

Minimize:

$$\sum_{w \in W(\tau)} \sum_{p \in P(\tau)} \textit{strategic_value}_{wp}(\tau) \cdot \alpha_{wp}(\tau) \quad (1)$$

$$+ \sum_{p \in P(\tau)} \sum_{r \in R(\tau)} \textit{strategic_penalty} \cdot \epsilon_{pr}(\tau) \quad (2)$$

$$- \sum_{p \in P(\tau)} \sum_{w1 \in W(\tau)} \sum_{w2 \in W(\tau)} \textit{clustering_value}_{w1,w2} \cdot \alpha_{w1p}(\tau) \cdot \alpha_{w2p}(\tau) \quad (3)$$

Subject to:

$$\begin{aligned} \sum_{w \in W(\tau)} \textit{work_order_work}_{wr} \cdot \alpha_{wp}(\tau) \\ \leq \textit{resource}_{pr}(\tau) + \epsilon_{pr}(\tau) \\ \forall p \in P(\tau) \quad \forall r \in R(\tau) \end{aligned} \quad (4)$$

$$\begin{aligned} \sum_{w \in W(\tau)} \alpha_{wp}(\tau) = 1 \\ \forall p \in P(\tau) \end{aligned} \quad (5)$$

$$\begin{aligned} \alpha_{wp}(\tau) = 0 \\ \forall (w, p) \in \textit{exclude}(\tau) \end{aligned} \quad (6)$$

$$\begin{aligned} \alpha_{wp}(\tau) = 1 \\ \forall (w, p) \in \textit{include}(\tau) \end{aligned} \quad (7)$$

$$\begin{aligned} \alpha_{wp}(\tau) \in \{0, 1\} \\ \forall w \in W(\tau) \quad \forall p \in P(\tau) \end{aligned} \quad (8)$$

$$\begin{aligned} \epsilon_{pr}(\tau) \in \mathbb{R}^+ \\ \forall p \in P(\tau) \quad \forall r \in R(\tau) \end{aligned} \quad (9)$$

$$\tau \in [0, \infty] \quad (10)$$

The objective function (1), (2), and (3) minimizes the total weighted delay of all work order assignments together with the penalty *strategic_penalty* for exceeding the resource capacity given in constraint (4). The third term of the model contains the *clustering_value_{w1,w2}* which turns the model into a quadratic problem. This term optimizes the value of putting two work orders