

Circuitos Electricos II

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Monitoria Circuitos II

GIT-HUB: https://github.com/brrsanchezfi/Circuitos_2022_1

Soluciones propuestas para los ejercicios del taller 4

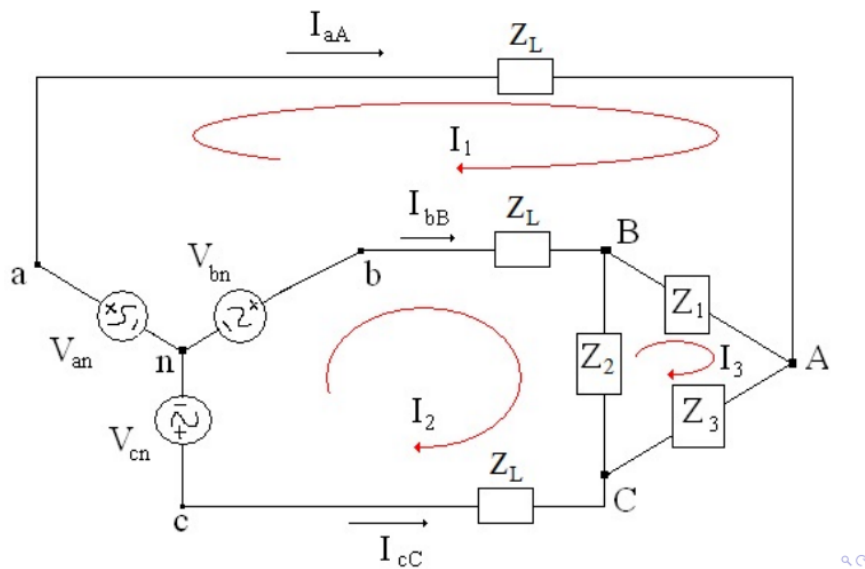
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1.Analisis por Matlab symbolic

Circuito Y-D

El siguiente metodo es la solucion que considero mas facil a la hora de entender el circuito.



Fuente trifásica: $V_{an} = 100\angle 0^\circ \text{ V}$, sec +
 Impedancia líneas: $Z_L = 0.5 \Omega$.

- 1 Proponga valores para las impedancias de carga.
- 2 Calcule la potencia compleja $S = VI^*$ para cada elemento del circuito.
- 3 Calcule la potencia de pérdidas.
- 4 Muestre el balance de potencia.

Voltaje = 100;

```
%{
  La funcion "pol_com(magnitud,angulo)" convierte un fador a rectangular
  por medio de la identidad de euler
%}
```

```
V_an_x = pol_com(Voltaje/sqrt(2),0);
V_bn_x = pol_com(Voltaje/sqrt(2),-120);
V_cn_x = pol_com(Voltaje/sqrt(2),120);
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%1. En estos blocks proporcionamos los valores de impedancia
```

```
Z1_x = 8+7i;
Z2_x = 6+3i;
Z3_x = 5+5i;
```

```
Z_L_x = 0.5;
```

```
syms I1 I2 I3 Z_L V_an V_bn V_cn Z1 Z2 Z3
```

```
Sys = [V_an - V_bn == Z_L*(I1) + Z1*(I1-I3) + Z_L*(I1-I2);
       V_bn - V_cn == Z_L*(I2-I1) + Z2*(I2-I3) + Z_L*(I2);
```

$$0 == Z1*(I3-I1) + Z2*(I3-I2) + Z3*(I3)]$$

Sys =

$$\begin{pmatrix} V_{an} - V_{bn} = I_1 Z_L + Z_1 (I_1 - I_3) + Z_L (I_1 - I_2) \\ V_{bn} - V_{cn} = I_2 Z_L + Z_2 (I_2 - I_3) - Z_L (I_1 - I_2) \\ 0 = I_3 Z_3 - Z_1 (I_1 - I_3) - Z_2 (I_2 - I_3) \end{pmatrix}$$

```
Sol = solve(Sys,[I1, I2, I3]);
```

```
I1 = Sol.I1 %reescribo la variable I1,I2,I3 con el nuevo valor simbolico
```

