



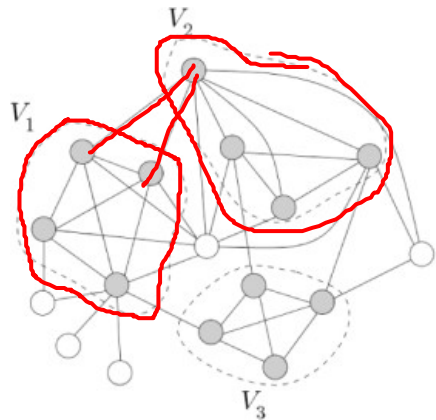
Large Graph Visualization

Edge Bundling

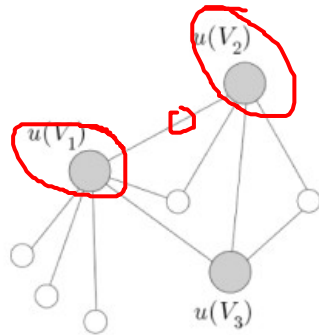
Scientific Visualization

Professor Eric Shaffer

Graph Aggregation



(a)



(b)

Produces a simpler/smaller 'cluster graph' from a large one

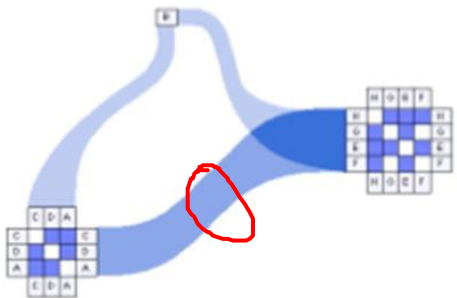
Vertices: partitioned between disjoint clusters

Edges: often aggregated between clusters

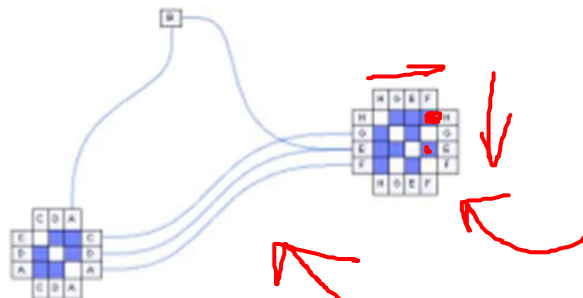
Many clustering methods (strongly-connected components, data based, ...)

Visualize the cluster graph

Cluster internals shown using a cluster icon (e.g. a matrix plot)



aggregated edges



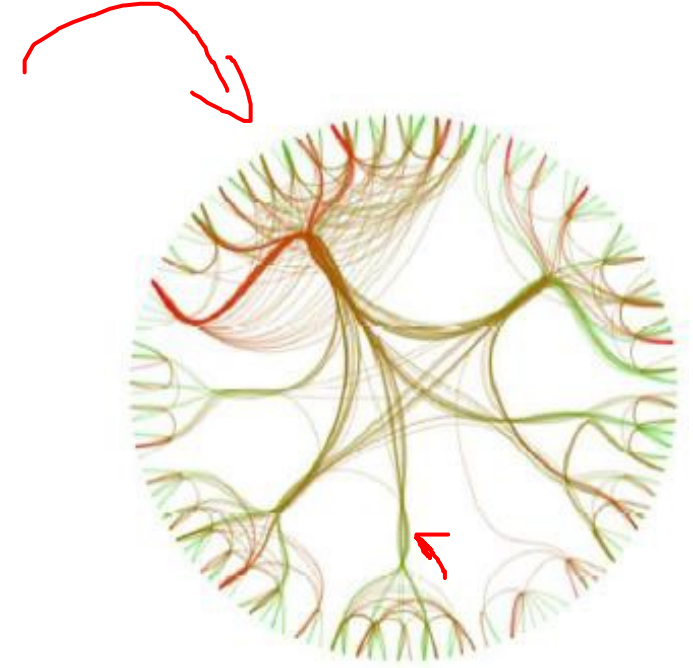
original edges

Graph Aggregation: Edge Bundling

- Edge bundles are clusters of similar edges
- Many approaches...usually cluster vertices
- Edges between clusters follow similar paths

Some metrics

- Shortest path distance to a “hub-node”
- Remove high-BC edges to discover clusters
- Lots of others.....

