CHECKLIST

- [X] Early stopping
- [X] Cost functions
- [X] Quadratic
- [X] Cross-entropy
- [X] log-likelihood
- [X] allow choice of cost function with a parameter
- [X] Momentum
- [X] L2 Regularization
- [X] Better initial weights
- [X] Transfer functions
- [X] tanh
- [X] softmax
- [X] ReLU
- [X] Minibatch shuffling
- [X] Learning rate schedule description
- [X] Returning learned network
- [X] Returning accuracy and costs for plotting
- [X] Did NOT include the MNIST data with my submission

Not sure, Details: Second test case for the iris dataset didn't perform as expected.

INSTRUCTIONS

The project code is stored in the file – **BackPropProj2.m**

function [weight, bias, acc, cost] = BackPropProj2(inputs, targets, nodeLayers, numEpochs, batchSize, eta, split, momentum, lambda, transFunction, costFun)

Input parameters to the function:

inputs: a matrix of input values

targets: a matrix of target/output values

nodeLayers: a vector with number of nodes in each layer (total number of node layers)

numEpochs: desired number of epochs to run batchSize: number of instances in a mini-batch

eta: learning rate for gradient descent

split: splits the data into training, testing and validation dataset (like [80 10 10])

momentum: momentum coefficient

lambda: lambda, the coefficient for L2 regularization

transFunction: activation or transfer function – 'sigmoid','tanh','relu' or 'softmax'

costFun: cost or error function – 'quadratic', 'cross-entropy' or 'log-likelihood'

Outputs generated:

weight: weights for each layer

bias: bias for each layer

acc: a cell array where first cell represents the training accuracy, and the second and the

third represent validation and testing accuracies respectively

cost: a cell where first cell represents the training cost, and the second and the third

represent validation and testing cost respectively

Invoking the function on the command window:

>> [weight bias acc cost] = BackPropProj2(irisinputs, iristargets, [4,20,3], 40, 10, 0.1, [80, 10, 10], 0.3, 5, 'sigmoid', 'cross');

Files included with submission:

BackPropProj2.m, dTransferPrime.m, transfer.m, SigmoidPrime.m

DESCRIPTION:

This project is implemented in Matlab and the code is well documented which helps to understand the functionality of the network.

function [weight, bias, acc, cost] = BackPropProj2(inputs, targets, nodeLayers, numEpochs, batchSize, eta, split, momentum, lambda, transFunction, costFun)

Overview:

The dataset is partitioned in train, test and validation sets using the ratio mentioned in the split parameter. 'dividerand' method is used to derive partitions.

Weights and biases are initialized by randn function with a mean of zero and std deviation of 1/sqrt(n-1).

Further, the input matrix is divided into mini batches as specified by the batchSize parameter and batch shuffling is done using the randperm function.

'transFunApply' function takes weighted inputs and applies transfer function as requested. The network is learned epoch by epoch and batch after batch –

Feedforward the network - For each layer z{layer} and a{layer} is calculated

The output layer Error for each activation function is computed

Hidden layer errors are then calculated and errors are back propagated through the network.

The momentum parameter is added to the Gradient Descent to find the minimum coefficients.

Final output layer errors, accuracies and correct values are computed and evaluated.

Early stopping strategy used- Validation cost is checked and halted when it increases after 65% of the total number of epochs.

Accuracy and cost plots are then generated.

CODE:

