

The introduction of Tensorflow with Python

Parallel session of UCSAS 2020

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September 29, 2020

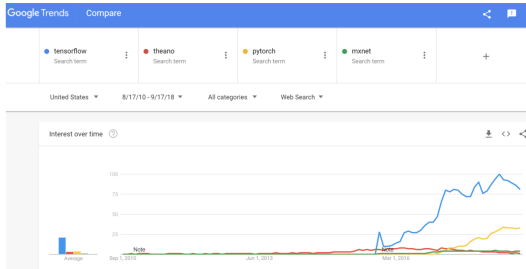


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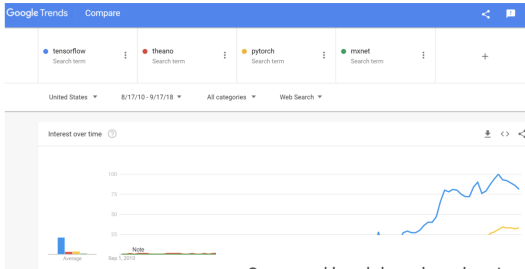
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Advantage

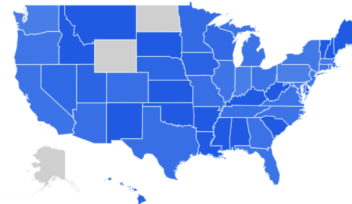


Advantage



Compared breakdown by subregion

● tensorflow ● theano ● pytorch ● mxnet



What is Tensor?

- Tensor is the data with dimension.
- 0-d tensor: scalar

$$c = 5$$

- 1-d tensor: vector

$$c = \begin{pmatrix} 1 \\ \vdots \\ 5 \end{pmatrix}$$

- 2-d tensor: matrix

$$c = \begin{pmatrix} 1 & \cdots & 5 \\ \vdots & \ddots & \vdots \\ 5 & \cdots & 5 \end{pmatrix}$$



Why Tensor special?

- Vector and matrix operations are dominant in machine learning and deep learning.

Example

$$(GD) : \hat{\beta}^{(t+1)} = \hat{\beta}^{(t)} - \gamma \nabla E_n \left[\ell \left(y, \hat{y} \left(\hat{\beta}^{(t)} \right) \right) \right]$$

- GPU structure leads to a powerful ability to solve linear tensor operations.

How to install Tensorflow in Python

- Anaconda management (GUI): click "environment" -> choose "Not installed" -> search "tensorflow"
- Anaconda Prompt:
`conda install tensorflow`
- Pip:
`pip install tensorflow`
- Verify whether your installation is successful: (open jupyter notebook or run at .py file)

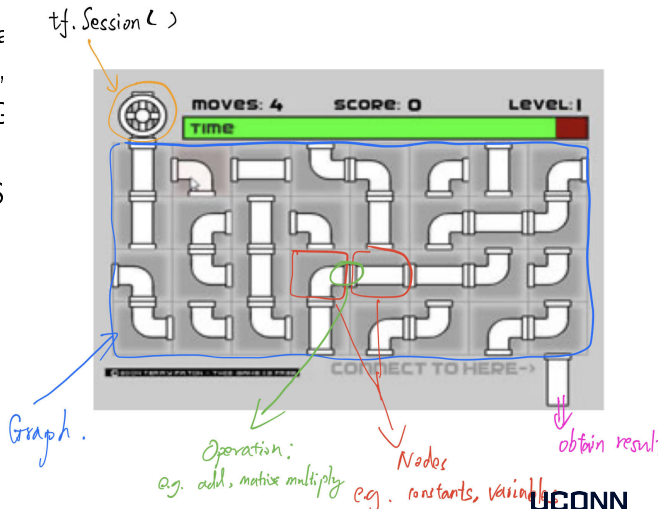
```
1 import tensorflow as tf
2 import tensorflow.compat.v1 as tfv1
3 tf.__version__
```

3 key concepts in tensorflow programming

- Operations: Data operations like "matmul" (matrix multiplication), "add".
- Graph: Build GRAPH which represents the data flow of the computation.
- Session: Run SESSION which executes the operations on the graph.

3 key concepts in tensorflow programming

- Operations: Data (e.g. matrix multiplication),
- Graph: Build computation.
- Session: Run S graph.



Basic widget: Constant

The constant can be either scalar, vector, or matrix. It is just a concept which is opposite with variable. Variable can be changed in the future by using `tf.assign()` method, while the constant can not.

```
1 s = tf.constant(2)
2 m = tf.constant([[1, 2], [3, 4]])
3 m = tf.constant([1, 2, 3, 4], shape=[2, 2])
```

With these two node, we can conduct a GRAPH and SESSION example. Here we use "tensorboard" for GRAPH and `tf.Session()` function for SESSION.

A simplest graph and session

```
1 g = tf.Graph()
2 with g.as_default():
3     s = tf.constant(2)
4     m = tf.constant([[1, 2], [3, 4]])
5     mmul = s*m
6 g
```

Here, we have already completed a graph, to "open the faucet", we use `tf.Session()`, like:

```
1 with tfv1.Session(graph=g) as sess:
2     print(sess.run(mmul))
```

Finally, we get the result. Remark: The `tf.Session()` only exist in tensorflow v1, so we call this function under v1 platform.