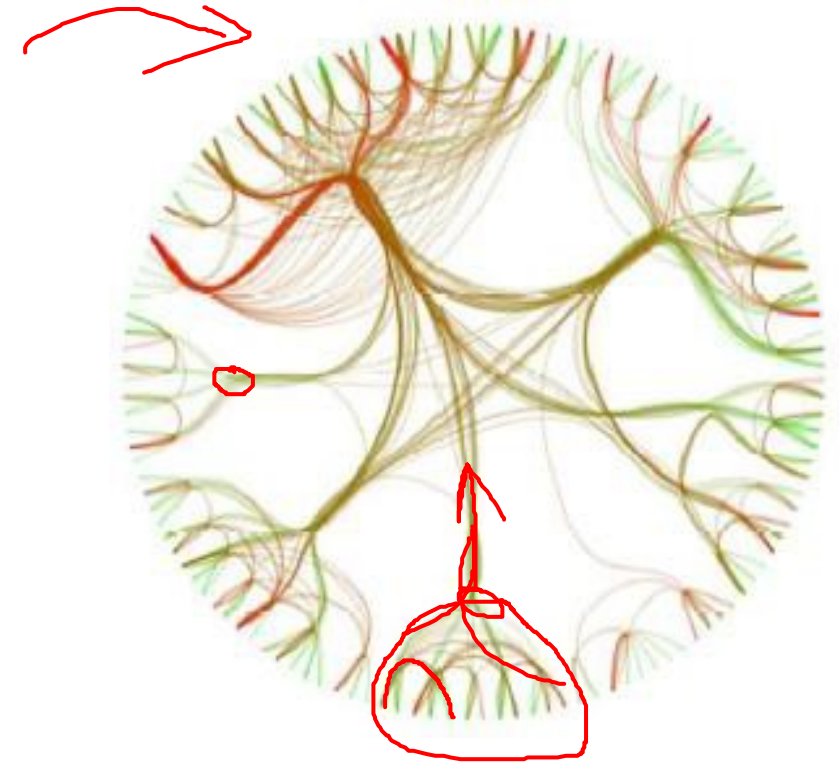


Hierarchical Edge Bundling: Example

Yuntao Jia, Michael Garland, John C. Hart:

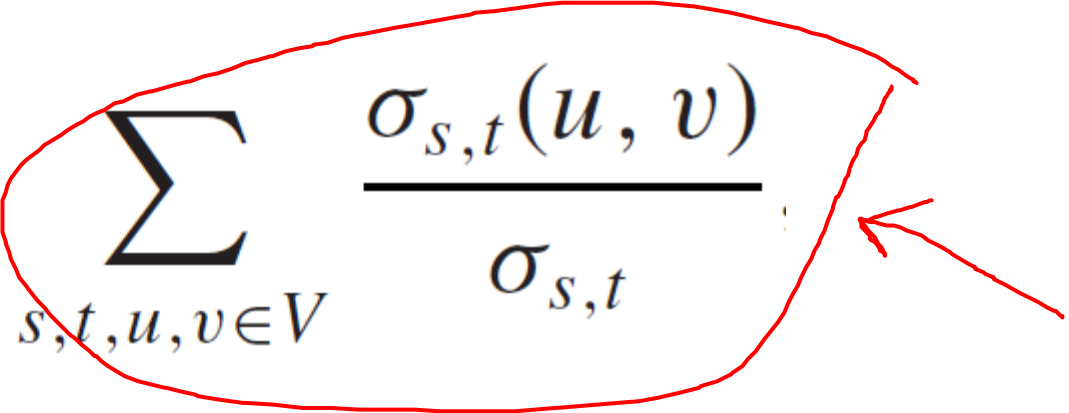
Social Network Clustering and Visualization using Hierarchical Edge Bundles.
Computer Graphics Forum (2011)

