



Volume Rendering

Volumetric Shading

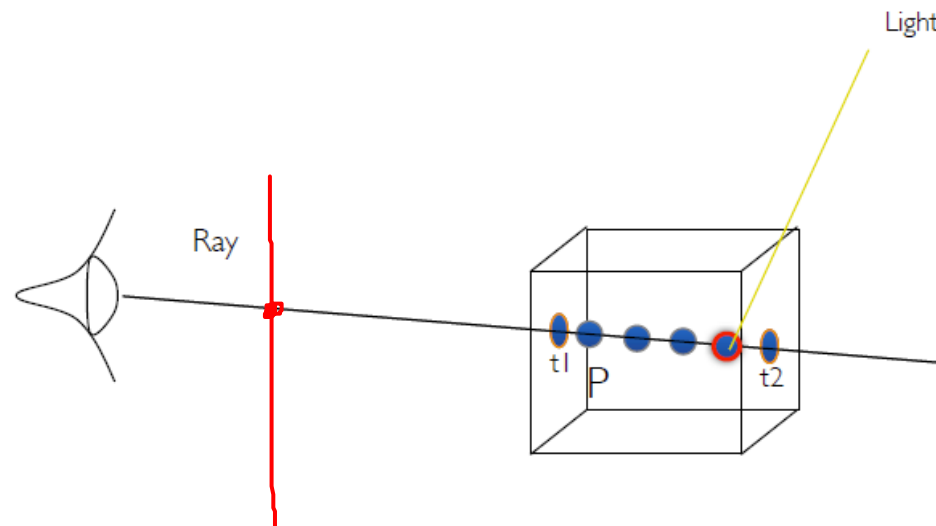
Scientific Visualization
Professor Eric Shaffer

Basic Idea

Shading allows viewers to perceive 3D shape and structure

Can apply shading to the volumetric data

Use it to modify light emitted at a sample point



The Blinn-Phong Reflection Model

$$I_p = k_a i_a + \sum_{m \in \text{lights}} (k_d (\hat{L}_m \cdot \hat{N}) i_{m,d} + k_s (\hat{H} \cdot \hat{V})^\alpha i_{m,s})$$

The material values are generated by the transfer function

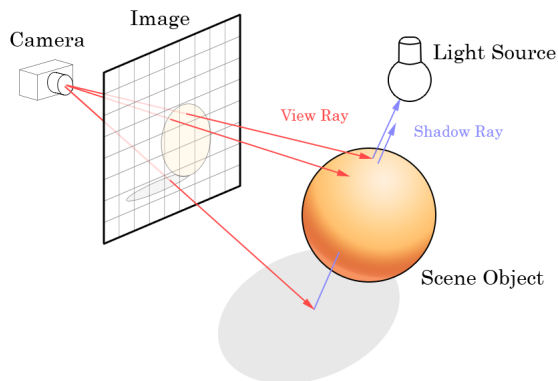
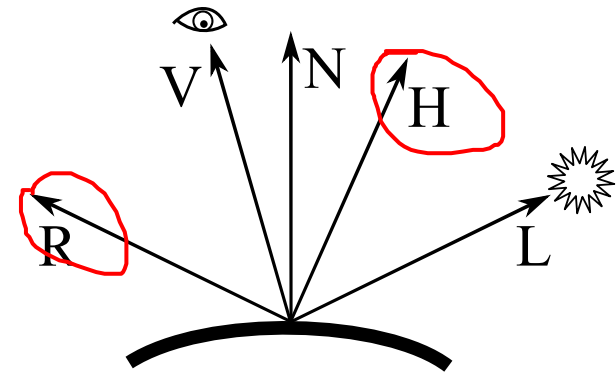
- k_a and $k_{m,s}$ and $k_{m,d}$
- Customary to use $(1,1,1)$ for i_a and $i_{m,s}$ and $i_{m,d}$

L is easy to compute given L_{pos} the light position: $L = \frac{L_{pos} - P}{\|L_{pos} - P\|}$

V can be computed using eyepoint E behind view plane: $V = \frac{E - P}{\|E - P\|}$

