Exponentiation and logarithms

- 1. Warm-up: Sketch a graph of $y = 2^x$ as well as $y = 2^{-x}$ What is the relationship between the 2 curves?
- 2. Solve the following exponential equations. You only have to provide the real number answers

a.
$$x^{3/2} = 8$$

b.
$$z^4 = 1$$

c.
$$2^k = 1024$$

- 3. Logarithms are the inverse of exponentiation, sketch a graph of $y = \log_2 x$ on the same graph as q1, what is the relationship between $y = \log_2 x$ and $y = 2^x$?
- 4. Now let's apply logarithms to solve some equations

a.
$$3^x + 10 = 739$$

b.
$$49^x - 5 \cdot 7^x + 6 = 0$$

c.
$$\frac{e^x + e^{-x}}{2} = 8$$

5. Using logarithmic properties, solve the following equations

a.
$$\log_3(x+5) + 1 = \log_3(x^2 - 3)$$

b.
$$\log_y 10 = \log_{10} y + 1$$
 (calculate y to 3 s.f.)

6. The rate of a chemical reaction (k) is found to obey the following relationship:

$$k = Ae^{-\frac{g}{RT}}$$

Where A is a constant, T is the temperature, and R is the universal gas constant. (take $R \approx 8.31$). A scientist found that the rate doubled when T increased from 298K to 323K (K is Kelvin; a unit of temperature)

Using this information, find the value of g.