Smart Contracts

Plutus & Marlowe

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Introduction

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- Although both have been created to add smart-contract capabilities to Cardano, they could in principle be used on other blockchains as well.
- Both are written in Haskell.
- Plutus is Turing-complete and general, Marlowe is a *non*-Turing-complete DSL for financial contracts.

Functional Programming and the UTxO-Model

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- This is similar to the relationship between imperative programming languages (like Java and Python) and functional languages (like Haskell).
- This makes it a good fit to write smart contracts for an account-based blockchain like Ethereum in an imperative language like Solidity and contracts for the UTxO-based Cardano in the functional language Haskell.

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- Taken together, these properties make it possible to write smart contracts in Plutus which are as least as powerful as Ethereum smart contracts.

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- Not only has Plutus been implemented in Haskell, you also program in Haskell, which means that Haskell is for Plutus Core what Solidity is for the EVM.
- This enables a seamless interplay between onchain code and offchain code (whereas Solidity only supports onchain code, so that offchain code has to be written in something like JavaScript.)

Lambda Calculus

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- Haskell is based upon and compiles to a (typed!) version of the lambda Calculus (as first intermediate compiler target, Core).

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- Fixed by Church in 1936 – Untyped Lambda Calculus.
- Relation to programming languages clarified in the 1960s.

Lambda expressions

Lambda expressions (or lambda terms) are composed of

- variables $v_1, v_2, \dots, v_n, \dots,$
- the abstraction symbols λ and $.\,,$
- parentheses $(\,)$.

The set of lambda expressions Λ is inductively defined as:

- If x is a variable, then $x \in \Lambda$. (variable)
- If x is a variable and $M \in \Lambda$, then $(\lambda x.M) \in \Lambda$. (lambda abstraction)
- If $M, N \in \Lambda$, then $(MN) \in \Lambda$. (application)

Free variables

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- In an abstraction $\lambda x.M$, we call the variable x bound.

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- This act of "plugging in" an expression for the bound variable in an abstraction is what constitutes the idea of computation in lambda Calculus.

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- and many more...

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- System F_ω adds functions from types to types (type constructors) to System F.

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- Marlowe is *not* Turing-complete, and it is simple enough to allow for static analysis, which can automatically derive and prove important properties of Marlowe contracts.
- Marlowe is also powerful enough to implement a significant part of all commonly used financial contracts.

Predictable Runtime

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- Marlowe guarantees that no money will be "trapped" in a contract forever: By the end of the contract, all money that has been paid into the contract will have been paid back to one of the parties participating in the contract.

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- An EDSL has the advantage that all features of the host language are available to help facilitate creating expressions in the DSL.
- This means for Marlowe, that we can use Haskell to write Marlowe contracts and that Marlowe contracts are nothing more than values of a specific Haskell type.

Blockly

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- This is tedious for complex contracts, but a good way for beginners.

JavaScript

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- This will hopefully make Marlowe more accessible for non-Haskellers.

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- Using this method makes It possible to classify and describe the majority of all financial instruments in about 30 types and patterns.
- IOHK plans to use Plutus and Marlowe to implement the complete Actus Standard in Cardano.