList}(\texttt{.List}), \texttt{D:Set}, \texttt{TList}(\texttt{G:List})) \implies \texttt{lengthCheck}(\texttt{size}(\texttt{G}), \texttt{size}(\texttt{D}))
syntax \hspace{0.1cm} KItem \hspace{0.1cm} ::= \hspace{0.1cm} aloopCheck \hspace{0.1cm} (K,K,K,K,K,K,K) \hspace{0.1cm} [\hspace{0.1cm} function\hspace{0.1cm}] \hspace{0.1cm} //(\hspace{0.1cm} (Alpha\hspace{0.1cm},\hspace{0.1cm} List \hspace{0.1cm} of \hspace{0.1cm} Alpha\hspace{0.1cm},\hspace{0.1cm} Set \hspace{0.1cm} of \hspace{0.1cm} Alpha\hspace{0.1cm},\hspace{0.1cm} CurrNode\hspace{0.1cm},\hspace{0.1cm} lengthcheck\hspace{0.1cm} (Alpha\hspace{0.1cm},\hspace{0.1cm} List \hspace{0.1cm} of \hspace{0.1cm} Alpha\hspace{0.1cm},\hspace{0.1cm} Set \hspace{0.1cm} of \hspace{0.1cm} Alpha\hspace{0.1cm},\hspace{0.1cm} CurrNode\hspace{0.1cm},\hspace{0.1cm} lengthcheck\hspace{0.1cm} (Alpha\hspace{0.1cm},\hspace{0.1cm} List \hspace{0.1cm} of \hspace{0.1cm} Alpha\hspace{0.1cm},\hspace{0.1cm} Set \hspace{0.1cm} of \hspace{0.1cm} Set \hspace{
rule <k> checkAlphaNoLoops
                                            => aloopCheck(A, List, Set, K, K, T, Set) ... </k>
                        <tempAlphaMap> A:K </tempAlphaMap>
                       <\!\!\operatorname{tempT}\!\!> \, T\!:\!K \,<\!\!/\!\operatorname{tempT}\!\!>
//aloopCheck set and list to check cycles
rule \ aloopCheck(Alpha:Map \ (A:KItem \ | -> \ B:KItem) \ , \ D:List \ , \ G:Set \ , \ .K, \ .K, T:K, S:Set) \ \Longrightarrow \ aloopCheck(Alpha \ , \ ListItem) \ , \ L
rule aloopCheck(Alpha:Map (H |-> B:KItem), D:List, G:Set, H:KItem, .K,T:K,S:Set) => aloopCheck(Alpha, ListItem
rule \ aloopCheck(Alpha:Map, \ D: List \ , \ G: Set \ , \ H: KItem \ , \ .K, T:K, S: Set) \ => \ aloopCheck(Alpha \ , \ .List \ , \ .Set \ , \ .K, \ length Control \ , \ .K, \ lengt
                          requires (notBool H in keys(Alpha)) andBool (H in typeSet(T, .Set) orBool H in S)
rule aloopCheck(Alpha:Map, D:List, G:Set, H:KItem, .K,T:K,S:Set) => error //terminal alpha rename is not in Tl
                         requires (notBool H in keys(Alpha)) andBool (notBool (H in typeSet(T, .Set) orBool H in S))
syntax Set ::= typeSet(K,K) [function] //(K, KSet)
rule \ typeSet(TList(ListItem(TObject(ModName:K, \ A:K,B:K,C:K)) \ Rest:List) \, , \ D:Set) \ \Rightarrow \ typeSet(TList(Rest) \, , \ SetItem(TObject(ModName:K, \ A:K,B:K,C:K)) \, ) \, . \\
```

rule typeSet(TList(.List), D:Set) => D

```
rule aloopCheck(Alpha:Map, D:List, G:Set, H:KItem, .K) => keys(Alpha) ~> H
                                                                    requires notBool H in keys(Alpha)
                         \texttt{rule aloopCheck(.Map, .List, .Set, .K, .K, T:K, S:Set)} \implies .K
                                   rule aloopCheck(AList(Front:List ListItem(AObject(H,B:K)) C:List), D:List, G:Set, H:ConId) => aloopCheck(AList(BistItem(ADbject(H,B:K)) C:List), D:List, G:Set, H:ConId) => aloopCheck(AList(BistItem(BistItem(ADbject(H,B:K)) C:List), D:List, G:Set, H:ConId) => aloopCheck(AList(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistItem(BistIt
                                    syntax \ \ KItem ::= \ TList(K) \ //list \ of \ T \ objects \ for \ every \ new \ type \ introduced \ by \ data \ and \ new type
                                    syntax \ \ KItem ::= \ TObject(K,K,K) \ \ //(type \ name, \ entire \ list \ of \ poly \ type \ vars, \ list \ of \ inner \ T \ pieces)
                                    syntax \ \ KItem ::= \ InnerTPiece(K,K,K,K,K) \ \ //(type \ constructor \, , \ poly \ type \ vars \, , \ argument \ sorts \, , \ entire \ constructor \, b \ \ b \ \ constructor \, )
//Make sure argument sorts [U] [W,V] are in the set of keys of alpha and targets of T, (keys of T)
                         syntax KItem ::= argSortCheck(K,K,K) [function] //(T,AlphaMap)
                         rule <k> checkArgSortsAreTargets
                                                                               => \ \operatorname{argSortCheck} \left( \operatorname{T}, \operatorname{A}, \operatorname{typeSet} \left( \operatorname{T}, . \operatorname{Set} \right) \right) \ \ldots < / \operatorname{k} >
                                                      <tempAlphaMap> A:K </tempAlphaMap>
                                                     <\!\!\operatorname{tempT}\!\!> \, T\!:\! K \,<\!\!/\!\operatorname{tempT}\!\!>
                         rule \ argSortCheck (TList(ListItem)(TObject(ModName:K,\ A:K,B:K,ListItem)(InnerTPiece(C:K,D:K,ListItem)(Arg:KItem)) \ ArgCortCheck(TList(ListItem)(TObject(ModName:K,\ A:K,B:K,ListItem)(InnerTPiece(C:K,D:K,ListItem)(Arg:KItem)) \ ArgCortCheck(TList(ListItem)(TObject(ModName:K,\ A:K,B:K,ListItem)(InnerTPiece(C:K,D:K,ListItem)(Arg:KItem)) \ ArgCortCheck(TList(ListItem)(TObject(ModName:K,\ A:K,B:K,ListItem)(InnerTPiece(C:K,D:K,ListItem)(Arg:KItem)) \ ArgCortCheck(TList(ListItem)(Arg:KItem)(Arg:KItem)) \ ArgCortCheck(TList(ListItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)) \ ArgCortCheck(TList(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem) \ ArgCortCheck(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem)(Arg:KItem
                                                       requires ((Arg in keys(AlphaMap)) orBool (Arg in Tset))
                         rule - argSortCheck (TList(ListItem(TObject(ModName:K,A:K,B:K,ListItem(InnerTPiece(C:K,D:K,ListItem(Arg:KItem)) - Arg(ListItem(ListItem)) - Arg(ListItem) - 
                                                        requires (notBool ((Arg in keys(AlphaMap)) orBool (Arg in Tset)))
                         rule \ argSortCheck (\ TList (\ ListItem \ (\ TObject (\ ModName: K, A:K, B:K, ListItem \ (\ InnerTPiece \ (C:K, D:K, .\ List \ , E:K, F:K))) \ InnerRecord (\ C:K, D:K, .\ List \ , E:K, F:K))
                         rule argSortCheck(TList(.List), AlphaMap: Map, Tset: Set) => .K
//NEED TO CHECK all the polymorphic parameters from right appear on left. RIGHT SIDE ONLY
//NEED TO CHECK UNIQUENESS FOR POLY PARAM ON LEFT SIDE ONLY
                         syntax \hspace{0.2cm} KItem \hspace{0.2cm} ::= \hspace{0.2cm} parCheck\hspace{0.05cm} (K,K) \hspace{0.2cm} [\hspace{0.2cm} function\hspace{0.1cm} ] \hspace{0.2cm} //(T,AlphaMap)
                         syntax KItem ::= makeTyVarList(K,K,K) [function] //(TyVars, NewList)
                        \mathtt{syntax} \ \mathsf{KItem} \ ::= \ \mathsf{lengthRet}\left(\mathsf{K},\mathsf{K},\mathsf{K}\right) \ [\, \mathsf{function} \,]
                         rule <k> checkParUsed
                                                                              => parCheck(T,.K) ... < / k>
                                                      <tempT> T:K </tempT>
                         //rule makeParLists(TList(ListItem(TObject(A:K, ListItem(Arg:KItem) PolyList:List,C:K)) Rest:List), Tlist:List, T
                         rule - parCheck(\,TList\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,)\,\,,.K) \  \, \Rightarrow \  \, parCheck\,(\,TList\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,) \  \, ,.K) \  \, \Rightarrow \  \, parCheck\,(\,TList\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,) \  \, ,.K) \  \, \Rightarrow \  \, parCheck\,(\,TList\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,) \  \, ,.K) \  \, \Rightarrow \  \, parCheck\,(\,TList\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,) \  \, ,.K) \  \, \Rightarrow \  \, parCheck\,(\,TList\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,(\,ListItem\,(\,TObject\,(ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,(\,ModName\,:K,A:K,B:K,C:K)\,) - Rest:\,List\,(\,ModName\,:K,A:K,B:K,C:K) - Rest:\,List\,(\,ModName\,:K,A:K,
                         rule - parCheck (\ TList (\ List Item \ (\ TObject (\ ModName : K,A : K,B : K,List Item \ (\ Inner TPiece \ (C : K,List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : Li
                                                       parCheck (TList (ListItem (TObject (ModName, A, B, ListItem (InnerTPiece (C, ParRest, D, E, F)) InnerRest)) Rest), NewS
                                                                         requires Par in NewSet
                         rule - parCheck (\ TList (\ List Item \ (\ TObject (\ ModName : K,A : K,B : K,List Item \ (\ Inner TPiece \ (C : K,List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : List Item \ (\ Par : K Item) - ParRest : Li
                                                                         requires notBool (Par in NewSet)
                         rule - parCheck (\ TList (\ List Item \ (\ TObject (\ ModName : K, A : K, B : K, \ List Item \ (\ Inner TPiece \ (C : K, . \ List \ , D : K, E : K, F : K)) - Inner Rest : (C : K, . \ List \ , D : K, E : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, . \ List \ , D : K, E : K, E : K) - (C : K, E : K, E : K) - (C : K, E : K, E : K) - (C : K, E : K, E : K) - (C : K, E : K, E : K) - (C : K, E : K, E : K, E : K) - (C : K, E : K, E : K, E : K) - (C : K, E : K, E : K, E : K) - (C : K, E :
                                                      parCheck(TList(ListItem(TObject(ModName, A, B, InnerRest)) Rest), NewSet)
                         rule \ parCheck (\ TList (\ List Item (\ TObject (\ ModName : K, A : K, B : K, .\ List )) \ Rest : List ) \ , NewSet : Set ) \ => \ rule \ parCheck (\ TList (\ List Item (\ TObject (\ ModName : K, A : K, B : K, .\ List )) \ Rest : List ) \ , NewSet : Set ) \ => \ rule \ parCheck (\ TList (\ List Item (\ TObject (\ ModName : K, A : K, B : K, .\ List )) \ Rest : List ) \ , NewSet : Set ) \ => \ rule \ parCheck (\ TList (\ List Item (\ TList Item 
                                                       parCheck (TList (Rest), NewSet)
                         rule parCheck(TList(.List), NewSet:Set) => .K
                         rule makeTyVarList('typeVars(A:K,, Rest:K), NewList:List, NewSet:Set) => makeTyVarList(Rest, ListItem(A) NewList,
                         rule \ makeTyVarList (.TyVars, NewList: List, NewSet: Set) \implies lengthRet (size (NewList), size (NewSet), NewSet)
                         rule lengthRet(A:Int, B:Int, C:K) \Rightarrow C
                                                                                                                           requires A ==Int B
                         \texttt{rule lengthRet}\left(A\!:\! \texttt{Int} \;,\; B\!:\! \texttt{Int} \;,\; C\!:\! K\right) \;\Longrightarrow\; \texttt{error}
                                                                                                                           requires A =/=Int B
                         //rule argSortCheck(TList(ListItem(TObject(A:K,B:K,C:K)
```