I1 =

$$-\frac{V_{bn} Z_2 Z_3 - V_{an} Z_2 Z_3 - V_{an} Z_1 Z_2 + V_{cn} Z_1 Z_2 - 2 V_{an} Z_1 Z_L - 2 V_{an} Z_2 Z_L - 2 V_{an} Z_3 Z_L + V_{bn} Z_1 Z_L + V_{bn} Z_2 Z_L}{3 Z_1 Z_L^2 + 3 Z_2 Z_L^2 + 3 Z_3 Z_L^2 + Z_1 Z_2 Z_3 + 2 Z_1 Z_2 Z_L + 2 Z_1 Z_3 Z_L + 2 Z_2 Z_3 Z_L}$$

```
I2 = Sol.I2;
```

```
I3 = Sol.I3;
```

%CORRIENTES DE MALLAS

```
I1 = subs(I1,[V_an V_bn V_cn Z1 Z2 Z3 Z_L],[V_an_x V_bn_x V_cn_x Z1_x Z2_x Z3_x Z_L_x]);
```

```
I2 = subs(I2,[V_an V_bn V_cn Z1 Z2 Z3 Z_L],[V_an_x V_bn_x V_cn_x Z1_x Z2_x Z3_x Z_L_x]);
```

```
I3 = subs(I3,[V_an V_bn V_cn Z1 Z2 Z3 Z_L],[V_an_x V_bn_x V_cn_x Z1_x Z2_x Z3_x Z_L_x]);
```

%CORRIENTES DE LINEAS

```
I_aA = I1;
```

```
I_bB = I2 - I1;
```

```
I_cC = -I2;
```

%convertimos las variables simbolicas a una de tipo numero

```
I_aA = double(I_aA)
```

```
I_aA = 16.0506 - 14.9532i
```

```
I_bB = double(I_bB)
```

```
I_bB = -15.9733 - 12.9620i
```

```
I_cC = double(I_cC)
```

```
I_cC = -0.0772 + 27.9152i
```

%%
%2. Calcule la potencia compleja

%Para hallar las potencias complejas usamos la formula suministrada en el enunciado, omito la demostracion del por que el conjugado (dogma de fe)

```
S_a = V_an_x*conj(I_aA) %potencia entregada por las fuentes
```

```
S_a = 1.1349e+03 + 1.0574e+03i
```

```
S_b = V_bn_x*conj(I_bB)
```

```
S_b = 1.3585e+03 + 5.1989e+02i
```

```
S_c = V_cn_x*conj(I_cC)
```

```
S_c = 1.7122e+03 + 9.8222e+02i
```

```
S = round(S_a+S_b+S_c, 0) %Potencia total compleja redondeada
```

```
S = 4.2060e+03 + 2.5590e+03i
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%  
%3. Calcule la potencia de perdidas, aplicamos ley ohm para impedancias y  
%aplicamos ley watt
```

```
S_ZL = round(Z_L_x * (abs(I_aA^2) + abs(I_bB^2)+ abs(I_cC^2)),0) %potencia perdida por la red
```

```
S_ZL = 842
```

```
%CORRIENTES DE CARGA
```

```
I_Z1 = double(I1-I3);
```

```
I_Z2 = double(I2-I3);
```

```
I_Z3 = double(I3);
```

```
S_Z1 = abs(I_Z1*I_Z1)*Z1_x;
```

```
S_Z2 = abs(I_Z2*I_Z2)*Z2_x;
```

```
S_Z3 = abs(I_Z3*I_Z3)*Z3_x;
```

```
S_Z_carga = round(S_Z1+S_Z2+S_Z3) %potencia consumida por la carga
```