BackPropProj2.m

```
%CSC578 - Project 2
%Improving a Neural Network
%Oct 22, 2017
function [weight, bias, acc, cost] = BackPropProj2(inputs, targets, nodeLayers, numEpochs, batchSize,
eta, split, momentum, lambda, transFunction, costFun)
%Partition dataset into train, test and validation sets using split attribute
  if (isempty(split))
      trainInputs = inputs;
      testInputs = [];
      valInputs = [];
      trainTargets = targets;
      testTargets = [];
valTargets = [];
      % using the dividerand function to split - [trainInd,valInd,testInd] =
dividerand(Q,trainRatio,valRatio,testRatio)
      [trainInd, valInd, testInd] = dividerand((size(inputs,2)), split(1)/100, split(2)/100,
split(3)/100);
      trainInputs = inputs(:, trainInd);
      valInputs = inputs(:, valInd);
      testInputs = inputs(:, testInd);
      trainTargets = targets(:, trainInd);
      valTargets = targets(:, valInd);
      testTargets = targets(:, testInd);
  %Initializations
  L = size(nodeLayers,2); %total number of node layers
  weight = cell(1,L); %Initialize a cell to hold the weight
  bias = cell(1,L); %Initialize a cell to hold the biases
  bigDeltaWeight = {}; %Initialize a cell to hold deltas for the weights
  bigDeltaBias = {}; %Initialize a cell to hold deltas for the bias
  trainInputSize = size(trainInputs,2);%Hold size of the train inputs
  valInputSize = size(valInputs,2);%Hold size of the validation inputs
  testInputSize = size(testInputs,2);%Hold size of the test inputs
  batchValues = {}; %Initialize a cell to hold batch values
  targetValues = {}; %Initialize a cell to hold target values
  batchIndex = 1; %Initialize a counter variable
  %To store costs for training, testing and validation sets
  trainCost = zeros(1,numEpochs);
  testCost = zeros(1,numEpochs);
  valCost = zeros(1,numEpochs);
  %Initialize cells for accuracy and cost to hold the final train, validation and test values
  acc = {};
  cost = {};
  for layer = 2 : L
    weight{layer} = randn(nodeLayers(layer), nodeLayers(layer-1))/sqrt(nodeLayers(layer-1));
    bias{layer} = randn(nodeLayers(layer), 1);
  %Dividing the input matrix into mini batches
  %Increment by the value batchSize(step) for each iteration
  for initPos = 1:batchSize:trainInputSize
    if trainInputSize - initPos >= batchSize
        miniBatch = trainInputs(:, initPos:initPos+batchSize-1);
        batchValues{batchIndex} = miniBatch;
        target = trainTargets(:, initPos:initPos+batchSize-1);
        targetValues{batchIndex} = target;
        batchIndex = batchIndex + 1;
        miniBatch = trainInputs(:, initPos:end);
        batchValues{batchIndex} = miniBatch;
target = trainTargets(:, initPos:end);
        targetValues{batchIndex} = target;
```

```
end
  end
  %To diaplay output headers
  fprintf('
                                            VALIDATION
                                                                               TEST\n');
  fprintf(
  fprintf('Epoch | Cost | Corr | Acc | Cost | Corr | Acc | Cost | Corr | Acc \n');
  fprintf('--
\n');
 %Displaying user input for 'softmax' and 'relu' transfer functions
if (strcmp(transFunction, 'softmax'))
      userInSoftMax = input('User Input required: Softmax function can only be used in the last layer
 elseif (strcmp(transFunction,'relu'))
    userInReLu = input('User Input required: Relu can only be used in the hidden layers \n');
  function a = transFunApply(input)
    if (strcmp(transFunction, 'sigmoid'))
        a = transfer(input, transFunction);
    elseif (strcmp(transFunction, 'tanh'))
        if layer == L
            a = transfer(input, transFunction);
        else
            a = tanh(input);
        end
    elseif (strcmp(transFunction, 'relu'))
        if layer == L
            a = transfer(input, userInReLu);%ReLu cannot be used in the last layer.
        else
            a = max(0, input);
        end
    elseif (strcmp(transFunction, 'softmax'))
        if layer == L
            a = transfer(input, transFunction);
            a = transfer(input, userInSoftMax);%Cannot use softmax if it's the last layer
        error('Not a valid Transfer function. Input sigmoid, tanh, relu or softmax')
  %Loop through each epoch and batch
  for epoch = 1:numEpochs
      %Using the randperm function for minibatch shuffling
      random = randperm(size(batchValues,2));
      batchCounter = 1;
      for batch = 1:size(batchValues,2)
          z = \{\}; %Initialize a cell to hold values for the intermediate nodes
          a = \{\}; %Initialize a cell to hold the activation function
          a{1} = batchValues{random(batchCounter)}; %Input value of the batch is assigned to the first
element of the activation cell
          %Feedforward the network - For each layer calculate z{layer} and a{layer}
          for layer = 2 : L
             z{layer} = weight{layer} * a{layer - 1} + bias{layer};
             a{layer} = transFunApply(z{layer});
          end
          delta = {}; %Initialize a cell to hold the error values
          error = (a{L} - targetValues{random(batch)});
          %Calculating the output layer Error for each activation function
          if (strcmp(transFunction, 'tanh'))
            delta{L} = error .* (1-tanh(z{L}).^2);
          elseif (strcmp(transFunction, 'sigmoid'))
            delta{L} = error .* SigmoidPrime(z{L});
          elseif (strcmp(transFunction, 'softmax'))
            %If softmax is the trans function for the last output layer
            delta{L} = error .* ones(size(z{L}));
          elseif (strcmp(transFunction, 'relu'))
            if (strcmp(userInReLu, 'softmax'))
```

```
delta{L} = error .* ones(size(z{L}));
             else
                 delta{L} = error .* (dTransferPrime(z{L}, userInReLu));
             end
           end
           % Back propagate error through the network from L to 2nd layer
           % Calculating Hidden layer errors
           for layer = (L - 1) : -1 : 2
               if (strcmp(transFunction, 'softmax'))%If softmax is the transfer function - it cannot be
used in hidden layers
                 delta{layer} = (weight{layer + 1}.' * delta{layer + 1}) .* dTransferPrime(z{layer},
userInSoftMax);
                 delta{layer} = (weight{layer + 1}.' * delta{layer + 1}) .* dTransferPrime(z{layer},
transFunction);
               end
          end
         %Gradient Descent and finding the minimum
          %For each layer from L to 2nd layer
           for layer = L : -1 : 2
               if epoch == 1 && batch == 1
                   -
weight{layer} = weight{layer} - eta/length(batchValues{random(batch)}) * delta{layer}
* a{layer - 1}.';
                   bias{layer} = bias{layer} - eta/length(batchValues{random(batch)}) *
sum(delta{layer}, 2);
                   bigDeltaWeight{layer} = eta/length(batchValues{random(batch)}) * delta{layer} *
a{layer - 1}.';
                   bigDeltaBias{layer} = eta/length(batchValues{random(batch)}) * sum(delta{layer}, 2);
               else %Using the momentum parameter to find the minimum coefficients