```
// STEP 3 Transform T into beta
                                  syntax KItem ::= "startTTransform"
                                  syntax KItem ::= "constructDelta"
                                  syntax KItem ::= "constructBeta"
                                  rule <k> startTTransform
                                                                                                            => constructDelta
                                                                                                                                        ~> (constructBeta) ... < /k>
                                  rule <k> constructDelta
                                                                                                            \Rightarrow makeDelta(T,.Map) ... < /k>
                                                                           <tempT> T:K </tempT>
                                  \mathtt{syntax} \ \ \mathsf{KItem} \ ::= \ makeDelta(\mathsf{K}, \mathsf{Map}) \ \ [\, \mathsf{function} \, ] \ \ //(\mathsf{T}, \mathsf{Delta})
                                  syntax KItem ::= newDelta(Map) //Delta
                                  syntax KItem ::= newBeta(Map) //beta
                                  syntax List ::= retPolyList(K, List) [function] //(T, Delta)
                                  \texttt{rule} \hspace{0.2cm} \texttt{makeDelta}(\hspace{0.1cm} \texttt{TList}(\hspace{0.1cm} \texttt{ListItem}\hspace{0.1cm} (\hspace{0.1cm} \texttt{TObject}(\hspace{0.1cm} \texttt{ModName}\hspace{0.1cm} : \hspace{0.1cm} \texttt{K}, \texttt{A}\hspace{0.1cm} : \hspace{0.1cm} \texttt{K}, \texttt{C}\hspace{0.1cm} : \hspace{0.1cm} \texttt{K})) \hspace{0.2cm} \hspace{0.1cm} \texttt{Rest} : \texttt{List}\hspace{0.1cm}) \hspace{0.1cm} , \hspace{0.1cm} \texttt{M:Map}) \hspace{0.1cm} = \hspace{0.1cm} \texttt{N:Map} \hspace{0.1cm} \texttt{M:Map} \hspace{0.1cm} = \hspace{0.1cm} \texttt{N:Map} \hspace{0.1cm} \texttt{M:Map} \hspace{0.1cm} \texttt{M:Ma
                                                                           makeDelta\left(\left.TList\left(\left.Rest\right)\right.,M[\left.ModPlusType\left(ModName,A\right)\right.<-\right.\\ size\left(\left.retPolyList\left(\left.Polys\right.,.\right.List\right.)\right)\right]\right)
                                  \verb"rule makeDelta" ( TList ( .List ) , M:Map) \implies \verb"newDelta" (M)
                                  rule \ retPolyList \left( \ 'typeVars \left( A:K, \, ,Rest:K \right), NewList : List \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ ListItem \left( A \right) \ NewList \right) \ = > \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = > \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = > \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = > \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = > \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = > \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = > \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = > \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, \ Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, Rest \, , \, \ Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, Rest \, , \, Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, Rest \, , \, Rest \, , \, Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, Rest \, , \, Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, Rest \, , \, Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, Rest \, , \, Rest \, , \, \ Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, Rest \, , \, Rest \, , \, Rest \, \right) \ = \ retPolyList \left( \, Rest \, , \, Rest \, , \, Rest \, , \, Rest \, \right) \ = \ retPolyList \left( \, Rest
                                  \texttt{rule retPolyList(.TyVars,L:List)} \implies \texttt{L}
                                  rule <k> new Delta (M: Map)
                                                                                                        => .K ... < / k>
                                                                           <tempDelta> OldDelta:K => M </tempDelta>
                                  rule <k> constructBeta
                                                                                                        => makeBeta(T,.Map) ... < /k>
                                                                         <\!\!\operatorname{tempT}\!\!> \, T\!:\!K \,<\!\!/\!\operatorname{tempT}\!\!>
                                  syntax KItem ::= makeBeta(K, Map) [function] //(T, Beta, Delta)
                                  rule - make Beta (\ TList (\ List Item (\ TObject (\ Mod Name : K, A : K, B : K, List Item (\ Inner TPiece (\ Con : K, H : K, D : K, E : K, F : K)) - Inner Rest : Con : K : Mod Name : M
                                                                           makeBeta(TList(ListItem(TObject(ModName,A,B,InnerRest)) \ Rest), Beta[ModPlusType(ModName,Con) < - \ betaParser \\ + \ betaP
                                  \texttt{rule} \hspace{0.2cm} \texttt{makeBeta} \hspace{0.1cm} (\hspace{0.1cm} \texttt{LList} \hspace{0.1cm} (\hspace{0.1cm} \texttt{List} \hspace{0.1cm} ) \hspace{0.1cm} \texttt{Dbject} \hspace{0.1cm} (\hspace{0.1cm} \texttt{ModName} \hspace{0.1cm} : \hspace{0.1cm} \texttt{K}, \texttt{A} \hspace{0.1cm} : \hspace{0.1cm} \texttt{K}, \texttt{List} \hspace{0.1cm} )) \hspace{0.2cm} \hspace{0.1cm} \texttt{Rest} \hspace{0.1cm} : \hspace{0.1cm} \texttt{List} \hspace{0.1cm} ) \hspace{0.1cm} , \hspace{0.1cm} \texttt{Beta} \hspace{0.1cm} : \hspace{0.1cm} \texttt{Map}) \hspace{0.1cm} = \hspace{0.1cm} > \hspace{0.1cm} \texttt{A} \hspace{0.1cm} \texttt{Map} \hspace{0.1cm} = \hspace{0.1cm} \texttt{A} \hspace{0.1cm} \texttt{Map} \hspace{0.1cm} + \hspace{0.1cm} \texttt{A} \hspace{0.1cm} \texttt{A} \hspace{0.1cm} \texttt{Map} \hspace{0.1cm} = \hspace{0.1cm} \texttt{A} \hspace{0.1cm} \texttt{A} \hspace{0.1cm} \texttt{Map} \hspace{0.1cm} = \hspace{0.1cm} \texttt{A} \hspace{0.
                                                                           makeBeta (TList (Rest), Beta)
                                  rule makeBeta(TList(.List),Beta:Map) =>
                                                                            newBeta (Beta)
                                                    rule - makeBeta(TList(ListItem(TObject(ModName:K,A:K,B:K,ListItem(InnerTPiece(C:K,H:K,D:K,E:K,F:K)) - InnerRest: \\ - rule - makeBeta(TList(ListItem(TObject(ModName:K,A:K,B:K,ListItem(InnerTPiece(C:K,H:K,D:K,E:K,F:K))) - InnerRest: \\ - rule - rul
                                                                                              makeBeta (TList (ListItem (TObject (ModName, A, B, InnerRest)) Rest), Beta)
                                  syntax \hspace{0.2cm} KItem \hspace{0.2cm} ::= \hspace{0.2cm} betaParser (K,K,K) \hspace{0.2cm} [\hspace{0.2cm} function \hspace{0.2cm}] \hspace{0.2cm} //(\hspace{0.2cm} Tree \hspace{0.2cm} Piece \hspace{0.2cm}, NewSyntax \hspace{0.2cm}, Parameters \hspace{0.2cm}, Constr)
                                 \mathtt{syntax} \ \mathtt{Set} \ ::= \ \mathtt{getTyVarsRHS}(\mathtt{K},\mathtt{List}) \ [\, \mathtt{function} \, ]
                                  syntax KItem ::= for All (Set ,K)
                                  syntax KItem ::= funtype(K,K)
                                  syntax Set ::= listToSet(List, Set) [function]
                                  \texttt{rule listToSet}\left(\texttt{ListItem}\left(\texttt{A:KItem}\right) \ \texttt{L:List} \ , \ \texttt{S:Set}\right) \ \Longrightarrow \ \texttt{listToSet}\left(\texttt{L} \ , \ \texttt{SetItem}\left(\texttt{A}\right) \ \texttt{S}\right)
                                  \mathtt{rule} \ \mathsf{listToSet} \, (\, . \, \mathsf{List} \, \, , \, \, \mathsf{S} \colon \mathsf{Set} \, ) \, \, \Longrightarrow \, \, \mathsf{S}
//\, {\tt if\ optbangAtypes} \,,\ {\tt need\ to\ see}\ {\tt if\ first\ variable\ is\ a\ typecon}
//if its a typecon then need to go into Delta and see the amount of parameters it has
//then count the number of optbangAtypes after the typecon
                                  rule \ betaParser (\ 'constrCon (A:K, \ B:K) \ , \ Par:K, \ Con:K) \ \Rightarrow \ for All (getTyVarsRHS (B, .List) \ , \ betaParser (B, \ Par \ , \ Con))
                                   rule \ betaParser ('optBangATypes('optBangAType('emptyBang(.KList),, 'atypeTyVar(Tyv:K)),, Rest:K), Par:K, Con:K) \\ rule \ betaParser ('optBangATypes('optBangAType('emptyBang(.KList),, 'baTypeCon(A:K,, B:K)),, Rest:K), Par:K, Con:K) \\ rule \ betaParser ('optBangATypes('optBangATypes('emptyBang(.KList),, 'baTypeCon(A:K,, B:K))),, Rest:K), Par:K, Con:K) \\ rule \ betaParser ('optBangATypes('optBangATypes('emptyBang(.KList),, 'baTypeCon(A:K,, B:K))),, Rest:K), Par:K, Con:K) \\ rule \ betaParser ('optBangATypes('optBangATypes('emptyBang(.KList),, 'baTypeCon(A:K,, B:K))),, Rest:K), Par:K, Con:K) \\ rule \ betaParser ('optBangATypes('optBangATypes('emptyBang(.KList),, 'baTypeCon(A:K,, B:K))),, Rest:K), Par:K, Con:K) \\ rule \ betaParser ('optBangATypes('optBangATypes('emptyBang(.KList),, 'baTypeCon(A:K,, B:K))), \\ rule \ betaParser ('optBangATypes('emptyBang(.KList),, 'baTypeCon(A:K,, B:K))), \\ rule \ betaParser ('optBangATypes(.KList),, 'baTypeCon(A:K,, B:K))), \\ rule \ betaPars
                                  rule\ betaParser\ ('optBangATypes\ ('optBangAType\ ('emptyBang\ (.KList)), \ 'atypeGTyCon\ (Tyc:K)),, \ Rest:K),\ Par:K,\ Con:KingATypeBang\ (.KList), \ Par:K,\ Con:KingATypeBang\ (.KList), \ Par:KingATypeBang\ (.KL
                                  \texttt{rule betaParser} \ (. \ OptBangATypes} \ , \ \ Par:K, \ \ Con:K) \ \Rightarrow \ \ 'simpleTypeCon (Con,, \ Par)
                                                  rule \ betaParser ('optBangATypes('optBangAType('emptyBang(.KList'),, \ 'atypeGTyCon(Tyc:K)),, \ Rest:KItem')) \ => \ get'' \ (the property of the property 
                                                  \verb|rule| | \verb|getTypeVars('optBangAType('emptyBang(.KList)), | | Rest:K)) | => | \verb|getTypeVars(Rest)| |
                                                 rule getTypeVars('atypeGTyCon(A:K)) => . List
//
                                                  \texttt{rule getTypeVars}\left(\,\, \text{'atypeTyVar}\left(A\!:\!K\right)\right) \; \Longrightarrow \; \texttt{ListItem}\left(A\right)
                                                  rule getTypeVars(.OptBangATypes) => .List
```

Draft of November 4, 2018 at 20:29

