

Respuestas Trabajo Práctico 2: Números complejos

1.

Z	-z	$ar{z}$	$z^{-1} = \frac{1}{z}$
z = 2 + i	-2 - i	2-i	$\frac{2}{5} - \frac{1}{5}i$
z = -1 + 3i	1 - 3i	-1 - 3i	$-\frac{1}{10} - \frac{3}{10}i$
z = -i	i	i	i
z = -3 + 4i	3 - 4i	-3 - 4i	$-\frac{3}{25} - \frac{4}{25}i$

2.

a.
$$z.w = 2 - 2i$$

b.
$$\bar{v} - w1 + (1 + \sqrt{3})i$$

c.
$$(2w - \bar{z}).(i - v) = 2 - (2 - 2\sqrt{3})i$$

d.
$$2(-z + 3v) = 2 + (-4 + 6\sqrt{3})i$$

3.

b. La longitud de cada diagonal es 2 y $\sqrt{20}$.

6.

•
$$z = 2 + 2i$$
,

$$|z| = \sqrt{8}$$
, $\arg(z) = \frac{\pi}{4}$

Forma trigonométrica $z = \sqrt{8} \cdot \left[\cos\left(\frac{\pi}{4}\right) + i \cdot \sin\left(\frac{\pi}{4}\right)\right]$

Forma exponencial $z = \sqrt{8}$. $e^{\frac{\pi}{4}i}$

•
$$v = 1 - \sqrt{3}i$$
,

$$|v| = 2, \qquad \arg(v) = \frac{5\pi}{3},$$

Forma trigonométrica $v = 2. \left[\cos \left(\frac{5\pi}{3} \right) + i. \operatorname{sen} \left(\frac{5\pi}{3} \right) \right]$

Forma exponencial v = 2. $e^{\frac{5\pi}{3}i}$

•
$$w = -i$$

$$|w| = 1, \qquad \arg(w) = \frac{3\pi}{2},$$

Forma trigonométrica $w=1.\left[\cos\left(\frac{3\pi}{2}\right)+i.\sin\left(\frac{3\pi}{2}\right)\right]$

Forma exponencial w = 1. $e^{\frac{3\pi}{2}i}$

7.

a.
$$a = -1$$

b. $arg(z) = \frac{4}{3}\pi$, el ángulo del primer cuadrante que se utiliza para realizar el pasaje es $\alpha = \frac{\pi}{3}$.

8.

a. Centro (0,0) y radio $\sqrt[n]{|z|}$. La ecuación $w^n=z$ tiene n soluciones complejas



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a.
$$S = \{1, 2\}$$

b.
$$S = \left\{ \sqrt[3]{2}e^{\frac{\pi}{2}i}, \sqrt[3]{2}e^{\frac{7\pi}{6}i}, \sqrt[3]{2}e^{\frac{11\pi}{6}i} \right\}$$

c. $S = \left\{ -2, 2, 1 + 2i, 1 - 2i \right\}$
d. $S = \left\{ 2e^{\frac{\pi}{3}i}, 2e^{\pi i}, 2e^{\frac{5\pi}{3}i} \right\}$

c.
$$S = \{-2, 2, 1 + 2i, 1 - 2i\}$$

d.
$$S = \left\{ 2e^{\frac{\pi}{3}i}, 2e^{\pi i}, 2e^{\frac{5\pi}{3}i} \right\}$$

e.
$$S = \begin{cases} \sqrt[4]{2}e^{\frac{5\pi}{12}i}, \sqrt[4]{2}e^{\frac{11\pi}{12}i}, \sqrt[4]{2}e^{\frac{17\pi}{12}i}, \sqrt[4]{2}e^{\frac{23\pi}{12}i} \end{cases}$$

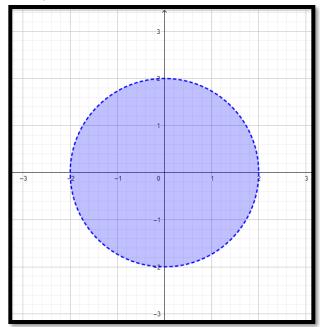
e.
$$S = \left\{ \sqrt[4]{2}e^{\frac{5\pi}{12}i}, \sqrt[4]{2}e^{\frac{11\pi}{12}i}, \sqrt[4]{2}e^{\frac{17\pi}{12}i}, \sqrt[4]{2}e^{\frac{23\pi}{12}i} \right\}$$

f. $S = \left\{ \sqrt[6]{2}e^{\frac{\pi}{24}i}, \sqrt[6]{2}e^{\frac{3\pi}{8}i}, \sqrt[6]{2}e^{\frac{17\pi}{24}i}, \sqrt[6]{2}e^{\frac{25\pi}{24}i}, \sqrt[6]{2}e^{\frac{33\pi}{24}i}, \sqrt[6]{2}e^{\frac{41\pi}{24}i} \right\}$

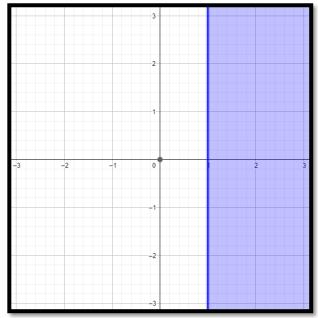
g.
$$S = \{-3, 3, -3i, 3i\}$$

10.

a.
$$R = \{z \in C: |z| < 2\}$$



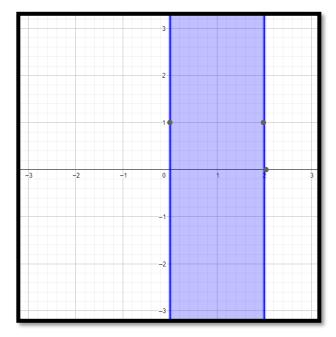
b.
$$R = \{z \in C : Re(z) \ge 1\}$$



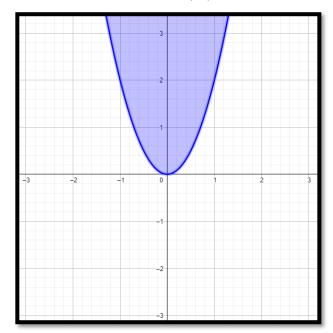


Respuestas Trabajo Práctico 2: Números complejos

c.
$$M = \{z \in C: |z - 1|^2 + Re(z^2) - [Re(z)]^2 \le 1\}$$



d.
$$N = \{z \in C: Re(iz) + |z^2| + Re(z^2) \le 0\}$$



11.

$$\text{a.}\quad \mathsf{R=}\left\{ z\in\mathcal{C} \colon Re(z)\leq3,\ Im(z)\leq2\right\}$$

b.
$$R = \{z \in C : Re(z) \le Im(z), Re(z) \ge 0, Im(z) \le 4\}$$

c.
$$R = \{z \in C: \frac{\pi}{4} \le \arg(z) \le \frac{7}{4}\pi \land |z| \le 2 \}$$