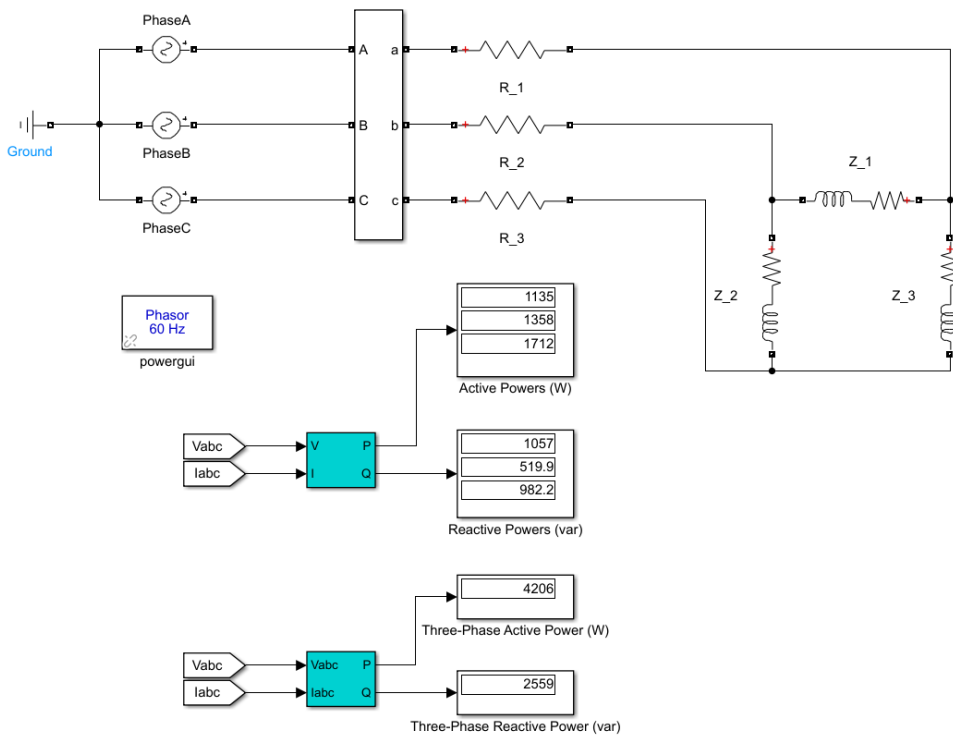
```
S_Z_carga = 3.3640e+03 + 2.5590e+03i
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%  
%4. Balance de potencia
```

```
Balance = round(S_ZL + S_Z_carga - S, 0)
```

```
Balance = 0
```

Simulacion

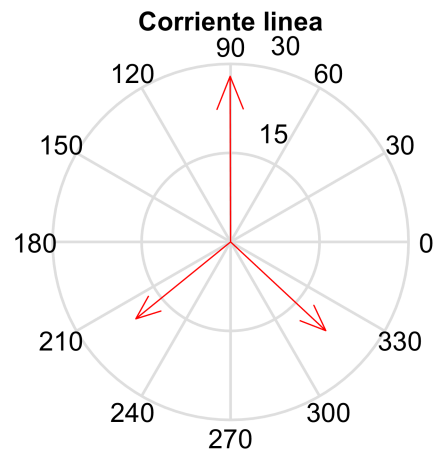
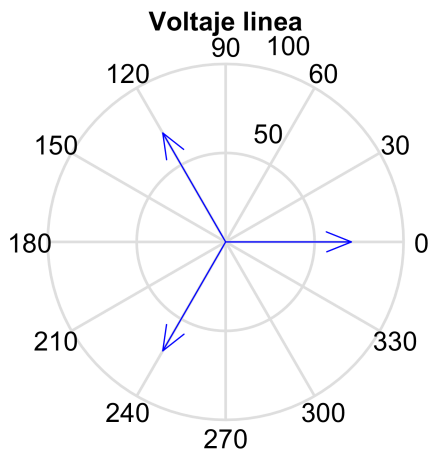