```
rule getTyVarsRHS(.OptBangATypes, Tylist:List) => listToSet(Tylist, .Set)
    \texttt{rule} \; <\!\! k\!\! > \; \texttt{newBeta} \, (M\!:\! \mathsf{Map})
             =>~.\,\mathrm{K}~\ldots</\,\mathrm{k}>
         <tempBeta> OldBeta:K => M </tempBeta>
syntax KItem ::= "insertAlphaBetaStar"
    syntax KItem ::= insertABRec(K, List)
    syntax KItem ::= insertAB(K)
    rule < k > insertAlphaBetaStar \Rightarrow insertABRec(Mod, Imp) \dots < / k >
         <\!\!\operatorname{tempModule}\!\!> \operatorname{Mod}\!:\!\operatorname{KItem} <\!\!/\operatorname{tempModule}\!\!>
         <importTree> Imp: List </importTree>
    rule <\!\!k\!\!> insertABRec(Node:KItem,\ ListItem(impObject(B:KItem,Node))\ I:List) \Rightarrow insertAB(B)\ \tilde{\ }> insertABRec(Node,RItem,Node)
    rule <k> insertABRec(Node: KItem, ListItem(impObject(B: KItem, C: KItem)) I: List) => insertABRec(Node, I) ... </k>
              requires Node =/=K C
    rule \langle k \rangle insertAB(B) \Rightarrow .K ... \langle k \rangle
         <\!\operatorname{tempAlphaStar}\!> \operatorname{Alph}\!:\!\operatorname{KItem}\ <\!/\operatorname{tempAlphaStar}\!>
         <tempBetaStar> Bet:KItem </tempBetaStar>
         <moduleImpBetas> ImpBetas:List => ListItem(Bet) ImpBetas </moduleImpBetas>
```

endmodule

MULTIPLE MODULE SUPPORT

The next step is to implement multiple modules into the Haskell semantics. Similar to including files or objects in other programming languages, Haskell modules can include other modules and use functions, types, and typeclasses declared in the module. There are a several considerations and additional checks that need to be made. Modules need to include other modules There cannot be inclusion cycles Modules need to be able to access user defined types from the other modules that are included When referencing types from other modules, there is a scope where if the user makes another type of the same name in the current module then when the user references the type, it refers to the type from the current module. For instance:

```
File 1: module File1 where \{data\ A=B\} File 2: module File2 where \{data\ A=B\ ; data\ C=B\ A\}
```

This will compile. The A used in data C is File2.A However, If there are multiple types with the same name declared outside of the current module. If you try to refer to the type without the parent module, there will be a compiler error because there is ambiguity. For instance:

```
File 1:
module File1 where
{data A = B
}
File 2:
module File2 where
{data A = B
}
File 3:
module File3 where
{import File1
;import File2
;data C = B A
}
```

This will not compile because in File 3, type A is ambiguous and can mean File1.A or File2.A Type synonyms need to include polymorphism For instance: The user can write type A = B a

Since we need to check for module inclusion cycles and also build the set of user defined types for each module and included modules, I decided to use a tree. The plan for the algorithm is as follows 1. Construct tree for module inclusion 2. Check tree for cycles 3. Go to each leaf and recursively go up the tree and build alpha* and beta* for the types of the module and the children and desugar the scope so that each type specifies the scope.

Where alpha is the map of type synonyms declared in the current module and alpha* is the map of type synonyms declared in the current module and all the included modules. Beta is the set of user defined types from using data and newtype declared in the current module. Beta* is the set of user defined types from using data and newtype declared in the current module and all the included modules. Desugar the scope means that when the user references a type, desugar the reference to also include the parent module at all times. The syntax also needed to be changed to allow for multiple modules. The new syntax added is

```
// CUSTOM SYNTAX NOT PART OF OFFICAL HASKELL
syntax ModuleList ::= Module [klabel('modListSingle)] | Module "<NEXTMODULE>" ModuleList [klabel('modList)]
```

This is because K cannot read mutiple files. So instead all the included modules for a program are dumped into one file and are seperated by the keyword ¡NEXTMODULE; This creates a list of modules called ModuleList.

INFERENCING

6.1 Data Structures

The next step is the actual type inferencing algorithm. I needed to create a syntax for polymorphic types that may contain monomorphic type variables and polymorphic type variables. Then I made a map from type constructor names to arities, called Delta. Then I made a map from data constructors and term identifiers to their most general polymorphic types, called beta. The first part was converting the T data structure into beta, which is more suited for type inferencing. Something to note is that for GHC:

$$fx = yx$$

$$yx = fx$$

This set of functions is allowed. When run, the function just simply runs forever. Another thing to note is that the

[context =>]

part of the syntax for the types is deprecated. https://stackoverflow.com/questions/9345589/guards vs-if-then-else-vs-cases-in-haskell For functions, function guards, cases, and if-then-else are all equivalent.

A polymorphic data type looks like $\forall abc, (a \rightarrow b) \rightarrow c$

6.1.1 Inferencing Rules

Haskell is a strong and static type system.

This means that type inferencing can be ran before compilation or running the code. used to ensure that fun

Type inferencing

Haskell's type system is a Hindley-Milner polymorphic type system that has been extended with type classes to account for overloaded function

A type system is a set of rules that assign a property to various constructs in a programming language called type. A type is a property that allows the programmer to add constraints to programs.

6.2 Type theory

Type theory was created by Bertrand Russell to prevent Russell's Paradox for set theory, introduced by Georg Cantor. The issue was that not specifying a certain property for sets allowed sets to contain themselves in Naive Set Theory. So Bertrand Russell prevented this problem by specifying a property called type for objects, and objects cannot contain their own type.

6.3 Lambda Calculus

The Lambda Calculus was created to

6.4 Hindley-Milner

6.5 Definition of Substitution

A substitution is a set of variables and their replacements. Applying a substitution to an expression means to simultaneously replace each variable in the expression with the replacement term.

[http://www.mathcs.duq.edu/simon/Fall04/notes-7-4/node3.html]

6.6 Composition of Substitutions

6.7 Inferencing Algorithm

$$\frac{\Gamma \vdash c : \tau \mid \text{unify}\{(\tau, \text{freshInstance}(\tau))\}}{\Gamma \vdash x : \tau \mid \text{unify}\{(\tau, \text{freshInstance}(\Gamma(x)))\}} \text{ Variable}$$

$$\frac{[x : \tau_1] + \Gamma \vdash e : \tau_2 \mid \sigma}{\Gamma \vdash \langle x \rightarrow e : \tau \mid \text{unify}\{(\sigma(\tau), \sigma(\tau_1 \rightarrow \tau_2))\} \circ \sigma} \text{ Lambda}$$

$$\frac{\Gamma \vdash e_1 : \text{bool} \mid \sigma_1 \qquad \sigma_1(\Gamma) \vdash e_2 : \sigma_1(\tau) \mid \sigma_2 \qquad \sigma_2 \circ \sigma_1(\Gamma) \vdash e_3 : \sigma_2 \circ \sigma_1(\tau) \mid \sigma_3}{\Gamma \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 : \tau \mid \sigma_3 \circ \sigma_2 \circ \sigma_1} \text{If ThenElse}$$

$$\frac{\Gamma \vdash e_1 : \tau_1 \to \tau \mid \sigma_1 \qquad \sigma_1(\Gamma) \vdash e_2 : \sigma_1(\tau_1) \mid \sigma_2}{\Gamma \vdash e_1 e_2 : \tau \mid \sigma_2 \circ \sigma_1}$$
 Application

$$\frac{1}{\Gamma \vdash c : \tau \mid \text{unify}\{(\tau, \text{freshInstance}(\tau))\}} \text{ LetIn}$$

[cs 421 gather exp ty substitution mp]

```
requires "haskell-syntax.k"
requires "haskell-configuration.k"
requires "haskell-preprocessing.k"

module HASKELL-TYPE-INFERENCING
imports HASKELL-SYNTAX
imports HASKELL-CONFIGURATION
imports HASKELL-PREPROCESSING

syntax KItem ::= "Bool" //Boolean

// STEP 4 Type Inferencing
syntax KItem ::= inferenceShell(K) [function]//Input, AlphaMap, Beta, Delta, Gamma
```