1. Generate a hierarchical structure of vertex clusters
2. Vertices are placed radially around circle
 1. Positions from in-order traversal of hierarchy
 2. Root nodes of clusters in interior, leaves on the perimeter
3. Edges are B-Spline curves
 1. Control points are hierarchy node layout positions
 2. Positions along shortest tree path between the two nodes



Community Discovery

- Edge betweenness centrality

$$\underline{BC(u, v)} = \sum_{s, t, u, v \in V} \frac{\sigma_{s, t}(u, v)}{\sigma_{s, t}}$$


- σ_{st} is the total number of shortest paths from node s to node t
- $\sigma_{st}(u, v)$ is the number of those paths that pass through edge u, v
- Low BC edges connect nodes within a community
- High BC edges connect communities

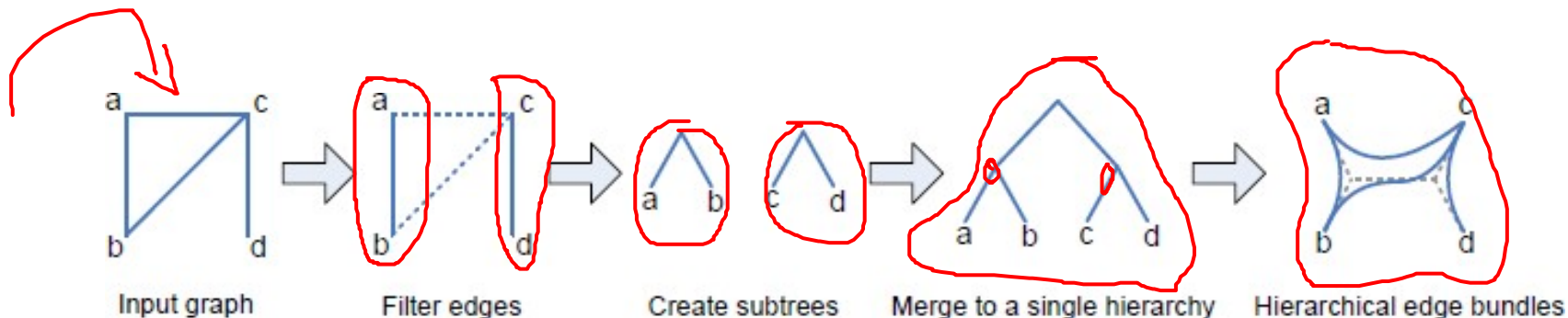
Balanced Hierarchy Construction

Filter edges by removing highest-bc edges first

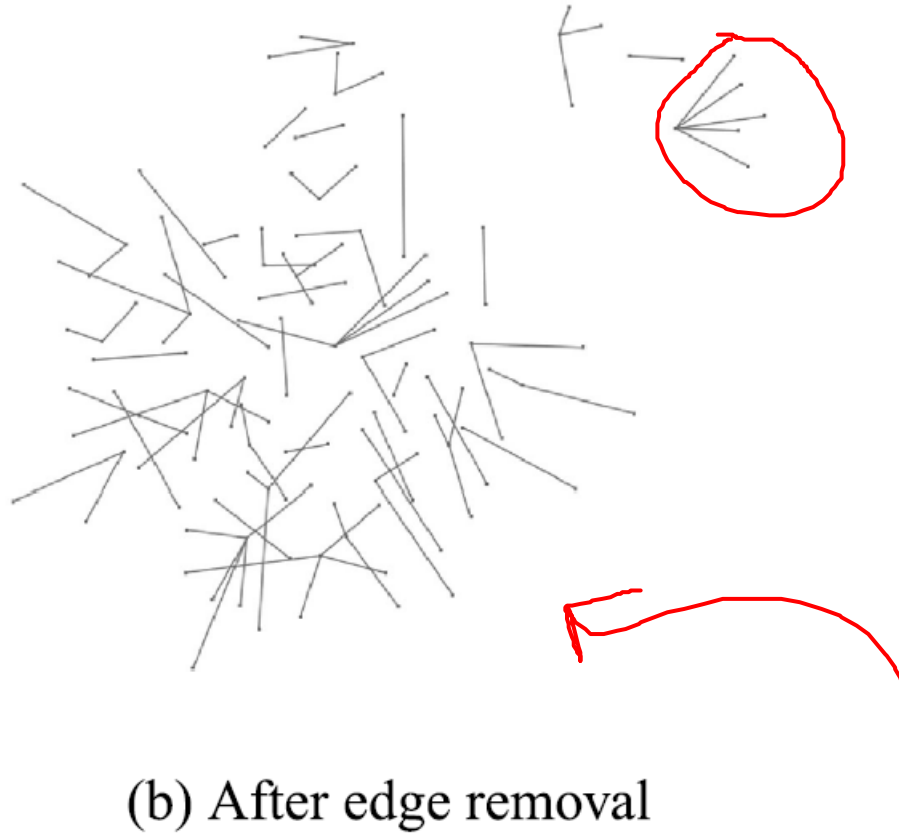
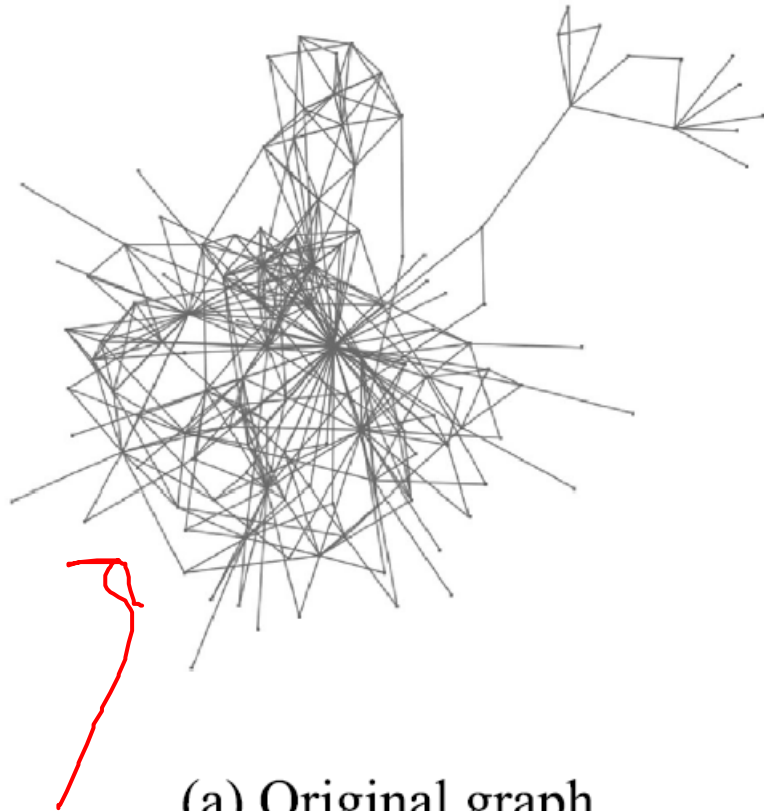
- An edge a,b is removed only if $\min(\deg(a), \deg(b)) > 1$
- And $BC(a,b) > 1$