%herramienta interesante

```

tiledlayout(1,2)
ax1 = nexttile;
compass(ax1,[V_an_x V_bn_x V_cn_x], 'b')
title(ax1, 'Voltaje linea')
ax2 = nexttile;
compass(ax2,[I_aA I_bB I_cC], 'r')
title(ax2, 'Corriente linea')

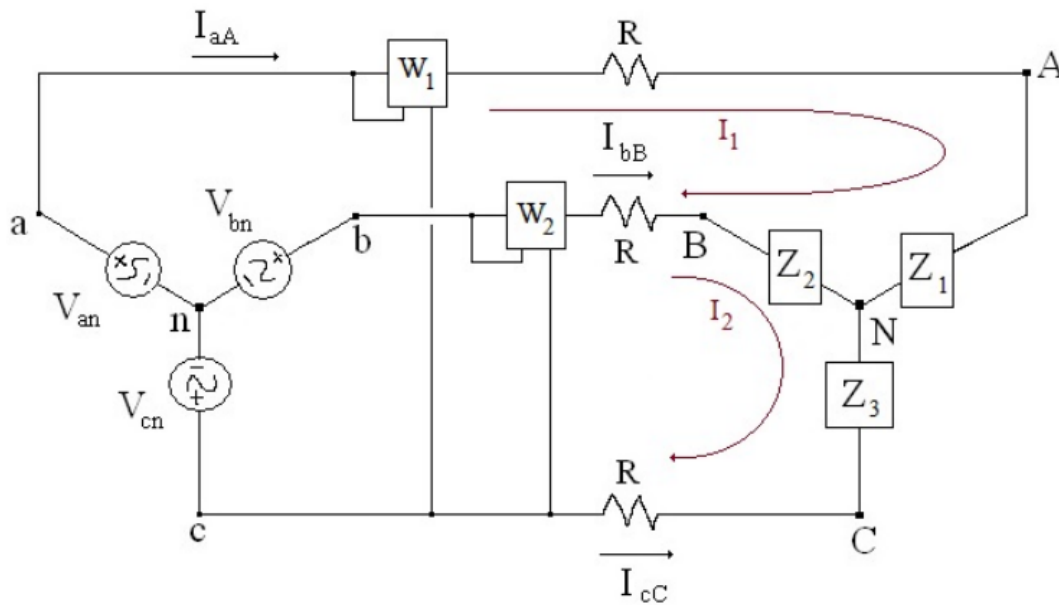
```



% hold off

2. Analisis por determinantes(Cramer) y metodo de Aron (2 vatimetros)

Circuito Y-Y



Fuente trifásica: $V_{an} = 100\angle 0^\circ V$, sec +
Resistencia líneas: $R = 0.5 \Omega$.

- 1 Proponga valores para las impedancias de carga.
- 2 Calcule la potencia compleja $S = VI^*$ para cada elemento del circuito.
- 3 Calcule la potencia de pérdidas.
- 4 Calcule las potencias de los dos vatímetros.
- 5 Muestre el balance de potencia.

```
Voltaje = 100;
```

```
V_an = pol_com(Voltaje/sqrt(2),0);      %Valores RMS
V_bn = pol_com(Voltaje/sqrt(2),-120);
V_cn = pol_com(Voltaje/sqrt(2),120);
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%1. En estos blocks proporcionamos los valores de impedancia
```

```
Z1 = 5+5i;
Z2 = 5+5i;
Z3 = 5+5i;
```

```
R = 0.5;
```

```
M_1=[(R+Z1+Z2+R); -(R+Z2)]          %impedancia malla 1
```

```
M_1 = 2x1 complex
```

```
11.0000 +10.0000i
-5.5000 - 5.0000i
```

```
M_2=[-(R+Z2); (R+Z2+Z3+R)] %impedancia malla 2
```

```
M_2 = 2x1 complex
-5.5000 - 5.0000i
11.0000 +10.0000i
```

```
M_V=[(V_an-V_bn); (V_bn-V_cn)] %Voltajes
```

```
M_V = 2x1 complex
10^2 x
1.0607 + 0.6124i
0.0000 - 1.2247i
```

```
%DETERMINANTES
```

```
DM_1_2=det([M_1,M_2]); % det
DM_V_2=det([M_V,M_2]); % I1
DM_1_V=det([M_1,M_V]); % I2
```

```
%CORRIENTE DE MALLA
```

```
I=[(DM_V_2/DM_1_2);(DM_1_V/DM_1_2)];
I1=I(1,1)
```

```
I1 = 7.0391 - 6.3992i
```

```
I2=I(2,1)
```

```
I2 = -2.0223 - 9.2956i
```

```
%CORRIENTE DE LINEA
```

```
I_aA = I1
```

```
I_aA = 7.0391 - 6.3992i
```

```
I_bB = I2- I1
```

```
I_bB = -9.0614 - 2.8964i
```

```
I_cC = -I2
```

```
I_cC = 2.0223 + 9.2956i
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%2. Calcule la potencia compleja
```

```
S_a = V_an*conj(I_aA);
```



```
S_b = V_bn*conj(I_bB);
S_c = V_cn*conj(I_cC);

S = round(S_a+S_b+S_c, 0)
```

```
S = 1.4930e+03 + 1.3570e+03i
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%3. Calcule la potencia de perdidas, aplicamos ley ohm para impedancias y
%aplicamos ley watt
```

```
S_R = round(R * (abs(I_aA^2) + abs(I_bB^2)+ abs(I_cC^2)),0)    %potencia perdida por la resistencia
```

```
S_R = 136
```

```
%CORRIENTES DE CARGA
```

```
I_Z1 = double(I1);
I_Z2 = double(I2-I1);
I_Z3 = double(-I2);
```

```
S_Z1 = abs(I_Z1*I_Z1)*Z1;
S_Z2 = abs(I_Z2*I_Z2)*Z2;
S_Z3 = abs(I_Z3*I_Z3)*Z3;
```

```
S_Z_carga = round(S_Z1+S_Z2+S_Z3)    %potencia consumida por la carga
```

```
S_Z_carga = 1.3570e+03 + 1.3570e+03i
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%4. Calcule la potencia de los dos vatimetros
```