```
//syntax KItem ::= typeInferenceFun(K,Map,Map,Map,Map,K,K) [function]//Input, Alpha, Beta, Delta, Gamma
// \operatorname{syntax} \ \operatorname{KItem} \ ::= \ \operatorname{typeInferenceFun} \left(\operatorname{Map}, K, K\right) \ // \operatorname{Gamma}, \ \operatorname{Expression} \ , \ \operatorname{Guessed} \ \operatorname{Type}
\mathtt{syntax}\ \mathrm{Map}\ ::=\ \mathrm{genGamma}(K,\mathrm{Map},K)\ [\ \mathtt{function}\ ]\ \ //\ \mathtt{Apatlist}\ ,\ \mathsf{Gamma}\ \mathsf{Type}
\mathtt{syntax} \ \ \mathsf{KItem} \ ::= \ \mathtt{genLambda}(\mathsf{K}, \mathsf{K}) \ \ [\, \mathtt{function} \, ]
syntax KItem ::= guessType(Int)
      syntax KItem ::= lambdaReturn(K,K,K)
syntax KItem ::= freshInstance(K, Int) [function]
\mathtt{syntax} \ \mathtt{Int} \ ::= \ \mathtt{paramSize}\left(K\right) \ [\, \mathtt{function} \, ]
syntax KItem ::= mapBag(Map)
syntax KResult ::= mapBagResult(Map)
syntax Map ::= gammaSub(Map,Map,Map) [function]//substitution, gamma
rule <k> performIndividualInferencing => inferenceShell(Code) ... </k>
                     <\!\!\operatorname{tempModule}\!\!> \operatorname{Mod}\!:\!\operatorname{KItem} <\!\!/\operatorname{tempModule}\!\!>
                     <moduleName> 'moduleName(Mod) </moduleName>
                     <moduleTempCode> Code:KItem </moduleTempCode>
rule \ inferenceShell ('topdeclslist('type(A:K,, B:K),, Rest:K)) \Rightarrow
                     inferenceShell(Rest) //constructalpha
rule \;\; inference Shell \left( \; 'top decls list \left( \; 'data (A:K, \; , \; B:K, \; , \; C:K, \; , \; D:K) \; , \; , \; \; Rest : K) \right) \;\; = \; \\
                      inferenceShell (Rest)
rule \;\; inference Shell \left( \; 'topdeclslist \left( \; 'newtype (A:K, \; B:K, \; C:K, \; D:K) \; , \; \; Rest : K) \right) \;\; = \; \; \\ \;\; rule \;\; inference Shell \left( \; 'topdeclslist \; (\; 'newtype (A:K, \; B:K, \; C:K, \; D:K) \; , \; \; Rest : K) \right) \;\; = \; \\ \;\; rule \;\; inference Shell \left( \; 'topdeclslist \; (\; 'newtype (A:K, \; B:K, \; C:K, \; C:K, \; Rest : K) \; ) \; \right) \;\; = \; \\ \;\; rule \;\; inference Shell \left( \; 'topdeclslist \; (\; 'newtype (A:K, \; B:K, \; Rest : K) \; ) \; \right) \;\; = \; \\ \;\; rule \;\; rule
                     inferenceShell (Rest)
 rule \ inference Shell \ (\ 'topdeclslist \ (\ 'class \ (A:K,\ ,\ B:K,\ ,\ C:K,\ ,\ D:K)\ ),\ =>
                      inferenceShell (Rest)
rule inferenceShell('topdeclslist('instance(A:K,, B:K,, C:K,, D:K),, Rest:K)) =>
                     inferenceShell (Rest)
rule \;\; inference Shell \left( \; 'topdeclslist \left( \; 'default \left( A:K, \; , \; B:K, \; , \; C:K, \; , \; D:K \right) \; , \; \; Rest : K \right) \right) \;\; = > \;\; logical formula \;\; logical for
                      inferenceShell (Rest)
rule inferenceShell('topdeclslist('foreign(A:K,, B:K,, C:K,, D:K),, Rest:K)) =>
                     inferenceShell (Rest)
rule inferenceShell ('topdeclslist ('topdecldecl(A:K),, Rest:K)) =>
                      typeInferenceFun\left(.\,ElemList\,,\ .Map\,,A\,,guessType\,(\,0\,)\right)\ \tilde{\ }>\ inferenceS\,hell\,(\,Rest\,)
{\tt rule} <\!\!k\!\!> {\tt typeInferenceFun} \, (\, . \, ElemList \, , \, \, Gamma : Map, \quad {\tt 'declFunLhsRhs} \, (Fn : K, \, , \quad Lhsrhs : K) \, , \quad Guess : K) \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \quad (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K, \, , \quad Lhsrhs : K) \, , \\ =\!\!\! > \, (Fn : K,
                      {\tt typeInferenceFun} \; (\, . \; ElemList \; , \; \; Gamma, \; \; Lhsrhs \; , \; \; Guess \, ) \; \; \ldots < / \, k >
rule <k> typeInferenceFun (.ElemList, Gamma:Map, 'eqExpOptDecls(Ex:K,, Optdecls:K), Guess:K) =>
                     typeInferenceFun (.ElemList, Gamma, Ex, Guess) ... </k>
//T-App
//rule typeInferenceFun('aexpQVar(Var:K), Alpha:Map, Beta:Map, Delta:Map, (Var |-> Sigma:K) Gamma:Map,.K,.K) =
//Gamma Proves x:phi(tau) if Gamma(x) = forall alpha_1, \dots, alpha_n. tau
//where phi replaces all occurrences of alpha-1, \dots, alpha-n by monotypes tau-1, \dots, tau-n
rule <k> typeInferenceFun (.ElemList, (Var |-> Type:K) Gamma:Map, 'aexpQVar(Var:K), Guess:KItem)
                       \Rightarrow mapBagResult(uniFun(ListItem(uniPair(Guess,freshInstance(Type, TypeIt))))) \ ... </ k > // Variable \ rule \ (All of the content of the c
                     <\!\!\mathrm{typeIterator}\!> \ \mathrm{TypeIt}: \mathrm{Int} \ =\!\!> \ \mathrm{TypeIt} \ + \mathrm{Int} \ \ \mathrm{paramSize}\left(\mathrm{Type}\right) \ <\!\!/\mathrm{typeIterator}\!>
                                                       \frac{1}{\Gamma \vdash c : \tau \mid \text{unify}\{(\tau, \text{freshInstance}(\tau))\}} \text{ Constant}
rule < k > typeInferenceFun (.ElemList, Gamma: Map, 'aexpGCon('conTyCon(Mid:K,, Gcon:K)), Guess: KItem) \\
                         \Rightarrow mapBagResult(uniFun(ListItem(uniPair(Guess,freshInstance(Type, TypeIt))))) \\ ... </k> // Constant rule \\ (2.15)
                     <tempBeta> (ModPlusType(Mid,Gcon) |-> Type:K) Beta:Map </tempBeta>
                    <typeIterator> TypeIt:Int => TypeIt +Int paramSize(Type) </typeIterator>
                                                 \frac{}{\Gamma \vdash x : \tau \mid \text{unify}\{(\tau, \text{freshInstance}(\Gamma(x)))\}} \text{ Variable}
```

