

Domain Modeling

Data Structures for Polygonal Meshes

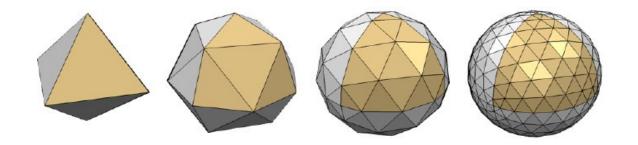
Scientific Visualization Professor Eric Shaffer



Mesh Data Structures

Need to store

- Geometry
- Connectivity



Can be used as file formats or internal formats

Considerations

- Space
- Efficient operations

Mesh processing has different requirements than rendering

• Example: Deforming a mesh when simulating physics...

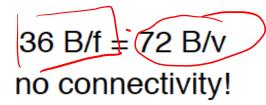


Mesh Data Structure: Face Set (STL)

- face:
 - 3 positions

	Triangles								
$\sqrt{1}$	X 11	y 11	$\mathbf{z}_{\mathbf{l}}$	X 12	Y 12	Z12	X 13	Y 13	\mathbf{z}_{13}
12	x ₂₁	Y 21	\mathbf{z}_{21}	x ₂₂	У 22	Z ₂₂	x ₂₃	Y 23	Z ₂₃
Í		• • •			• • •			• • •	
	X _F 1	y _{F1}	ZFl	XF2	Уг2	ZF2	XF3	У F3	ZF3





Designed in 1987 for stereolithography (3D printing technology)

No explicit information about which vertices are shared by which triangles Consider how efficiently we could:

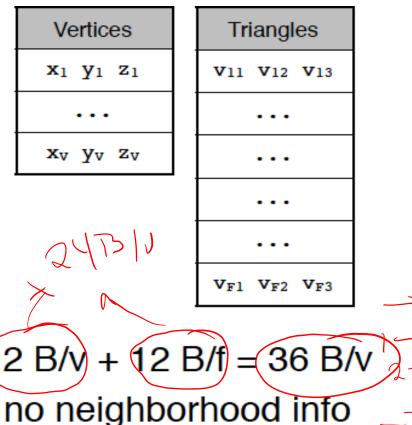
- Deform mesh by moving vertices
- Lookup vertex neighbor information

We will be focusing on triangle meshes...but all of these structures generalize to other polygons...storage requirements will change.



Mesh Data Structure: Indexed Face Set (OBJ)

- vertex:
 - position
- face:
 - vertex indices



2v こF

The OBJ file format is a popular storage format for meshes

Developed by Wavefront Technologies...now part of AutoDesk

Text files with .obj extension

```
# List of geometric vertices
v 0.123 0.234 0.345
v ...
v ...

# List of triangles
f 1 3 4
f 2 4 5
```

Indexed Face Set

One block of data are the vertices

- Each vertex is a set of 3 coordinates
- Often referred to as the geometry of the mesh

Another block of data is the set of triangles

- Each triangle is set of 3 integers vertex IDs
- The vertex IDs are indices into the vertex block

Vertices			
x_1 y_1 z_1			
•••			
$x_v y_v z_v$			

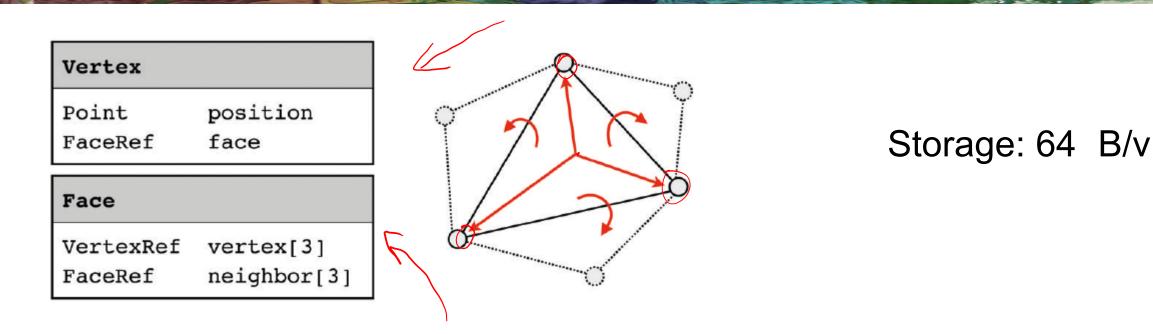
Triangles			
V11 V12 V13			
•••			
•••			
•••			
•••			
V _{F1} V _{F2} V _{F3}			

What are some advantages of this representation?

Disadvantages?