  weight{layer} = weight{layer} + bigDeltaWeight{layer};
                   bias{layer} = bias{layer} + bigDeltaBias{layer};
bigDeltaWeight{layer} = momentum .* bigDeltaWeight{layer} -
eta/length(batchValues{random(batch)}) * delta{layer} * a{layer - 1}.';
                   bigDeltaBias{layer} = momentum .* bigDeltaBias{layer} -
eta/length(batchValues{random(batch)}) * sum(delta{layer}, 2);
           end
           batchCounter = batchCounter + 1;
      %Compute final output values after updating weights
      trainOut = {}; %Initialize a cell to hold the final training output values
      trainOut{1} = trainInputs; %Assign inputs to first element of the output cell
      valOut = {}; %Initialize a cell to hold the final validation output values
      valOut{1} = valInputs;
      testOut = {}; %Initialize a cell to hold the final testing output values
      testOut{1} = testInputs;
      ztrain = cell(1,L);
      zval = cell(1,L);
      ztest = cell(1,L);
      weightSum = 0:
      %For each layer from the 2nd layer
      for laver = 2 : L
          ztrain{layer} = (weight{layer} * trainOut{layer-1}) + (bias{layer});
zval{layer} = (weight{layer} * valOut{layer-1}) + (bias{layer});
ztest{layer} = (weight{layer} * testOut{layer-1}) + (bias{layer});
           trainOut{layer} = transFunApply(ztrain{layer});
           valOut{layer} = transFunApply(zval{layer});
           testOut{layer} = transFunApply(ztest{layer});
           weightSum = weightSum + sum(sum(weight{layer}.^2));
      L2Train = lambda/(2*trainInputSize) * weightSum;
      L2Val = lambda/(2*valInputSize) * weightSum;
      L2Test = lambda/(2*testInputSize) * weightSum;
      %Compute the number of correct cases
      %correct = correct + sum(all(targets==round(output{L}),1),2);
      trainCorrect = sum(all(trainTargets == round(trainOut{L}),1),2);
      valCorrect = sum(all(valTargets == round(valOut{L}),1),2);
```

```
testCorrect = sum(all(testTargets == round(testOut{L}),1),2);
      %Computing train, validation and test set accuracies
      trainAccuracy = trainCorrect/trainInputSize;
valAccuracy = valCorrect/valInputSize;
      testAccuracy = testCorrect/testInputSize;
      % Computing cost
      if (strcmp(costFun, 'quad')) %Quadratic
    trainCost = 1/(2*trainInputSize) * sum(sum((0.5*(trainTargets - trainOut{L}).^2)))+L2Train;
          valCost = 1/(2*valInputSize) * sum(sum((0.5*(valTargets - valOut{L}).^2)))+L2Val;
          testCost = 1/(2*testInputSize) * sum(sum((0.5*(testTargets - testOut{L}).^2)))+L2Test;
      elseif (strcmp(costFun, 'cross')) %Cross-Entropy
          trainCost = -1/(trainInputSize) .* sum(sum(trainTargets .* log(trainOut{L}+eps) + (1-
trainTargets) .* log(1-trainOut{L}))+eps)+L2Train;
          valCost = -1/(valInputSize) .* sum(sum(valTargets .* log(valOut{L}+eps) + (1-valTargets) .*
log(1-valOut{L}))+eps)+L2Val;
          testCost = -1/(testInputSize) .* sum(sum(testTargets .* log(testOut{L}+eps) + (1-testTargets)
.* log(1-testOut{L}))+eps)+L2Test;
      elseif (strcmp(costFun, 'log')) %log-likelihood
          trainCost = sum(-log(max(trainOut{L}))+eps)/trainInputSize)+L2Train;
          valCost = sum(-log(max(valOut{L}))+eps)/valInputSize)+L2Val;
          testCost = sum(-log(max(testOut{L}))+eps)/testInputSize)+L2Test;
      % store costs for early stopping
      trainCost(epoch) = trainCost;
      valCost(epoch) = valCost;
      testCost(epoch) = testCost;
      fprintf('%d\t| %.5f | %d/%d | %.5f || %.5f | %d/%d | %.5f || %.5f | %d/%d | %.5f\n', ...
      epoch, trainCost(epoch), trainCorrect, trainInputSize, trainAccuracy,...
      valCost(epoch), valCorrect, valInputSize, valAccuracy,...
      testCost(epoch),testCorrect,testInputSize,testAccuracy);
      %Early stopping conditions and plots
      %Storing accuracy and costs for each epoch
      acc{1}(epoch) = trainAccuracy;
      acc{2}(epoch) = valAccuracy;
      acc{3}(epoch) = testAccuracy;
      cost{1}(epoch) = trainCost(epoch);
      cost{2}(epoch) = valCost(epoch);
      cost{3}(epoch) = testCost(epoch);
      %Early Stopping based on Accuracy -- If all the input cases are correct - accuracy=1
      if trainCorrect == trainInputSize && valCorrect == valInputSize && testCorrect == testInputSize
          fprintf('Accuracy is 1 and all the cases are identified correct - Early stopping \n');
          subplot(2,1,1)
          plot(cost{1}); hold on; plot(cost{2});plot(cost{3});
          title('Cost plot'); xlabel('Number of epochs'); ylabel('cost');
          legend('Training cost', 'Validation cost', 'Testing cost');hold off;
          subplot(2,1,2):
          plot(acc{1});hold on;plot(acc{2});plot(acc{3});
          title('Accuracy plot'); xlabel('Number of epochs'); ylabel('Accuracy'); legend('Training acc', 'Validation acc', 'Testing acc'); hold off;
      %Early stopping strategy - check if Validation cost increases when the number of epochs is
greater than 65% of the epochs
      elseif epoch > round(numEpochs*0.65)
          if valCost(epoch) > valCost(epoch-1)
              subplot(2,1,1);
              fprintf('Validation cost increased after 65 percent of epochs were executed -- Early
stopping criteria \n');
              plot(cost{1}); hold on;plot(cost{2}); plot(cost{3});
              title('Cost plot'); xlabel('Number of epochs'); ylabel('cost');
              legend('Training cost', 'Validation cost', 'Testing cost');hold off;
              subplot(2,1,2);
              plot(acc{1}); hold on;plot(acc{2}); plot(acc{3});
              title('Accuracy plot'); xlabel('Number of epochs'); ylabel('Accuracy');
              legend('Training acc', 'Validation acc', 'Testing acc'); hold off;
          end
      else
```

```
subplot(2,1,1);
          plot(cost{1}); hold on; plot(cost{2}); plot(cost{3});
           title('Cost plot'); xlabel('Number of epochs'); ylabel('cost');
          legend('Training cost','Validation cost', 'Testing cost');hold off;
          plot(acc{1});hold on;plot(acc{2}); plot(acc{3});
          title('Accuracy plot'); xlabel('Number of epochs'); ylabel('Accuracy'); legend('Training acc', 'Validation acc', 'Testing acc'); hold off;
      end
  end
end
transfer.m
%Brunda Chouthoy
%CSC578 - Project 2
%Improving a Neural Network
%Oct 22, 2017
%Transfer functions
function f = transfer(z, fun)
    if (strcmp(fun, 'sigmoid'))
    f=logsig(z);
    elseif (strcmp(fun, 'tanh'))
       f=tanh(z);
    elseif (strcmp(fun, 'relu'))
        f=max(0,z);
    elseif (strcmp(fun, 'softmax'))
        f=softmax(z);
dTransferPrime.m
%Brunda Chouthoy
%CSC578 - Project 2
%Improving a Neural Network
%Oct 22, 2017
%dTransfer function finds derivative of the activation function
function df = dTransferPrime(z, fun)
    if (strcmp(fun, 'sigmoid'))
        df=transfer(z,fun).*(1-transfer(z,fun));
    elseif (strcmp(fun, 'tanh'))
        df=1-transfer(z,fun).^2;
    elseif (strcmp(fun, 'relu'))
        df=double(z>0);
    elseif (strcmp(fun, 'softmax'))
        df=transfer(z,fun).*(1-transfer(z,fun));
    end
```