```
syntax \hspace{0.1cm} KItem \hspace{0.1cm} ::= \hspace{0.1cm} typeInferenceFun (\hspace{0.1cm} ElemList \hspace{0.1cm} , \hspace{0.1cm} Map, \hspace{0.1cm} K, \hspace{0.1cm} K) \hspace{0.1cm} [\hspace{0.1cm} strict \hspace{0.1cm} (\hspace{0.1cm} 1)\hspace{0.1cm} ]
           syntax \hspace{0.2cm} KItem \hspace{0.2cm} ::= \hspace{0.2cm} typeInferenceFunLambda(\hspace{0.2cm} ElemList\hspace{0.2cm} , \hspace{0.2cm} K, \hspace{0.2cm} K, \hspace{0.2cm} K) \hspace{0.2cm} \left[\hspace{0.2cm} strict\hspace{0.2cm} (\hspace{0.2cm} 1)\hspace{0.2cm} \right]
/*\ automatically\ generated\ by\ the\ strict(1)\ in\ typeInferenceFun\ or\ typeInferenceFunAux
           \texttt{rule typeInferenceFunAux}(\texttt{Es:ElemList}, \texttt{ C:K}, \texttt{ A:K}, \texttt{ B:K}) \implies \texttt{Es} \texttt{ `> typeInferenceFun}(\texttt{HOLE}, \texttt{ C}, \texttt{ A}, \texttt{ B})
                               requires notBool isKResult(Es)
           rule Es:KResult ~> typeInferenceFunAux(HOLE, C:K,A:K, B:K) => typeInferenceFun(Es, C, A, B)
               //lambda rule
               rule < k > typeInferenceFun (.ElemList, Gamma: Map, 'lambdaFun (Apatlist: K,, Ex:K), Guess: KItem)
                                    => typeInferenceFunLambda(val(typeInferenceFun(.ElemList, genGamma(Apatlist,Gamma,guessType(TypeIt)), gen
                                 <typeIterator> TypeIt:Int => TypeIt +Int 2 </typeIterator>
               rule < k > typeInferenceFunLambda(valValue(mapBagResult(Sigma:Map))), \ . ElemList, \ Tau:K, \ Tauone:K, \ Tautwo:K) > typeInferenceFunLambda(valValue(mapBagResult(Sigma:Map))), \ . ElemList, \ Tauone:K, \ Ta
                                 => mapBagResult (compose (uniFun (ListItem (uniPair (typeSub (Sigma, Tau), typeSub (Sigma, funtype (Tauone, Tautwo)))
                                           \frac{[x:\tau_1] + \Gamma \vdash e:\tau_2 \mid \sigma}{\Gamma \vdash \backslash x \to e:\tau \mid \text{unify}\{(\sigma(\tau), \sigma(\tau_1 \to \tau_2))\} \circ \sigma} \text{Lambda}
               syntax KItem ::= typeInferenceFunAppli(ElemList, Map, K, K, Map) [strict(1)]
               //application rule
               rule <k> typeInferenceFun(.ElemList, Gamma:Map, 'funApp(Eone:K,, Etwo:K), Guess:KItem)
                                    \Rightarrow \texttt{typeInferenceFunAppli(val(typeInferenceFun(.ElemList, Gamma, Eone, funtype(guessType(TypeIt), Guess)))}
                                 <\!\operatorname{typeIterator}\!> \ \operatorname{TypeIt}: \operatorname{Int} \ =\!\!> \ \operatorname{TypeIt} \ + \operatorname{Int} \ 1 \ <\!\!/\operatorname{typeIterator}\!>
               rule <k> typeInferenceFunAppli(valValue(mapBagResult(Sigmaone:Map)), .ElemList, Gamma:Map, Etwo:KItem, guessTy
                                    => typeInferenceFunAppli(val(typeInferenceFun(.ElemList, gammaSub(Sigmaone, Gamma, .Map), Etwo, typeSub(
               rule <k> typeInferenceFunAppli(valValue(mapBagResult(Sigmatwo:Map)), .ElemList, .Map, .K, .K, Sigmaone:Map)
                                    => mapBagResult(compose(Sigmatwo, Sigmaone)) ... </k>
                                        \frac{\Gamma \vdash e_1 : \tau_1 \to \tau \mid \sigma_1 \qquad \sigma_1(\Gamma) \vdash e_2 : \sigma_1(\tau_1) \mid \sigma_2}{\Gamma \vdash e_1 e_2 : \tau \mid \sigma_2 \circ \sigma_1} \text{Application}
               syntax KItem ::= typeInferenceFunIfThen(ElemList, Map, K, K, K, Map, Map) [strict(1)]
               //if_then_else rule
               rule < \!\! k\!\! > typeInferenceFun\,(.\,ElemList\,,\,\,Gamma:Map,\,\,\,'ifThenElse\,(Eone:K,\,,\,\,Optsem:K,\,,\,\,Etwo:K,\,,\,\,Optsemtwo:K,\,,\,\,Ethree:LouiseFun\,(Eone:K,\,,\,\,Optsem:K,\,,\,\,Ethree:LouiseFun\,(Eone:K,\,,\,\,Optsem:K,\,,\,\,Ethree:LouiseFun\,(Eone:K,\,,\,\,Optsem:K,\,,\,\,Optsem:K,\,,\,\,Optsem:K,\,,\,\,Optsem:K,\,,\,\,Optsem:K,\,,\,\,Optsem:K,\,,\,\,Optsem:K,\,,\,\,Optsem:K,\,,\,\,Optsem:K,\,,\,Optsem:K,\,,\,Optsem:K,\,,\,Optsem:K,\,,\,Optsem:K,\,,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Optsem:K,\,Op
                                     ⇒ typeInferenceFunIfThen(val(typeInferenceFun(, ElemList, Gamma, Eone, Bool)), , ElemList, Gamma, Etwo, E
               rule <k> typeInferenceFunIfThen(valValue(mapBagResult(Sigmaone:Map)), .ElemList, Gamma:Map, Etwo:KItem, Ethree
                                    => typeInferenceFunIfThen(val(typeInferenceFun(.ElemList, gammaSub(Sigmaone, Gamma, .Map), Etwo, typeSub
               rule < k > typeInferenceFunIfThen (valValue (mapBagResult (Sigmatwo: Map)) \,, \; . ElemList \,, \; Gamma: Map, \; .K, \; Ethree: KItem \,, \; .K, \; .
                                    => typeInferenceFunIfThen(val(typeInferenceFun(.ElemList, gammaSub(compose(Sigmatwo, Sigmaone), Gamma, ...)
               rule <k> typeInferenceFunIfThen(valValue(mapBagResult(Sigmathree:Map)), .ElemList, .Map, .K, .K, .K, Sigmaone:
                                    => mapBagResult(compose(compose(Sigmathree, Sigmatwo), Sigmaone)) ...</k>
```

$$\frac{\Gamma \vdash e_1 : \text{bool} \mid \sigma_1 \qquad \sigma_1(\Gamma) \vdash e_2 : \sigma_1(\tau) \mid \sigma_2 \qquad \sigma_2 \circ \sigma_1(\Gamma) \vdash e_3 : \sigma_2 \circ \sigma_1(\tau) \mid \sigma_3}{\Gamma \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 : \tau \mid \sigma_3 \circ \sigma_2 \circ \sigma_1} \text{IfThenElse}$$