Face-Based Connectivity



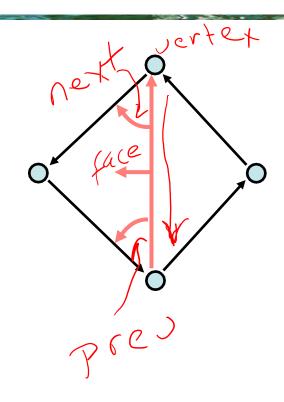
No edges: gathering vertex neighbors is not straight-forward...multiple cases



Vertex	
Point	position
HalfedgeRef	halfedge

Face	
HalfedgeRef	halfedge

Halfedge	
VertexRef	vertex
FaceRef	face
HalfedgeRef	next
HalfedgeRef	prev
HalfedgeRef	opposite





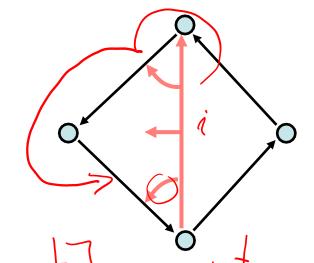
Vertex

Point position HalfedgeRef halfedge

Face

HalfedgeRef halfedge Halfedge

VertexRef vertex FaceRef face HalfedgeRef next HalfedgeRef prev HalfedgeRef opposite



HIJ. preu = HIHIJ. nextJ. next



Vertex

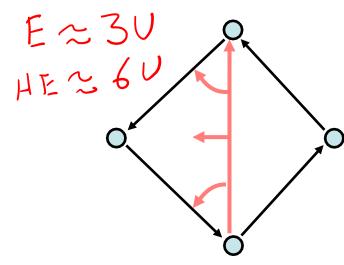
Point position HalfedgeRef halfedge

Face

HalfedgeRef halfedge

Halfedge

vertex VertexRef FaceRef face HalfedgeRef next HalfedgeRef prev HalfedgeRef opposite



96 to 144 B/v

16 150 + 3/0 + 72 3/0 = (963/0) no case distinctions during traversal

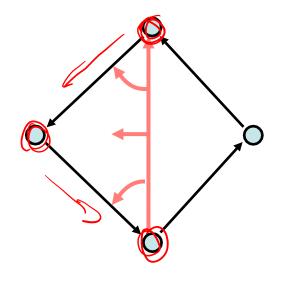


Halfedge Data Structure: Gathering Vertices

Vertex	
Point	position
HalfedgeRef	halfedge

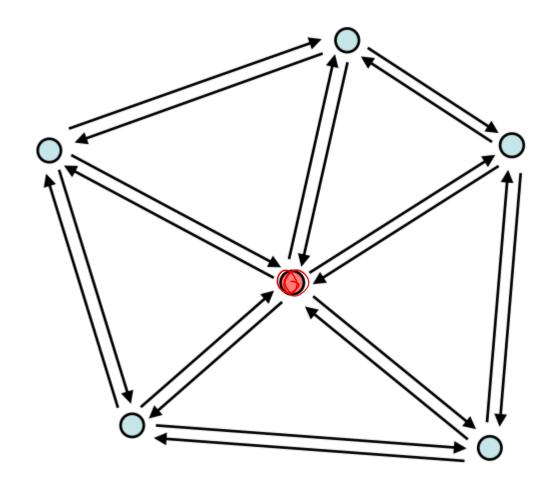
Face	
HalfedgeRef	halfedge

Halfedge	
VertexRef	vertex
FaceRef	face
HalfedgeRef	next
HalfedgeRef	prev
HalfedgeRef	opposite