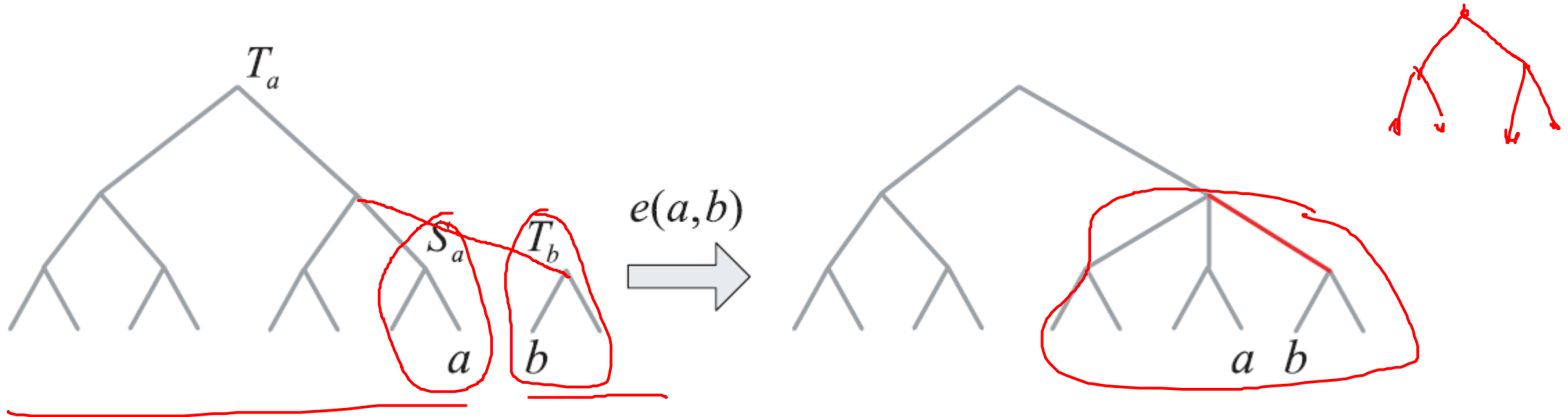
Construct communities by merging in increasing BC order of removed edges



Edge Removal



Merging Communities into a Hierarchy



We scan the list of removed edges in order of increasing BC and merge subtrees connected by those edges.

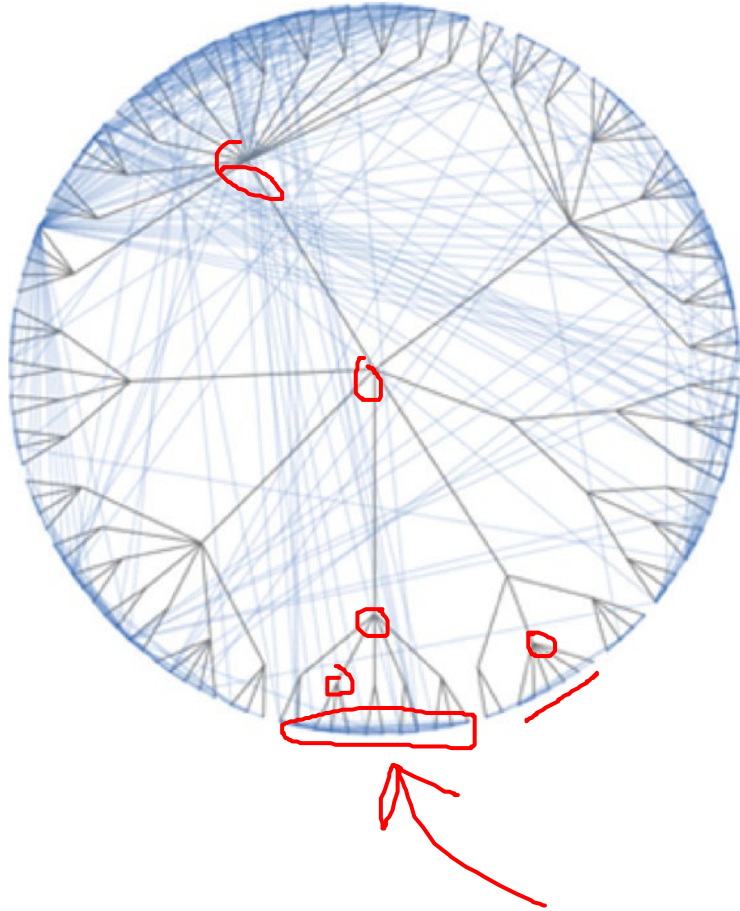
If T_a and T_b share the same height, then they can be merged as children of the same new parent tree node.