```
syntax KItem ::= typeInferenceFunLetIn(ElemList, Map, Map, K, K, K, Int, Int, Map, Map) [strict(1)]
          syntax \ KItem ::= \ grabLetDeclName(K, \ Int) \ [function]
          \mathtt{syntax} \ \ \mathsf{KItem} \ ::= \ \mathtt{grabLetDeclExp}\left(\mathsf{K}, \ \mathsf{Int}\right) \ [\, \mathsf{function}\,]
          \mathtt{syntax} \ \mathsf{KItem} \ ::= \ \mathsf{mapLookup}(\mathsf{Map}, \ \mathsf{K}) \ [\, \mathsf{function} \,]
          \mathtt{syntax} \ \mathtt{Map} \ ::= \ \mathtt{makeDeclMap}(\mathtt{K}, \ \mathtt{Int} \ , \ \mathtt{Map}) \ \ [\, \mathtt{function} \, ]
          syntax Map ::= applyGEN(Map, Map, Map, Map) [function]
          //Haskell let in rule (let rec in exp + let in rule combined)
          //gamma \mid - let rec f1 = e1 and f2 = e2 and f3 = e3 .... in e =>
          // beta \, , \, \, [\, f1 \, -\! > \, tau1 \, , \, \, f2 \, -\! > \, tau2 \, , \, \, f3 \, -\! > \, tau3 \, , \dots . \, ] \, + \, gamma \, \, |- \, e1 \, : \, tau1 \, \, | \, \, sigma1 \, , \, \, \, [\, f1 \, -\! > \, simga1(tau1) \, , \, \, f2 \, -\! > \, simga1(tau1) \, , \, \, f2 \, -\! > \, simga1(tau1) \, , \, \, f3 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f4 \, -\! > \, simga1(tau1) \, , \, \, f5 \, -\! > \, simga1(tau1) \, , \, \, f5 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, f6 \, -\! > \, simga1(tau1) \, , \, \, 
[f1 -> sigma2 o sigma1(tau1), f2 -> sigma2 o sigma1(tau2), f3 -> sigma2 o sigma1(tau3),....] + sigma2 o sigma1(gam
[f1 -> gen(sigma_n o sigma2 o sigma1(tau1), sigma_n o sigma2 o sigma1(Gamma)), f2 -> gen(tau2), f3 -> gen(tau3),... rule <k> typeInferenceFun(.ElemList, Gamma:Map, 'letIn(D:K,, E:K), Guess:KItem)
                         => typeInferenceFunLetIn (.ElemList , Gamma, makeDeclMap(D, TypeIt , .Map) , D, E, Guess , 0 , TypeIt , .Map, B
                       <typeIterator> TypeIt:Int => TypeIt +Int size(makeDeclMap(D, TypeIt, .Map)) .Map()
                       <tempBeta> Beta:Map </tempBeta>
          rule <k> typeInferenceFunLetIn (.ElemList , Gamma:Map, DeclMap:Map, D:KItem , E:KItem , Guess:KItem , Iter:Int , Typ
                             => typeInferenceFunLetIn(val(typeInferenceFun(.ElemList, Gamma DeclMap, grabLetDeclExp(D, Iter), mapLoo
                          requires Iter <Int (size(DeclMap))
          => typeInferenceFunLetIn (.ElemList, gammaSub(Sigma,Gamma,.Map), gammaSub(Sigma, DeclMap,.Map), D, E, type
                          rule <k> typeInferenceFunLetIn (.ElemList, Gamma:Map, DeclMap:Map, D:KItem, E:KItem, Guess:KItem, Iter:Int, Typ
                          => typeInferenceFunLetIn(val(typeInferenceFun(.ElemList, Gamma applyGEN(Gamma, DeclMap, .Map, Beta), E,
                          requires Iter >=Int (size(DeclMap))
          rule <k> typeInferenceFunLetIn(valValue(mapBagResult(Sigma:Map)), .ElemList, Gamma:Map, DeclMap:Map, D:KItem, l
                          \Rightarrow mapBagResult(compose(Sigma, OldSigma))...</k>
                          requires Iter >=Int (size(DeclMap))
                                                 \frac{1}{\Gamma \vdash c : \tau \mid \text{unify}\{(\tau, \text{freshInstance}(\tau))\}} \text{ LetIn}
          \verb"rule mapLookup" ((Name |-> Type: KItem") DeclMap: Map", Name: KItem") => Type
           rule mapLookup(DeclMap:Map, Name:KItem) => Name
                        requires notBool(Name in keys(DeclMap))
          \verb|rule| makeDeclMap('decls(Dec:K)|, TypeIt:Int|, NewMap:Map)| => makeDeclMap(Dec|, TypeIt|, NewMap)|
          rule \ make DeclMap (\ 'declsList (\ 'declPatRhs (\ 'apatVar (Var : K) \ , \ , \ Righthand : K) \ , \ , \ Rest : K) \ , \ Type It : Int \ , \ New Map : Map) \ \Longrightarrow \ make DeclMap (\ 'declsList (\ 'declPatRhs (\ 'apatVar (\ Var : K) \ ) \ , \ , \ Rest : K) \ , \ Type It : Int \ , \ New Map : Map) \ \Longrightarrow \ make DeclMap (\ 'declsList (\ 'declPatRhs (\ 'apatVar (\ Var : K) \ ) \ , \ , \ Rest : K) \ , \ Type It : Int \ , \ New Map : Map \ ) \ \Longrightarrow \ make DeclMap (\ 'declsList (\ 'decls
          \verb"rule makeDeclMap" (.DeclsList", TypeIt:Int", NewMap:Map") \implies NewMap
          rule grabLetDeclName('decls(Dec:K), Iter:Int) => grabLetDeclName(Dec, Iter)
          rule \ grabLetDeclName(\ 'declsList(Dec:K,\ ,\ Rest:K)\ ,\ Iter:Int) \ \Longrightarrow \ grabLetDeclName(\ Rest\ ,\ Iter\ -Int\ 1)
                       requires Iter >Int 0
```

```
rule grabLetDeclName('declsList(Dec:K,, Rest:K), Iter:Int) => grabLetDeclName(Rest, Iter-Int 1)
requires Iter >Int 0
rule grabLetDeclName('declsList('declPatRhs('apatVar(Var:K),, Righthand:K),, Rest:K), Iter:Int) => Var
requires Iter <=Int 0

rule grabLetDeclExp('decls(Dec:K), Iter:Int) => grabLetDeclExp(Dec, Iter)
rule grabLetDeclExp('declsList(Dec:K,, Rest:K), Iter:Int) => grabLetDeclExp(Rest, Iter-Int 1)
requires Iter >Int 0

rule grabLetDeclExp('declsList('declPatRhs('apatVar(Var:K),, Righthand:K),, Rest:K), Iter:Int) => grabLetDeclExp
requires Iter <=Int 0

rule grabLetDeclExp('declx)('declPatRhs('apatVar(Var:K),, Righthand:K),, Rest:K), Iter:Int) => grabLetDeclExp
requires Iter <=Int 0

rule grabLetDeclExp('eqExpOptDecls(Righthand:K,, Opt:K), Iter:Int) => 'eqExpOptDecls(Righthand,, Opt)

rule genGamma('apatVar(Vari:K), Gamma:Map, Guess:K) => Gamma[Vari <- Guess]

rule genGamma('apatVar(Vari:K), Ex:K) => Ex
rule genLambda('apatVar(Vari:K), Ex:K) => tlambdaFun(Pattwo,, Ex)

rule gammaSub(Sigma:Map, (Key:KItem |-> Type:KItem) Gamma:Map, Newgamma:Map)
=> gammaSub(Sigma, Gamma, Newgamma[Key <- typeSub(Sigma, Type) ] )
```

```
rule gammaSub(Sigma: Map, . Map, Newgamma: Map)
      => Newgamma
\verb|rule| freshInstance(guessType(TypeIt:Int), Iter:Int)| \Rightarrow guessType(TypeIt)|
rule freshInstance(forAll(.Set, B:K), Iter:Int) => B
rule freshInstance(forAll(SetItem(C:KItem) A:Set, B:K), Iter:Int) => freshInstance(forAll(A, freshInstanceInne
syntax \hspace{0.2cm} KItem \hspace{0.2cm} ::= \hspace{0.2cm} freshInstanceInner(K,K,Int) \hspace{0.2cm} [\hspace{0.2cm} function \hspace{0.2cm}]
rule \;\; freshInstanceInner\,(Repl:KItem\,, \;\; funtype\,(A:K,\;B:K)\,, \;\; Iter:Int\,) \;\; \Rightarrow \;\; funtype\,(freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInstanceInner\,(Repl:A,Iter)\,,freshInsta
rule freshInstanceInner(Repl:KItem, Repl, Iter:Int) => guessType(Iter)
rule \;\; freshInstanceInner(Repl:KItem\,, \;\; Target:KItem\,, \;\; Iter:Int) \;\; => \;\; Target \;\; [\; owise \;]
rule paramSize(forAll(A:Set, B:K)) \implies size(A)
rule paramSize(A:K) => 0 [owise]
   => applyGEN(Gamma, DeclMap, NewMap[Key <- gen(Gamma, Type, Beta)], Beta)
   \verb"rule" applyGEN (Gamma: Map, .Map, NewMap: Map, Beta: Map)"
         => NewMap
//GEN
//GEN(Gamma, Tau) \implies Forall alpha
syntax KItem ::= gen(Map, K, Map) [function]
\mathtt{syntax} \ \mathtt{Set} \ ::= \ \mathtt{freeVarsTy}\left(\mathtt{K}, \ \mathtt{Map}\right) \ [\, \mathtt{function} \, ]
syntax Set ::= freeVarsEnv(Map, Map) [function]
rule \ gen (Gamma: Map, \ for All (Para: Set , \ Tau: KItem) \ , \ Beta: Map) \ => \ for All (free Vars Ty (for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (Para: Set , \ Tau) \ , \ Beta) \ -> \ for All (
rule gen (Gamma: Map, Tau: KItem, Beta: Map) => forAll (freeVarsTy(Tau, Beta) -Set freeVarsEnv(Gamma, Beta), Tau) [
//rule gen(Gamma:Map, forAll(Para:Set, Tau:KItem), Beta:Map) => forAll(freeVarsTy(forAll(Para:Set, Tau), Beta)
\texttt{rule freeVarsTy} \, (\, \texttt{guessType} \, (\, \texttt{TypeIt} \, : \, \texttt{Int} \, ) \, , \ \ \texttt{Beta} \, : \\ \texttt{Map}) \, \, \Rightarrow \, \, \, \, \texttt{SetItem} \, (\, \texttt{guessType} \, (\, \texttt{TypeIt} \, : \, \texttt{Int} \, ) \, ) \, 
rule freeVarsTy(funtype(Tauone:KItem, Tautwo:KItem), Beta:Map) => freeVarsTy(Tauone, Beta) freeVarsTy(Tautwo,
rule freeVarsTy(Tau:KItem, Beta:Map) => .Set
                 requires (for All (.Set , Tau)) in values (Beta)
rule freeVarsTy(forAll(Para:Set, Tau:KItem), Beta:Map) => freeVarsTy(Tau, Beta) -Set Para
\texttt{rule freeVarsEnv}\left(\texttt{Gamma:Map}, \ \texttt{Beta:Map}\right) \ \Longrightarrow \ \texttt{listToSet}\left(\texttt{values}\left(\texttt{Beta}\right), \ . \, \, \texttt{Set}\right)
```

6.7.1 Unification Algorithm