$$P_{\text{total}} = P_{w1} + P_{w2}$$

$$P_{w1} = P_{\text{fase-fase}} \cdot \cos(\phi_{\text{linea}})$$

```
W1 = (V_an-V_cn)*conj(I_aA)
```

```
W1 = 1.1385e+03 + 2.4768e+02i
```

```
W2 = (V_bn-V_cn)*conj(I_bB)
```

```
W2 = 3.5474e+02 + 1.1098e+03i
```

```
W_total = (W1 + W2)
```

```
W_total = 1.4932e+03 + 1.3575e+03i
```

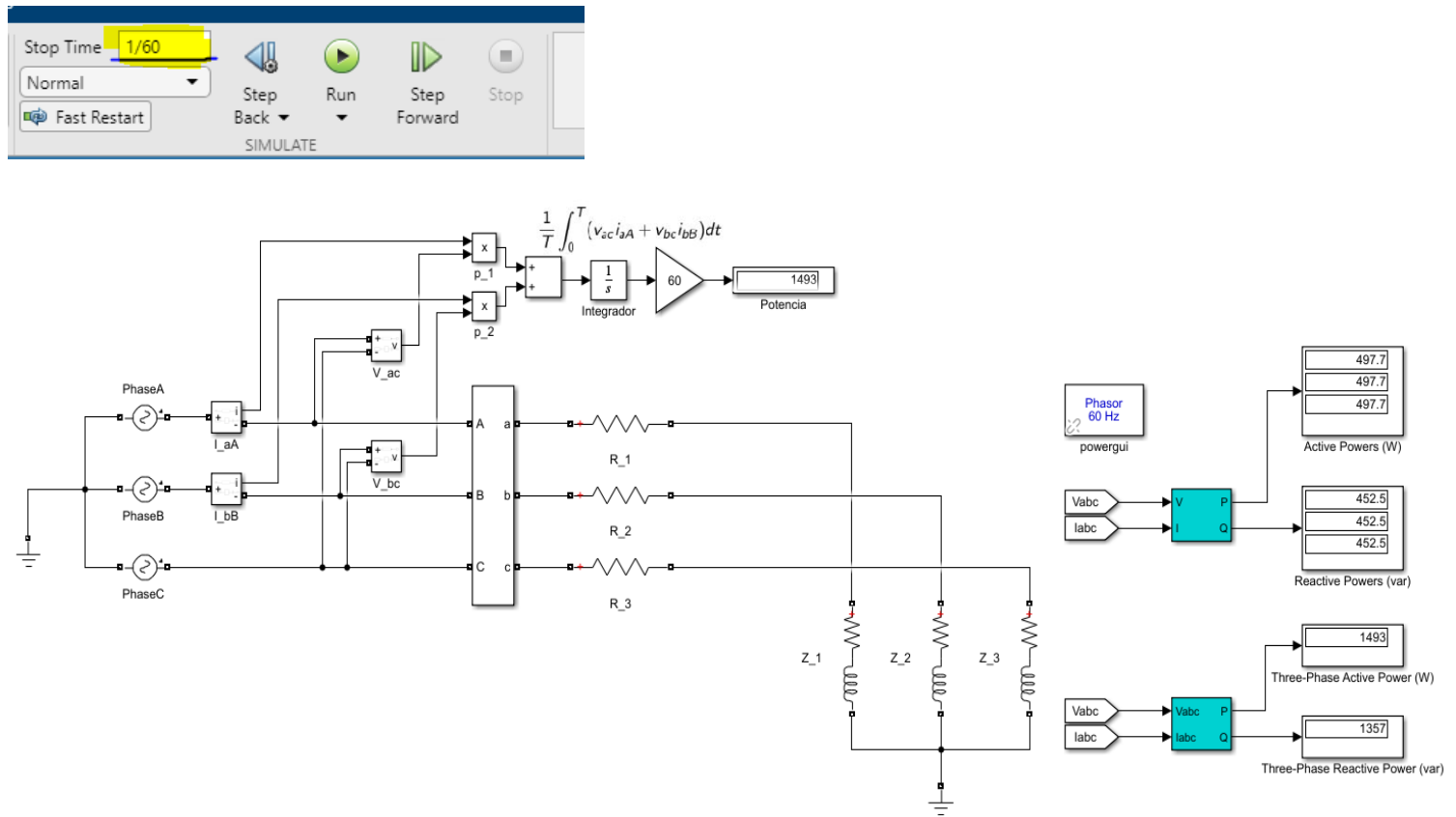
```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

%5. Balance de cargas

Balance = round(S_R + S_Z_carga - S, 0)

Balance = 0

Simulacion

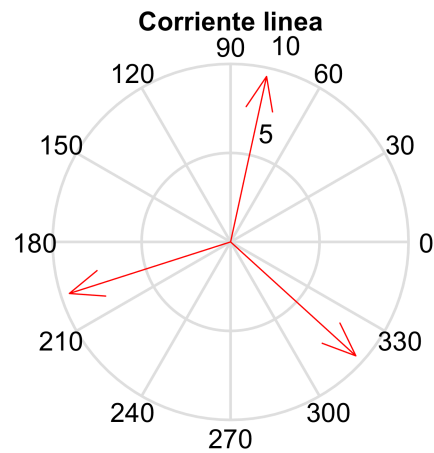
