

Smart Contracts

Plutus & Marlowe

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- Both are written in **Haskell**.
- Plutus is Turing-complete and general, Marlowe is a *non*-Turing-complete **DSL for financial contracts**.



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- This is similar to the relationship between **imperative** programming languages (like Java and Python) and **functional** languages (like Haskell).
- This makes it a good fit to write smart contracts for an account-based blockchain like Ethereum in an imperative language like Solidity and contracts for the UTxO-based Cardano in the functional language Haskell.

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- Taken together, these properties make it possible to write smart contracts in Plutus which are at least as powerful as Ethereum smart contracts.



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- Not only has Plutus been implemented in Haskell, you also program in Haskell, which means that Haskell is for Plutus Core what Solidity is for the EVM.
- This enables a seamless interplay between onchain code and offchain code (whereas Solidity only supports onchain code, so that offchain code has to be written in something like JavaScript.)



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- Turing complete.
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- **Haskell** is based upon and compiles to a (typed!) version of the lambda Calculus (as first intermediate compiler target, **Core**).

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- Fixed by Church in 1936 – Untyped Lambda Calculus.
- Relation to programming languages clarified in the 1960s.

Lambda expressions

Lambda expressions (or lambda terms) are composed of

- variables $v_1, v_2, \dots, v_n, \dots$,
- the abstraction symbols λ and $.$,
- parentheses $()$.

The set of lambda expressions Λ is inductively defined as:

- If x is a variable, then $x \in \Lambda$. (variable)
- If x is a variable and $M \in \Lambda$, then $(\lambda x.M) \in \Lambda$. (lambda abstraction)
- If $M, N \in \Lambda$, then $(MN) \in \Lambda$. (application)

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- In an abstraction $\lambda x.M$, we call the variable x **bound**.

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- This act of “plugging in” an expression for the bound variable in an abstraction is what constitutes the idea of computation in lambda Calculus.

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- and many more...

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- **System F_ω** adds functions from types to types (**type constructors**) to System F.

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- Marlowe is also powerful enough to implement a significant part of all commonly used financial contracts.



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- Marlowe guarantees that no money will be “trapped” in a contract forever: By the end of the contract, all money that has been paid into the contract will have been paid back to one of the parties participating in the contract.



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- Marlowe’s host language is **Haskell**.
- An EDSL has the advantage that all features of the host language are available to help facilitate creating expressions in the DSL.
- This means for Marlowe, that we can use Haskell to write Marlowe contracts and that Marlowe contracts are nothing more than values of a specific Haskell type.



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- This is tedious for complex contracts, but a good way for beginners.



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- Using this method makes it possible to classify and describe the majority of all financial instruments in about 30 types and patterns.
- IOHK plans to use Plutus and Marlowe to implement the complete Actus Standard in Cardano.