```
Let S = \{(s_1, t_1), (s_2, t_2), \dots, (s_n, t_n)\} be a unification problem.

Case S = \{\} : \text{Unif}(S) = \text{Identity function (ie no substitution)}

Case S = (s, t) \cup S'): Four main steps

Delete: if s = t (they are the same term) then Unif(S) = Unif(S')

Decompose: if s = f(q_1, \dots, q_m) and t = f(r_1, \dots, r_m) (same f, same m!),

then \text{Unif}(S) = \text{Unif}(\{(q_1, r_1), ..., (q_m, r_m)\} \cup S')

Orient: if t = x is a variable, and s is not a variable, \text{Unif}(S) = \text{Unif}(\{(x, s)\} \cup S')

Eliminate: if s = x is a variable, and x does not occur in t (the occurs check), then

Let \phi = x \mapsto t
```

```
Let \psi = \text{Unif}(\phi(S'))
         \mathrm{Unif}(S) = \{x \mapsto \psi(t)\} \circ \psi
         Note: x - a \circ y - b = y - (x - a(b) \circ x - a \text{ if } y \text{ not in } a
          [cs 421 class notes]
               //Unification
               syntax Map ::= uniFun(List) [function]
              syntax Bool ::= isVarType(K) [function]
               \mathtt{syntax} \ \mathtt{Bool} \ ::= \ \mathtt{notChildVar}\left(K,K\right) \ [\, \mathtt{function} \, ]
               syntax KItem ::= uniPair(K,K)
               syntax List ::= uniSub(Map,K) [function] //apply substitution to unification
               \operatorname{syntax} \ \operatorname{KItem} \ ::= \ \operatorname{typeSub}(\operatorname{Map}, \operatorname{K}) \ [\operatorname{function}] \ //\operatorname{apply} \ \operatorname{substitution} \ \operatorname{to} \ \operatorname{type}
               \mathtt{syntax}\ \mathtt{Map}\ ::=\ \mathtt{compose}\left(\mathtt{Map},\mathtt{Map}\right)\ [\ \mathtt{function}\ ]
               rule uniFun(.List) => .Map //substi(.K,.K) is id substitution
               rule uniFun(ListItem(uniPair(S:K,S)) Rest:List) => uniFun(Rest) //delete rule
               rule \ uniFun (ListItem (uniPair (S:K,T:K)) \ Rest: List) \implies uniFun (ListItem (uniPair (T,S)) \ Rest) \ //orient \ rule \ (UniPair (S:K,T:K)) \ Rest \ //orient \ rule \ (UniPair (S:K,T:K)) \ Rest \ //orient \ rule \ //orient \ rule \ //orient \ rule \ //orient \ rule \ //orient \ //or
                                 requires isVarType(T) andBool (notBool isVarType(S))
               rule \ uniFun(ListItem(uniPair(funtype(A:K,\ B:K),\ funtype(C:K,\ D:K))) \ Rest:List) \implies uniFun(ListItem(uniPair(A,\ C:K),\ C:K)) \implies uniFun(ListItem(uniPa
               rule uniFun(ListItem(uniPair(S:K,T:K)) Rest:List)
                     // \  \  \Rightarrow \  \  \, compose(uniFun(uniSub((S \mid -> T),Rest)),(S \mid -> typeSub(uniFun(uniSub((S \mid -> T),Rest)),T))) \  \  //eliminate \  \  \, r
                                requires isVarType(S) andBool notChildVar(S,T)
               rule isVarType(S:K) \Rightarrow true
                                 \texttt{requires getKLabel(S) ==} KLabel \ \texttt{'guessType}
               rule isVarType(S:K) => false [owise]
               rule notChildVar(S:K,T:K) => true
               \mathtt{rule} \ \mathtt{uniSub} \, (\, \mathtt{Sigma} \, ; \mathtt{Map} \, , \, . \, \, \mathtt{List} \, \, ) \, \, \Longrightarrow \, \, . \, \, \mathtt{List}
               rule uniSub(.Map,L:List) => L
               rule \ uniSub(Sigma: Map, \ Rest: List \ ListItem(uniPair(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Sigma, \ Rest) \ ListItem(uniPair(typeSub(A:K, \ B:K))) \ => \ uniSub(Sigma, \ Sigma, \ Sig
               //\operatorname{rule} \ \operatorname{typeSub} \left( \operatorname{substi} \left( .\operatorname{Map} \right) ,\operatorname{Tau} :\operatorname{KItem} \right) \implies \operatorname{Tau}
               \verb|rule typeSub|(Sigma:Map (Tau |-> Newtau); KItem)| => typeSub(Sigma (Tau |-> Newtau), Newtau)|
               rule typeSub(Sigma: Map, funtype(Tauone: KItem, Tautwo: KItem)) => funtype(typeSub(Sigma, Tauone), typeSub(Sigma, Tautwo: KItem))
               \verb"rule typeSub" (Sigma: Map, Tau: KItem") \implies Tau \ [owise]
               \mathtt{syntax}\ \mathtt{Map}\ ::=\ \mathtt{composeIn}\left(\mathtt{Map},\ \mathtt{Map},\ \mathtt{Map},\ \mathtt{K},\ \mathtt{K}\right)\ [\,\mathtt{function}\,]
               \verb|rule| compose(Sigmaone:Map, Sigmatwo:Map)| => composeIn(Sigmaone, Sigmatwo, .Kap, .K)
               rule composeIn (Sigmaone: Map, (Key: KItem |-> Type: KItem) Sigmatwo: Map, NewMap: Map, .K, .K) => composeIn (Sigmaone
               \verb|rule| composeIn((Keyone |-> Typetwo: KItem)| Sigmaone: Map, Sigmatwo: Map, NewMap: Map, Keyone: KItem)|
               rule composeIn((Typeone |-> Typetwo:KItem) Sigmaone:Map, Sigmatwo:Map, NewMap:Map, Keyone:KItem, Typeone:KItem
                                  requires notBool (Keyone in keys (Sigmaone))
               rule composeIn(Sigmaone:Map, Sigmatwo:Map, NewMap:Map, Keyone:KItem, Typeone:KItem) => composeIn(Sigmaone, Sigra
               rule composeIn(Sigmaone:Map, .Map, NewMap:Map, .K, .K) => Sigmaone NewMap
endmodule
```

CHAPTER 7 CONCLUSION

This is my conclusion.