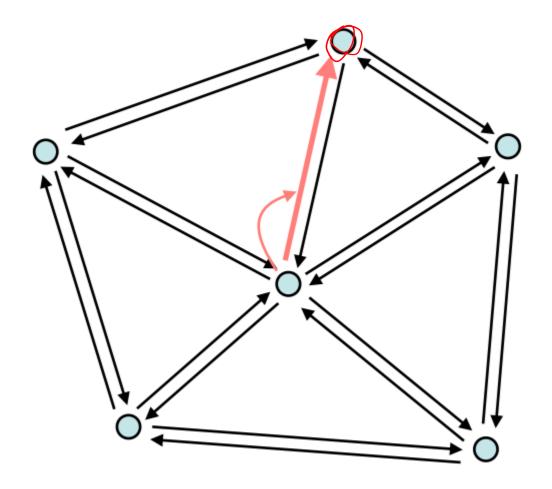


1. Start at vertex



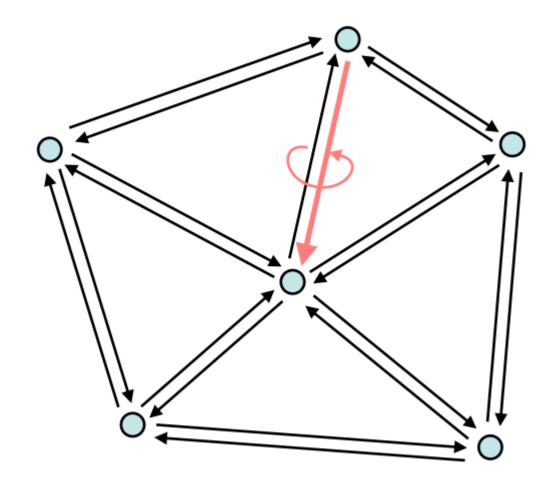


- 1. Start at vertex
- 2. Outgoing halfedge



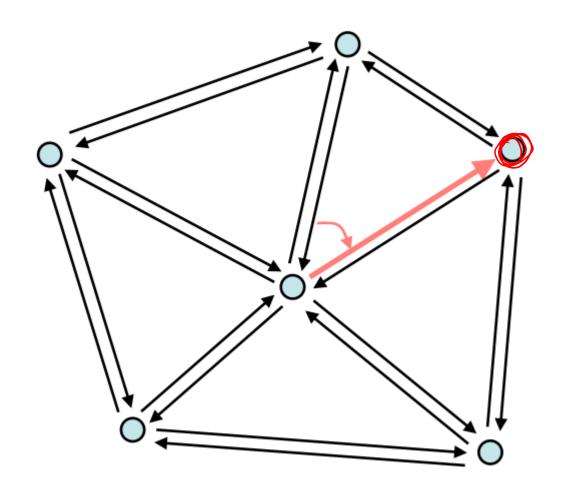


- 1. Start at vertex
- 2. Outgoing halfedge
- 3. Opposite halfedge



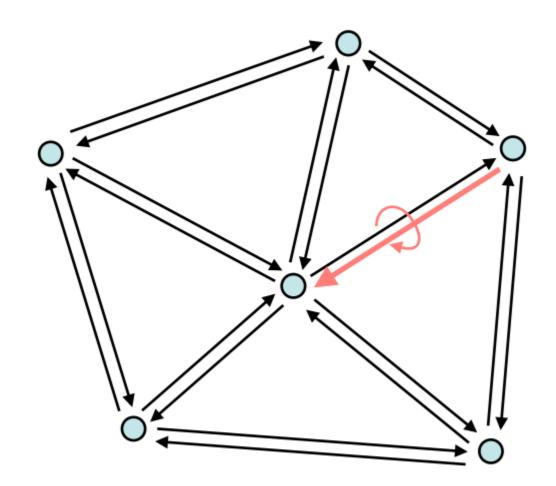


- 1. Start at vertex
- 2. Outgoing halfedge
- 3. Opposite halfedge
- 4. Next halfedge



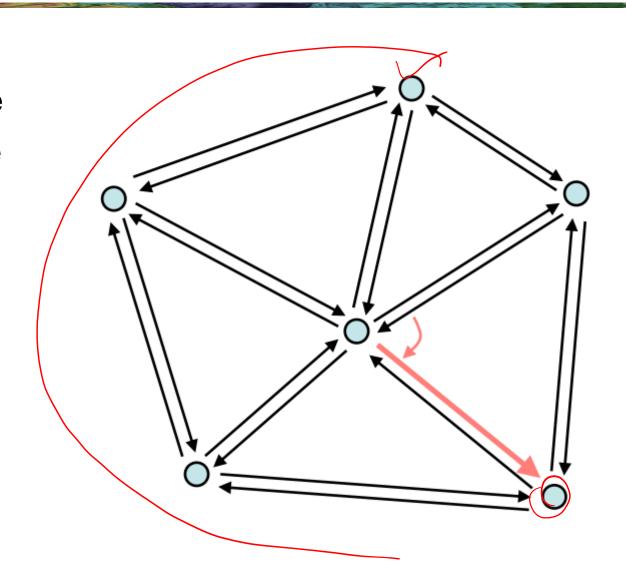


- 1. Start at vertex
- 2. Outgoing halfedge
- 3. Opposite halfedge
- 4. Next halfedge
- 5. Opposite





- 1. Start at vertex
- 2. Outgoing halfedge
- 3. Opposite halfedge
- 4. Next halfedge
- 5. Opposite
- 6.Next
- 7. ...

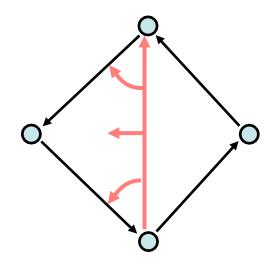




Vertex	
Point HalfedgeRef	position halfedge
Face	

HalfedgeRef halfedge

Halfedge	
VertexRef	vertex
FaceRef	face
HalfedgeRef	next
HalfedgeRef	prev
HalfedgeRef	opposite



Advantages:

- simple and efficient traversals of vertex neighborhoods
- can be applied to any polygonal mesh



Where to See Them in the Wild....

Computational Geometry Libraries

- CGAL
- OpenMesh

File Formats

- VTK (Visualization Toolkit)
- OBJ

More advanced formats as well...

- gltf for streaming (graphics file format...)
- cgns (computational fluid dynamics)
- ...lots of discipline specific formats