Otherwise assume without loss of generality that T_a is taller than T_b .

Let S_a be the unique (lowest) subtree of T_a that contains a and shares the same height as T_b .

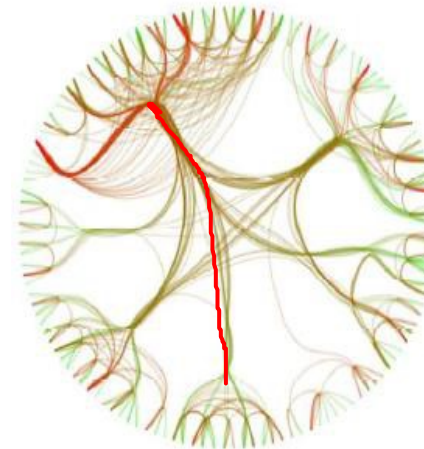
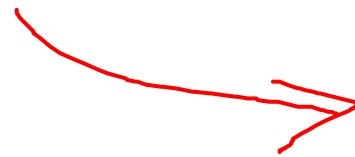
Then the communities are merged by assigning the parent of S_a as the parent of T_b .

Using the Hierarchy to Bundle Edges

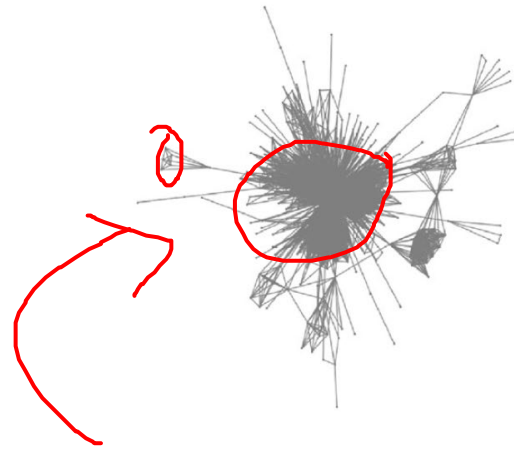


Gray lines show the computed hierarchy used to layout the graph
Blue lines show edges drawn linearly between nodes

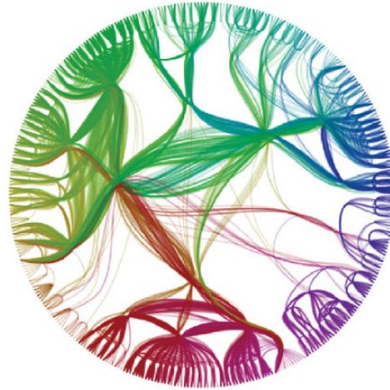
Edge bundling is accomplished by drawing them as curves
Curves with control points defined by the internal nodes
Edges between 2 communities will be drawn with similar curves