ANALYSIS:

The implemented network in this project works properly for all the datasets with changes in the number of hidden layers, number of epochs, learning rates, lambda regularization and momentum coefficients, different transfer functions (softmax, relu, tanh and sigmoid) and cost functions (quad, cross and log). The code was tested using 3 different datasets – iris.csv, MNIST and xor.csv for different configuration settings. The outputs and the graphs are displayed in the output section below. Second test case provided for the iris dataset with 'relu' transfer function didn't seem to perform as expected – the accuracy values are very low.

IDEAS FOR ENHANCEMENT:

- Make this network more scalable by increasing the dataset size so that the network is exposed to different samples of data and will result is a better performance.
- Use a grid search method to choose the best configuration parameters for the network that results in better and higher performance.

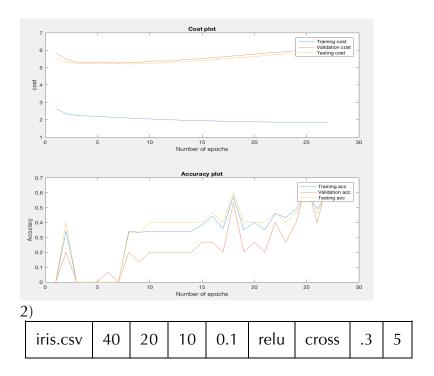
OUTPUTS:

1)

data set	epochs	hids	batch	eta	trans.	cost	mom.	reg.
iris.csv	40	20	10	0.1	sigmoid	cross ^A	.3	5

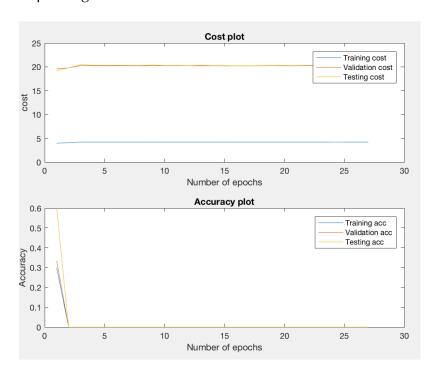
```
>> iris = csvread('iris.csv');
>> irisinputs = iris(:, 1:4).';
>> iristargets = iris(:, 5:7).';
>> BackPropProj2(irisinputs, iristargets, [4,20,3], 40, 10, 0.1, [80, 10, 10], 0.3, 5, 'sigmoid', 'cross');
```

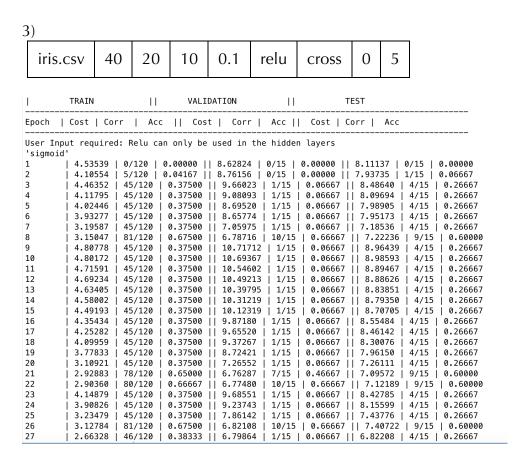
```
>> BackPropProj2(irisinputs, iristargets, [4,20,3], 40, 10, 0.1, [80, 10, 10], 0.3, 5, 'sigmoid', 'cross');
         TRAIN
                         -11
                                 VALIDATION
                                                     \Box
                                                                 TEST
Epoch | Cost | Corr | Acc || Cost | Corr | Acc || Cost | Corr | Acc
          2.64638 |
                    0/120 | 0.00000 || 5.83945 | 0/15 | 0.00000 || 5.51796 | 0/15 | 0.00000
          2.35151
                    41/120 | 0.34167 || 5.47846 | 3/15 | 0.20000 || 5.30385 | 6/15 | 0.40000
                            0.00000 || 5.31092 | 0/15 | 0.00000 || 5.23139 |
          2.23811
                    0/120 I
                                                                             0/15 I
                                                                                    0.00000
          2.21136
                    0/120
                            0.00000
                                    || 5.29809
                                                 0/15
                                                        0.00000
                                                                   5.21933
                                                                             0/15
                                                                                    0.00000
          2.18804
                    0/120
                            0.00000
                                                 0/15
                                                        0.00000
                                                                   5.22957
                                       5.31272
                                                                              0/15
                                                                                     0.00000
          2.15549
                    0/120
                            0.00000
                                       5.29425
                                                 1/15
                                                        0.06667
                                                                   5.22184
                                                                             0/15
                                                                                     0.00000
          2.12765
                    0/120 |
                            0.00000 || 5.26462
                                                 0/15 |
                                                        0.00000 ||
                                                                   5.23557
                                                                             0/15 I
                                                                                     0.00000
                           | 0.34167
          2.09462
                    41/120
                                        5.29781
                                                1 3/15
                                                         0.20000
                                                                  11 5.20374
                                                                             1 5/15
                                                                                      0.33333
                                                                    5.22369
          2.06281
                    40/120
                             0.33333
                                        5.30313
                                                  2/15
                                                         0.13333
                                                                              5/15
          2.04188
                    41/120
                             0.34167
                                        5.35652
                                                  3/15
                                                         0.20000
                                                                    5.23923
                                                                              6/15
                                                                                      0.40000
10
11
          2.01743
                    41/120
                             0.34167
                                        5.38174
                                                  3/15
                                                         0.20000
                                                                    5.26591
                                                                              6/15
                                                                                      0.40000
12
          1.99362
                    41/120
                             0.34167
                                        5.38544
                                                  3/15
                                                         0.20000
                                                                    5.30304
                                                                               6/15
                                                                                      0.40000
          1.97353
                             0.34167
                                        5.44561
                                                         0.20000
                                                                    5.33118
                    41/120
                                                  3/15
                                                                               6/15
                                                                                      0.40000
13
                    41/120
          1.95440
                             0.34167
                                        5,47921
                                                  3/15
                                                         0.20000
                                                                     5.37092
                                                                               6/15
                                                                                      0.40000
15
          1.94524
                    46/120
                             0.38333
                                        5.52044
                                                  4/15
                                                         0.26667
                                                                    5.41565
                                                                               6/15
                                                                                      0.40000
16
          1.93175
                    53/120
                             0.44167
                                        5.57135
                                                  4/15
                                                         0.26667
                                                                    5.45809
                                                                               7/15
                                                                                      0.46667
                                                                    5.50149
                             0.35833
                                        5.61072
17
          1.91014
                    43/120
                                                  3/15
                                                         0.20000
                                                                               6/15
                                                                                      0.40000
                    69/120
                             0.57500
                                                                    5.54952
          1.90711
                                        5.67002
                                                  8/15
                                                         0.53333
                                                                               9/15
                                                                                      0.60000
18
                    42/120
                                                                     5.58896
          1.88597
                             0.35000
                                        5.72235
                                                  3/15
                                                         0.20000
                                                                               6/15
20
          1.87904
                    48/120
                             0.40000
                                        5.77352
                                                  4/15
                                                         0.26667
                                                                     5.63485
                                                                               6/15
                                                                                      0.40000
21
          1.86707
                    42/120
                             0.35000
                                        5.82632
                                                  3/15
                                                         0.20000
                                                                    5.68549
                                                                              6/15
                                                                                      0.40000
22
          1.85894
                    55/120
                             0.45833
                                        5.86293
                                                  6/15 I
                                                         0.40000
                                                                    5.73654
                                                                              7/15
                                                                                      0.46667
23
          1.85129
                    52/120
                             0.43333
                                        5.91903
                                                  4/15
                                                         0.26667
                                                                    5.78466
                                                                              6/15
                                                                                      0.40000
          1.84432
                    59/120
                             0.49167
                                        5.96920
                                                  6/15 |
                                                         0.40000 || 5.82976 | 7/15 | 0.46667
25
          1.83885
                    73/120
                             0.60833
                                        6.01675
                                                  10/15 | 0.66667 || 5.87544 | 9/15 | 0.60000
          1.83200
                    59/120
                             0.49167
                                        6.07935
                                                  6/15 |
                                                         0.40000 || 5.92454 | 7/15 | 0.46667
                    71/120 | 0.59167 || 6.12763 | 10/15 | 0.66667 || 5.97439 | 9/15 | 0.60000
          1.82678 I
Validation cost increased after 65 percent of epochs were executed -- Early stopping criteria
```