Basic widget: Variable

Variables are used to hold and update parameters. Another important difference with the constant is that it be treated as variable in the calculation of gradient. To create a variable,

```
1 w = tf.Variable(tf.ones((2,2))) # 2*2 matrix with all elements as 1
```

Alert

The variable must be initialized immediately after "the data faucet is open" (i.e. `tfv1.Session()`).

```
1 with tfv1.Session() as sess:  
2     sess.run(tfv1.global_variables_initializer())  
3     print(sess.run(w))
```

Basic widget: Variable

As we mentioned earlier, variable can be assigned with a new value.

```
1 with tfv1.Session() as sess:
2     sess.run(tfv1.global_variables_initializer())
3     print(sess.run(w))
4     # Change w to a 2*2 matrix with all elements as 0
5     sess.run(w.assign(tf.zeros((2,2))))
6     print(sess.run(w))
```

Basic widget: Placeholder

We can notice that although variable is more flexible than constant, it still need a initial value. In practice, sometimes the value of a parameter is determined by the actual data. So we need the placeholder to tell the PC, there is a variable, but I don't tell you the value, I will give you the value when I open the data faucet.

```
1 import numpy as np
2 node1 = tfv1.placeholder(tf.float32, shape = [1,2])
3 node2 = tfv1.placeholder(tf.float32, shape = [1,2])
4 w_linear = tf.matmul(node1,w) + node2
5 with tfv1.Session() as sess:
6     sess.run(tfv1.global_variables_initializer())
7     print(sess.run(w))
8     print(sess.run(w_linear, feed_dict={node1:np.matrix([1.0,2.0]),
9         node2:np.matrix([1.0,2.0])}))
```

Basic Operations

Given x and y ,

- $x+y$ (element-wise): `tf.add(x,y)`
- $x-y$ (element-wise): `tf.subtract(x,y)`
- $x*y$ (element-wise): `tf.multiply(x,y)`
- x/y (element-wise): `tf.divide(x,y)`
- $x*y$ (matrix style): `tf.matmul(x,y)`
- $x < y$ (judgment): `tf.less(x,y)`
- $x > y$ (judgment): `tf.greater(x,y)`
- $x \leq y$ (judgment): `tf.less_equal(x,y)`



Gradient

One of the most powerful thing for the Tensorflow is that it can calculate the gradient with a high flexibility and high speed. The core lines are:

```
1 with tf.GradientTape() as tape:  
2     y1 = <Expression of x1, x2, ... >  
3     y2 = <Expression of y1>  
4     tape.gradient(y2, [x1, x2, ...])
```

It returns the gradients of y2 with respect to x1, x2,... separately.

Alert

The gradient operation can only return value when it is with respect to a trainable variable.

Gradient



```
1 x = tf.Variable(3.0)
2 with tf.GradientTape() as tape:
3     y = x**2
4     dy_dx = tape.gradient(y, x)
5     # dy = 2x * dx
6 with tfv1.Session() as sess:
7     sess.run(tfv1.global_variables_initializer())
8     print(sess.run(dy_dx))
```

Basic Logic: If

The core line is:

```
1 tf.cond(tf_statement, A, B)
```

It implement a function that if `tf_statement` is true, then run `A`, otherwise, run `B`. By the way, if we want to choose from options more than 2, we can use `tf.switch_case()` function, that is not included in this session.

Example

```
1 t1 = tf.constant(1)
2 t2 = tf.constant(2)
3 def f1(): return t1+t2
4 def f2(): return t1-t2
5 res = tf.cond(t1<t2, f1, f2)
6 with tfv1.Session() as sess:
7     print(sess.run(res))
```

It will return 1+2 as 1 is indeed less than 2.

Basic Logic: While

The core line is:

```
1 tf.nn.whole_loop(tf_statement, body, variables)
```

It implement a function that if `tf_statement` is true, then run `body`, until `tf_statement` is false. The variables position need a tuple or list including all the tensorflow variables needed in the body part and `tf_statement` part. The loop will return the variables after the final iteration.

Example

```
1 t1 = tf.constant(1)
2 t2 = tf.constant(5)
3 body = (tf.add(t1, 1), t2)
4 def cond(t1, t2): return t1 < t2
5 def body(t1, t2):
6     t1 = tf.add(t1, 1)
7     return (t1, t2)
8 res = tf.nn.whole_loop(cond, body, (t1, t2))
9 with tf.nn.Session() as sess:
10     print(sess.run(res))
```

Framework

With all the knowledge we have learned, we now turn to something practical. Generally, we'd like the model training and model predicting to be simple, we prefer a using style likes the following:

```
1 model = model_creation_function()
```

Firstly, we use a certain `model_creation_function` to implement the initialization of variables and parameters we need, actually, it create a *class* data in Python. Then:

```
1 model.fit(x=..., y=...)
```

we hope this class type model hold a function called "fit", and the input should be `x` and `y` (in most cases of supervised learning).

Finally,

```
1 predict_value = model.predict(x=...)
```

we also hope this class type model hold functions for prediction, evaluation and etc.

Linear Regression Exercise

Given $X \in \mathbb{R}^{n \times 2}$ and $Y \in \mathbb{R}^n$, find a $\beta \in \mathbb{R}^2$ which is the OLS estimator for model

$$Y = X\beta + \varepsilon, \varepsilon \sim N(0, \sigma^2).$$

Key idea:

Implement the (loss) objective function:

$$L(\beta) = \|Y - X\beta\|^2.$$

Give any initial value $\hat{\beta}^{(0)} = (0, 0)^T$ and use the Gradient Descent method. The solution of this exercise is attached in the code directory. Thank you for listening. 🍁

Useful info

The material of this session is in [Session Material](#).

Our department website is [Department of Statistics](#).

Our website for statistical data science lab at Uconn is Data Science Lab