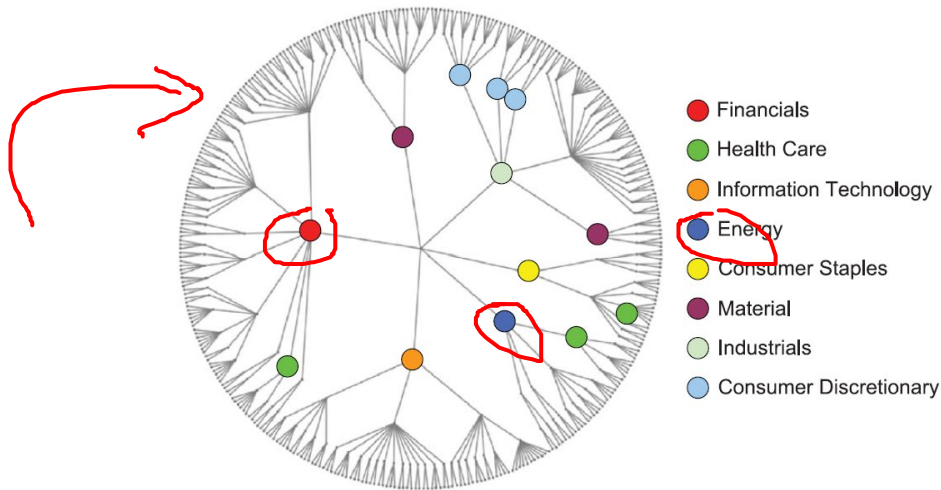
Example: E-mail in the Enron Scandal



(a) Original graph



(b) Edge Bundles



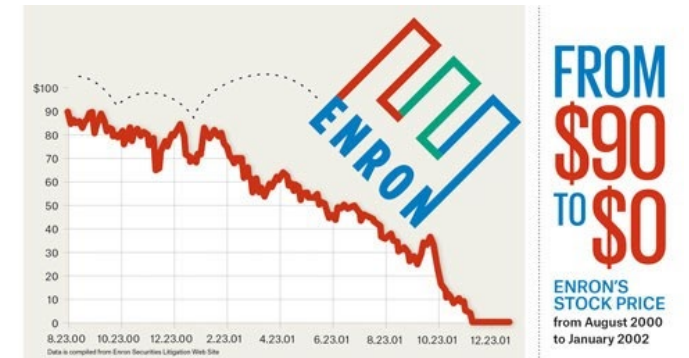
(c) Generated Hierarchy (with user supplied labels)

The Enron scandal was an accounting scandal of Enron Corporation, an American energy company based in Houston, Texas. It was publicized in October 2001, and led to the bankruptcy of the company, and the de facto dissolution of Arthur Andersen, which was one of the five largest audit and accountancy partnerships in the world. In addition to being the largest bankruptcy reorganization in American history at that time, Enron was cited as the biggest audit failure.