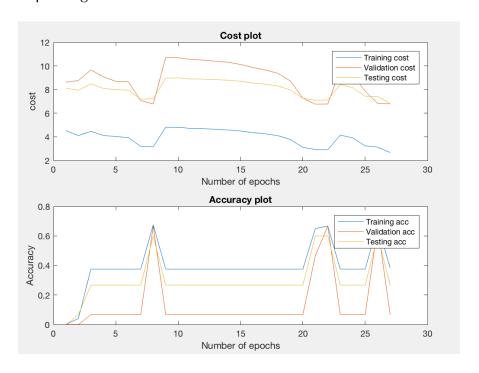


>> BackPropProj2(irisinputs, iristargets, [4,20,3], 40, 10, 0.1, [80, 10, 10], 0.3, 5, 'relu', 'cross');

Epoch	Cost Co	rr Acc Cost Corr Acc Cost Corr Acc
User Inp	 ut required	d: Relu can only be used in the hidden layers
'softmax		,
1	3.97748	36/120 0.30000 19.59380 5/15 0.33333 19.23157 9/15 0.60000
2	4.05704	0/120 0.00000 19.80446 0/15 0.00000 19.81179 0/15 0.00000
3	4.21095	0/120 0.00000 20.27497 0/15 0.00000 20.46830 0/15 0.00000
4	4.19479	0/120 0.00000 20.24968 0/15 0.00000 20.33307 0/15 0.00000
5	4.19726	0/120 0.00000 20.22632 0/15 0.00000 20.32323 0/15 0.00000
6	4.19409	0/120 0.00000 20.24107 0/15 0.00000 20.32674 0/15 0.00000
7	4.19409	0/120 0.00000 20.24560 0/15 0.00000 20.31184 0/15 0.00000
8	4.19378	0/120 0.00000 20.22972 0/15 0.00000 20.29302 0/15 0.00000
9	4.20044	0/120 0.00000 20.25707 0/15 0.00000 20.40078 0/15 0.00000
10	4.19369	0/120 0.00000 20.23516 0/15 0.00000 20.28031 0/15 0.00000
11	4.19354	0/120 0.00000 20.23836 0/15 0.00000 20.29437 0/15 0.00000
12	4.19457	0/120 0.00000 20.23776 0/15 0.00000 20.26777 0/15 0.00000
13	4.19641	0/120 0.00000 20.23177 0/15 0.00000 20.33494 0/15 0.00000
14	4.19421	0/120 0.00000 20.22775 0/15 0.00000 20.26610 0/15 0.00000
15	4.19951	0/120 0.00000 20.21314 0/15 0.00000 20.26158 0/15 0.00000
16	4.19676	0/120 0.00000 20.21867 0/15 0.00000 20.24369 0/15 0.00000
17	4.19714	0/120 0.00000 20.21680 0/15 0.00000 20.25075 0/15 0.00000
18	4.19547	0/120 0.00000 20.22112 0/15 0.00000 20.25942 0/15 0.00000
19	4.19715	0/120 0.00000 20.25644 0/15 0.00000 20.29465 0/15 0.00000
20	4.19452	0/120 0.00000 20.22592 0/15 0.00000 20.29224 0/15 0.00000
21	4.19534	0/120 0.00000 20.22123 0/15 0.00000 20.26892 0/15 0.00000
22	4.19711	0/120 0.00000 20.26100 0/15 0.00000 20.32753 0/15 0.00000
23	4.19501	0/120 0.00000 20.22242 0/15 0.00000 20.26655 0/15 0.00000
24	4.19739	0/120 0.00000 20.26026 0/15 0.00000 20.31211 0/15 0.00000
25	4.19735	0/120 0.00000 20.25200 0/15 0.00000 20.37346 0/15 0.00000
26	4.19419	0/120 0.00000 20.24369 0/15 0.00000 20.32868 0/15 0.00000
27	4.19661	0/120 0.00000 20.21824 0/15 0.00000 20.27149 0/15 0.00000
Validati	on cost in	creased after 65 percent of epochs were executed Early stopping criteria





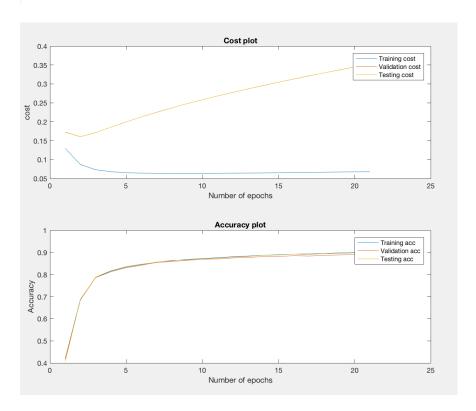


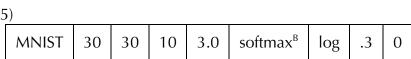
4	4)											
	MNIST	30	30	10	3.0	sigmoid	quad	.3	5			

>> load('mnistTrn.mat');

>> BackPropProj2(trn, trnAns, [784,30,10], 30, 10, 3, [80, 10, 10], 0.3, 5, 'sigmoid', 'quad');