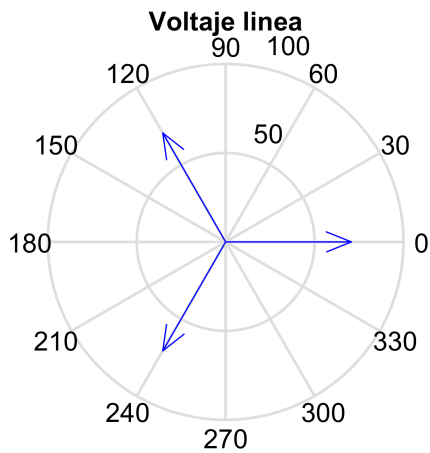


%herramienta interesante

```

tiledlayout(1,2)
ax1 = nexttile;
compass(ax1,[V_an V_bn V_cn], 'b')
title(ax1, 'Voltaje linea')
ax2 = nexttile;
compass(ax2,[I_aA I_bB I_cC], 'r')
title(ax2, 'Corriente linea')

```



3.Demostracion

Verificar la siguiente igualdad,

$$\frac{1}{T} \int_0^T (v_{an}i_{aA} + v_{bn}i_{bB} + v_{cn}i_{cC})dt = \frac{1}{T} \int_0^T (v_{ac}i_{aA} + v_{bc}i_{bB})dt$$

```
function Complejo = pol_com(M,A) % magnitud, angulo
Complejo = M * exp (deg2rad (A) * 1i);
end
```