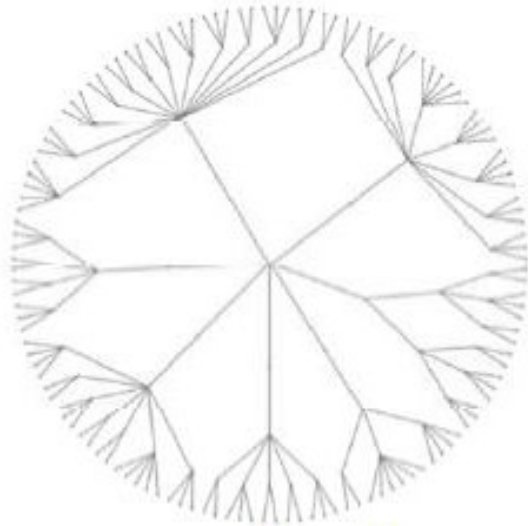
- Wikipedia



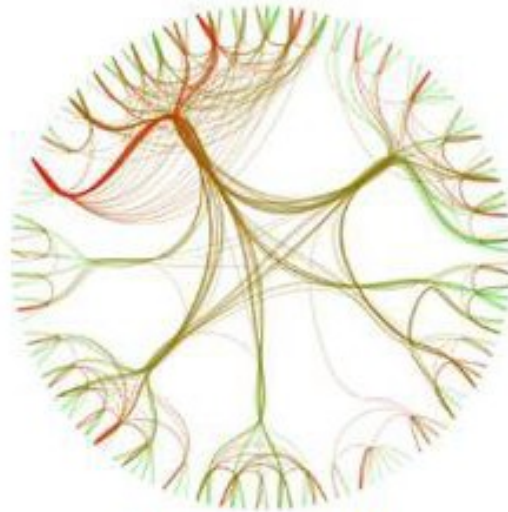
Endless possibilities.™



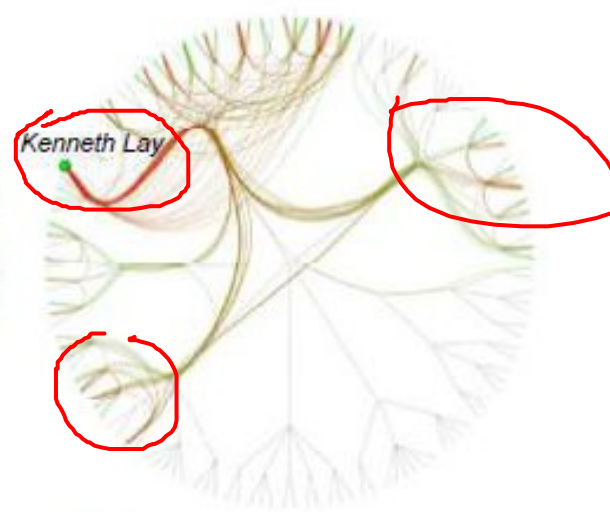
Enron E-Mail Graph



Fixed Depth



Edge Bundles



Selected visualization

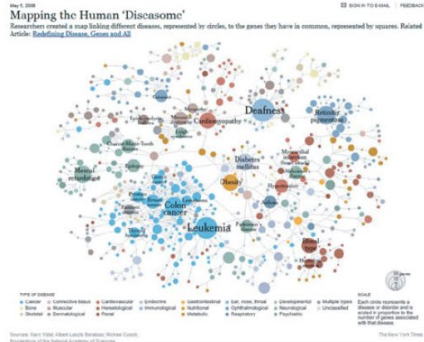
Enron scandal 2001

389 e-mails, 132 employees

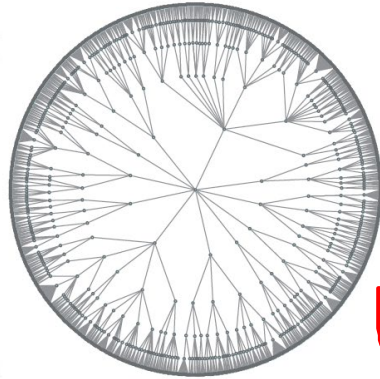
Red = sender, Green = recipient

Can select node to see which communities that person contacted

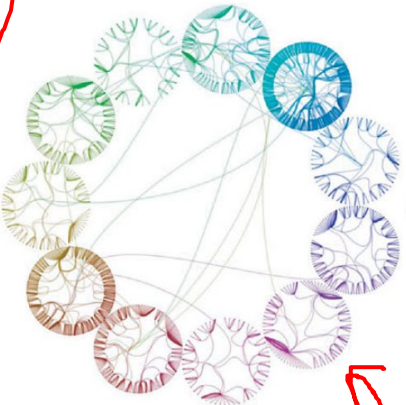
Example: Diseasome



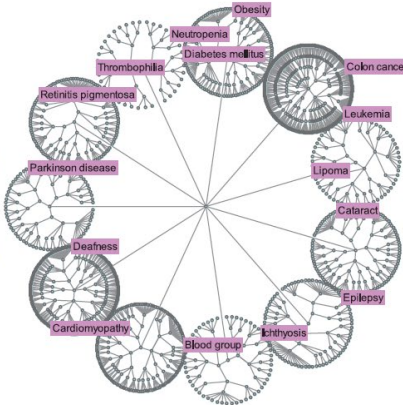
(a) “diseasome”



(b) Generated hierarchy



(c) Edge bundles



(d) Adaptive hierarchy drawing

A bipartite human disorder-gene network

1550 associations between 1419 disorders and genes

A disorder and gene connect if disorder arises from mutation of the gene

(a) shows a visualization of the network published in New York Times

- squares correspond to genes and circles correspond to disorders
- coloured by disorder types
- sized by the number of gene links

(b) HEB clusters form a community hierarchy

(d) Hierarchy laid out using adaptive tree drawing

- all first level internal nodes are drawn on different layout circles
- disorders are also labelled
- same type of disorders is likely clustered into the same community

(c) disorder–gene edge bundles are drawn on top of hierarchy

- seldom connections between communities