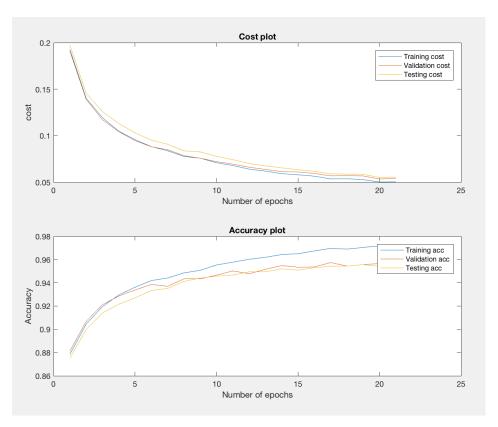
Epoch	Cost Coi	r Acc Cost Corr Acc Cost Corr Acc	
1	0.12969	16743/40000 0.41857 0.17232 2079/5000 0.41580 0.17267 2032/5000	0.40640
2	0.08688	27522/40000 0.68805 0.16046 3423/5000 0.68460 0.16063 3433/5000 0	0.68660
3	0.07307	31454/40000 0.78635 0.17116 3930/5000 0.78600 0.17126 3939/5000 0	0.78780
4	0.06778	32602/40000 0.81505 0.18554 4061/5000 0.81220 0.18558 4087/5000 0	0.81740
5	0.06527	33344/40000 0.83360 0.19944 4153/5000 0.83060 0.19955 4180/5000 0	0.83600
6	0.06414	33786/40000 0.84465 0.21275 4208/5000 0.84160 0.21276 4232/5000 0	0.84640
7	0.06346	34245/40000 0.85613 0.22481 4272/5000 0.85440 0.22503 4278/5000 0	0.85560
8	0.06326	34475/40000 0.86187 0.23648 4292/5000 0.85840 0.23653 4319/5000 0	0.86380
9	0.06339	34721/40000 0.86803 0.24779 4320/5000 0.86400 0.24774 4328/5000 0	0.86560
10	0.06335	34875/40000 0.87187 0.25797 4345/5000 0.86900 0.25793 4349/5000 0	0.86980
11	0.06366	35029/40000 0.87572 0.26806 4350/5000 0.87000 0.26814 4368/5000 0	0.87360
12	0.06400	35212/40000 0.88030 0.27754 4373/5000 0.87460 0.27767 4393/5000 0	0.87860
13	0.06425	35337/40000 0.88343 0.28677 4387/5000 0.87740 0.28686 4408/5000 0	0.88160
14	0.06467	35471/40000 0.88677 0.29563 4402/5000 0.88040 0.29581 4432/5000 0	0.88640
15	0.06511	35573/40000 0.88933 0.30447 4408/5000 0.88160 0.30454 4440/5000 0	0.88800
16	0.06554	35666/40000 0.89165 0.31279 4424/5000 0.88480 0.31293 4458/5000 0	0.89160
17	0.06610	35723/40000 0.89307 0.32114 4417/5000 0.88340 0.32137 4452/5000 0	0.89040
18	0.06652	35799/40000 0.89497 0.32925 4431/5000 0.88620 0.32925 4471/5000 0	0.89420
19	0.06701	35899/40000 0.89748 0.33697 4442/5000 0.88840 0.33718 4473/5000 0	0.89460
20	0.06756	35978/40000 0.89945 0.34470 4452/5000 0.89040 0.34487 4486/5000 0	0.89720
21	0.06804	36067/40000 0.90168 0.35223 4461/5000 0.89220 0.35239 4498/5000	0.89960

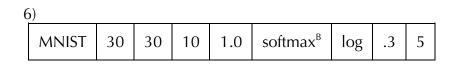




BackPropProj2(trn, trnAns, [784,30,10], 30, 10, 3, [80, 10, 10], 0.3, 0, 'softmax', 'log');

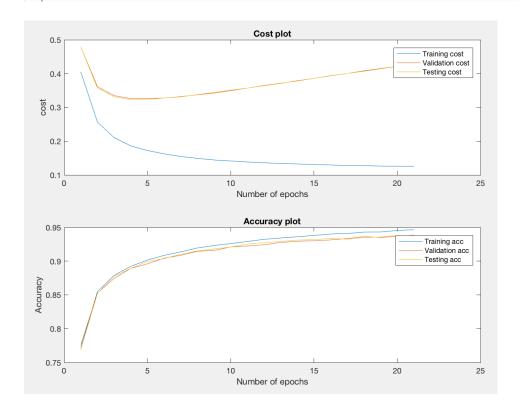
>> BackP	ropProj2(trn, trnAns, [784,30,10], 30, 10, 3, [80, 10, 10], 0.3, 0, 'softmax', 'log'); TRAIN VALIDATION TEST
Epoch	Cost Corr Acc Cost Corr Acc Cost Corr Acc
User Inp	ut required: Softmax function can only be used in the last layer
1	0.19255 35140/40000 0.87850 0.19104 4406/5000 0.88120 0.19743 4376/5000 0.87520
2	0.14023 36179/40000 0.90448 0.13910 4534/5000 0.90680 0.14566 4499/5000 0.89980
3	0.11933 36782/40000 0.91955 0.11713 4606/5000 0.92120 0.12591 4570/5000 0.91400
4	0.10480 37179/40000 0.92948 0.10449 4643/5000 0.92860 0.11314 4608/5000 0.92160
5	0.09576 37448/40000 0.93620 0.09460 4669/5000 0.93380 0.10303 4635/5000 0.92700
6	0.08826 37676/40000 0.94190 0.08816 4693/5000 0.93860 0.09536 4667/5000 0.93340
7	0.08380 37766/40000 0.94415 0.08492 4685/5000 0.93700 0.09076 4676/5000 0.93520
8	0.07771 37941/40000 0.94852 0.07855 4717/5000 0.94340 0.08376 4706/5000 0.94120
9	0.07582 38029/40000 0.95073 0.07579 4717/5000 0.94340 0.08260 4720/5000 0.94400
10	0.07092 38213/40000 0.95532 0.07212 4733/5000 0.94660 0.07777 4729/5000 0.94580
11	0.06796 38310/40000 0.95775 0.06946 4751/5000 0.95020 0.07426 4733/5000 0.94660
12	0.06409 38409/40000 0.96022 0.06619 4739/5000 0.94780 0.07012 4747/5000 0.94940
13	0.06190 38477/40000 0.96193 0.06368 4758/5000 0.95160 0.06751 4747/5000 0.94940
14	0.05923 38572/40000 0.96430 0.06146 4774/5000 0.95480 0.06543 4760/5000 0.95200
15	0.05797 38599/40000 0.96498 0.06100 4767/5000 0.95340 0.06344 4754/5000 0.95080
16	0.05650 38695/40000 0.96737 0.05947 4768/5000 0.95360 0.06169 4765/5000 0.95300
17	0.05360 38783/40000 0.96957 0.05682 4787/5000 0.95740 0.05898 4771/5000 0.95420
18	0.05372 38758/40000 0.96895 0.05695 4772/5000 0.95440 0.05869 4772/5000 0.95440
19	0.05272 38816/40000 0.97040 0.05676 4778/5000 0.95560 0.05850 4778/5000 0.95560
20	0.05023 38873/40000 0.97183 0.05348 4783/5000 0.95660 0.05511 4771/5000 0.95420
21	0.05047 38847/40000 0.97118 0.05438 4780/5000 0.95600 0.05545 4773/5000 0.95460
Validati	on cost increased after 65 percent of epochs were executed Early stopping criteria
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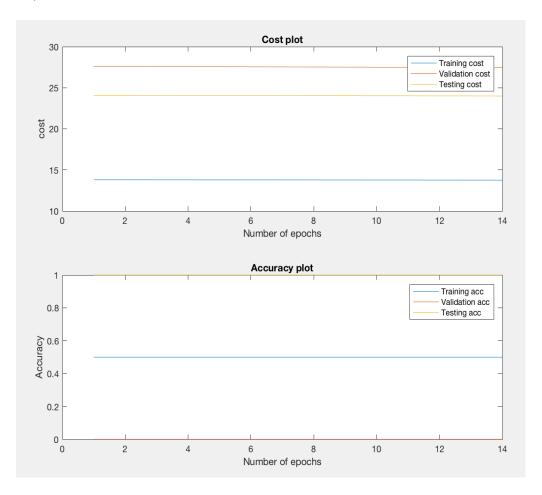
>> BackPropProj2(trn, trnAns, [784,30,10], 30, 10, 1, [80, 10, 10], 0.3, 5, 'softmax', 'log'); | >> BackPropProj2(trn, trnAns, [784,30,10], 30, 10, 1, [80, 10, 10], 0.3, 5, 'softmax', 'log'); | TRAIN | TRAI