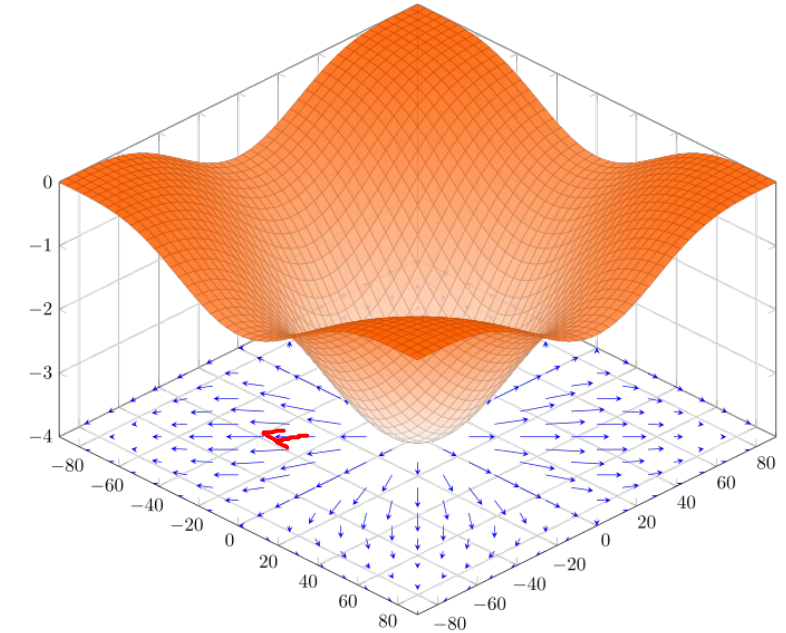
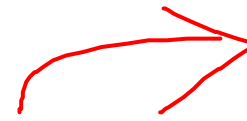
Can substitute H for R in the equation...with $H = \frac{V + L}{2}$

Need to compute the normal N



The Gradient

$$\nabla f(p) = \left\langle \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z} \right\rangle$$



Points in the direction of most rapid ascent in function values


Gradient of a function is normal to a contour of a function

Can use gradient as a normal...imagine point on the ray has been sampled from an isosurface

Approximating the Gradient

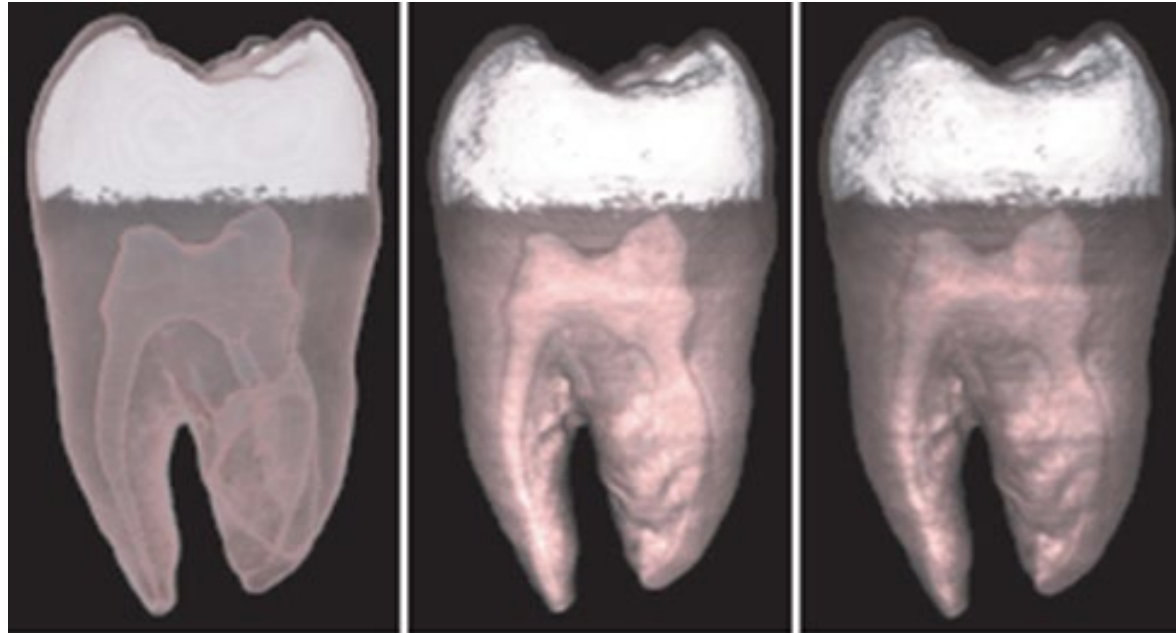
If the gradient cannot be determined analytically, can approximate it numerically
e.g when function f is unknown

central difference formula

$$\nabla f(p) \approx \left\langle \frac{f(x+h, y, z) - f(x-h, y, z)}{2h}, \frac{f(x, y+h, z) - f(x, y-h, z)}{2h}, \frac{f(x, y, z+h) - f(x, y, z-h)}{2h} \right\rangle$$


Use trilinear interpolation
to sample scalar field
values

Volumetric Shading



(a)

No Shading

(b)

Diffuse

(c)

Specular