1	TRAIN	П	VALIDATION	П	TEST	
Epoch	Cost Cor	r Acc	Cost Corr A	cc Cost	Corr Acc	_
User Inpu	ut required	: Softmax fun	ction can only be u	sed in the la	ast layer	
'sigmoid	•					
1	0.40457	30876/40000	0.77190 0.4788	4 3882/5000	0 0.77640 0.47858 3	844/5000 0.76880
2	0.25635	34199/40000	0.85498 0.3611	9 4264/5000	0 0.85280 0.35762 4	262/5000 0.85240
3	0.21063	35156/40000	0.87890 0.3348	7 4372/5000	0 0.87440 0.33160 4	388/5000 0.87760
4	0.18602	35694/40000	0.89235 0.3258	2 4446/5000	0 0.88920 0.32289 4	446/5000 0.88920
5	0.17226	36063/40000	0.90158 0.3262	0 4480/5000	0 0.89600 0.32361 4	497/5000 0.89940
6	0.16257	36342/40000	0.90855 0.3275	9 4522/5000	0 0.90440 0.32761 4	519/5000 0.90380
7	0.15443	36550/40000	0.91375 0.3318	5 4543/5000	0 0.90860 0.33115 4	551/5000 0.91020
8	0.14912	36779/40000	0.91948 0.3372	4 4573/5000	0 0.91460 0.33772 4	575/5000 0.91500
9	0.14430	36926/40000	0.92315 0.3423	6 4579/5000	0 0.91580 0.34424 4	590/5000 0.91800
10	0.14135	37036/40000	0.92590 0.3496	1 4605/5000	0 0.92100 0.35088 4	604/5000 0.92080
11	0.13837	37165/40000	0.92912 0.3569	9 4612/5000	0 0.92240 0.35708 4	626/5000 0.92520
12	0.13613	37290/40000	0.93225 0.3648	9 4621/5000	0 0.92420 0.36421 4	637/5000 0.92740
13	0.13376	37369/40000	0.93422 0.3715	1 4638/5000	0 0.92760 0.37092 4	645/5000 0.92900
14	0.13259	37444/40000	0.93610 0.3783	1 4647/5000	0 0.92940 0.37916 4	656/5000 0.93120
15	0.13085	37520/40000	0.93800 0.3858	9 4651/5000	0 0.93020 0.38586 4	659/5000 0.93180
16	0.12940	37604/40000	0.94010 0.3935	9 4657/5000	0 0.93140 0.39315 4	668/5000 0.93360
17	0.12798	37635/40000	0.94088 0.4004	1 4667/5000	0 0.93340 0.40036 4	662/5000 0.93240
18	0.12757	37720/40000	0.94300 0.4073	9 4681/5000	0 0.93620 0.40858 4	675/5000 0.93500
19	0.12637	37724/40000	0.94310 0.4143	3 4675/5000	0 0.93500 0.41518 4	678/5000 0.93560
20	0.12572	37814/40000	0.94535 0.4218	0 4684/5000	0 0.93680 0.42189 4	690/5000 0.93800
21	0.12532	37859/40000	0.94647 0.4290	6 4693/5000	0 0.93860 0.42955 4	683/5000 0.93660
Validatio	on cost inc	reased after	65 percent of epoch	s were execut	ted Early stopping crit	eria
>>						



7	·)								
	xor.csv	20	[3 2]	1	0.1	sigmoid	cross	.3	5

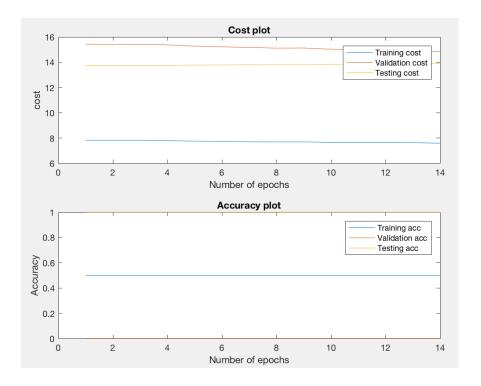
Epoch	Cost Corr Acc Cost Corr Acc Cost Corr Acc
1	13.81300 1/2 0.50000 27.59776 0/1 0.00000 24.08835 1/1 1.00000
2	13.81476 1/2 0.50000 27.60130 0/1 0.00000 24.09082 1/1 1.00000
3	13.80612 1/2 0.50000 27.58397 0/1 0.00000 24.07882 1/1 1.00000
4	13.80050 1/2 0.50000 27.57269 0/1 0.00000 24.07102 1/1 1.00000
5	13.79514 1/2 0.50000 27.56194 0/1 0.00000 24.06359 1/1 1.00000
6	13.78979 1/2 0.50000 27.55122 0/1 0.00000 24.05619 1/1 1.00000
7	13.78445 1/2 0.50000 27.54050 0/1 0.00000 24.04879 1/1 1.00000
8	13.77910 1/2 0.50000 27.52977 0/1 0.00000 24.04139 1/1 1.00000
9	13.77374 1/2 0.50000 27.51903 0/1 0.00000 24.03399 1/1 1.00000
10	13.76838 1/2 0.50000 27.50827 0/1 0.00000 24.02658 1/1 1.00000
11	13.76701 1/2 0.50000 27.50552 0/1 0.00000 24.02470 1/1 1.00000
12	13.75800 1/2 0.50000 27.48746 0/1 0.00000 24.01226 1/1 1.00000
13	13.75631 1/2 0.50000 27.48406 0/1 0.00000 24.00993 1/1 1.00000
14	13.74725 1/2 0.50000 27.46589 0/1 0.00000 23.99743 1/1 1.00000
Valida >>	tion cost increased after 65 percent of epochs were executed Early stopping criter



xor.csv	20	[3 2]	1	0.1	tanh ^C	cross	.3	5
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>> BackPropProj2(inputs, targets, [2,3,2,1], 20, 1, 0.1, [60,20,20], 0.3, 5, 'tanh', 'cross');

>> BackP	ropProj2(inputs, TRAIN	targets, [2,3,2,1], 20, 1, 0.1, [60,20,20], 0.3, 5, 'tanh', 'cross'); VALIDATION TEST
Epoch	Cost Corr	Acc Cost Corr Acc Cost Corr Acc
1	7.82170 1/2	0.50000 15.43216 0/1 0.00000 13.75276 1/1 1.00000
2	7.81459 1/2	i ii i i i ii ii
3	7.81575 1/2	0.50000 15.42009 0/1 0.00000 13.75182 1/1 1.00000
4	7.79522 1/2	0.50000 15.37387 0/1 0.00000 13.75493 1/1 1.00000
5	7.75158 1/2	0.50000 15.27220 0/1 0.00000 13.76783 1/1 1.00000
6	7.72844 1/2	0.50000 15.21718 0/1 0.00000 13.77726 1/1 1.00000
7	7.70747 1/2	0.50000 15.16622 0/1 0.00000 13.78804 1/1 1.00000
8	7.68735 1/2	0.50000 15.11608 0/1 0.00000 13.80085 1/1 1.00000
9	7.69001 1/2	0.50000 15.12476 0/1 0.00000 13.79604 1/1 1.00000
10	7.65225 1/2	0.50000 15.02488 0/1 0.00000 13.83045 1/1 1.00000
11	7.63360 1/2	0.50000 14.97326 0/1 0.00000 13.85187 1/1 1.00000
12	7.63747 1/2	0.50000 14.98740 0/1 0.00000 13.84192 1/1 1.00000
13	7.62316 1/2	0.50000 14.94718 0/1 0.00000 13.85964 1/1 1.00000
14	7.59188 1/2	0.50000 14.84593 0/1 0.00000 13.92126 1/1 1.00000
Validati	on cost increase	d after 65 percent of epochs were executed Early stopping criteria



9)								
xor.csv	20	[3 2]	1	0.1	relu	cross	.3	5

>> BackPropProj2(inputs, targets, [2,3,2,1], 20, 1, 0.1, [60,20,20], 0.3, 5, 'relu', 'cross');

```
>> BackPropProj2(inputs, targets, [2,3,2,1], 20, 1, 0.1, [60,20,20], 0.3, 5, 'relu', 'cross');
         TRAIN
                                 VALIDATION
                                                                 TEST
                         | |
                                                     | |
      | Cost | Corr | Acc || Cost | Corr |
                                                 Acc || Cost | Corr | Acc
User Input required: Relu can only be used in the hidden layers
'sigmoid'
1
         4.57945 | 1/2 | 0.50000 || 8.77021 | 0/1 | 0.00000 || 8.08206 | 1/1 | 1.00000
          4.57962 | 1/2 |
                          0.50000 || 8.77586
                                                                         1/1 | 1.00000
2
                                              0/1 |
                                                     0.00000 || 8.07870 |
3
          4.58055
                   1/2
                          0.50000
                                  || 8.80087
                                               0/1
                                                     0.00000 || 8.05394
                                                                         1/1
                                                                                1.00000
4
          4.58181
                  1 1/2
                         0.50000 || 8.76216
                                              0/1
                                                     0.00000 || 8.11543 | 1/1
                                                                               1.00000
5
                          0.50000 ||
                                                     0.00000 || 8.14227
                                                                               1.00000
          4.58407
                   1/2
                                     8.75237
                                               0/1
                                                                         1/1
6
          4.58657
                   1/2
                          0.50000
                                     8.74636
                                               0/1
                                                     0.00000
                                                             || 8.16520
                                                                         1/1
7
          4.58940
                   1/2
                          0.50000 || 8.74176
                                               0/1
                                                     0.00000 || 8.18758
                                                                         1/1
                                                                               1.00000
8
          4.59253
                          0.50000 ||
                                                     0.00000 || 8.20975
                   1/2
                                    8.73827
                                               0/1
                                                                          1/1
                                                                                1.00000
9
          4.58913
                   1/2
                          0.50000
                                     8.76038
                                               0/1
                                                     0.00000
                                                             || 8.17422
                                                                          1/1
10
          4.59842
                   1/2
                          0.50000
                                     8.73568
                                               0/1
                                                     0.00000 || 8.24706
                                                                         1/1
                                                                                1.00000
          4.60308
                          0.50000 || 8.73292
                                                     0.00000 || 8.27416
11
                   1/2 |
                                               0/1
                                                                         1/1
                                                                               1.00000
12
          4.59746 | 1/2
                          0.50000
                                  || 8.75373
                                               0/1
                                                     0.00000 || 8.23289
                                                                         1/1
                                                                               1.00000
13
          4.60987 | 1/2 | 0.50000 || 8.73477
                                              0/1
                                                   0.00000 | 8.30977 | 1/1 | 1.00000
         4.61522 | 1/2 | 0.50000 || 8.73460 | 0/1 | 0.00000 || 8.33637 | 1/1 | 1.00000
Validation cost increased after 65 percent of epochs were executed -- Early stopping criteria
```

