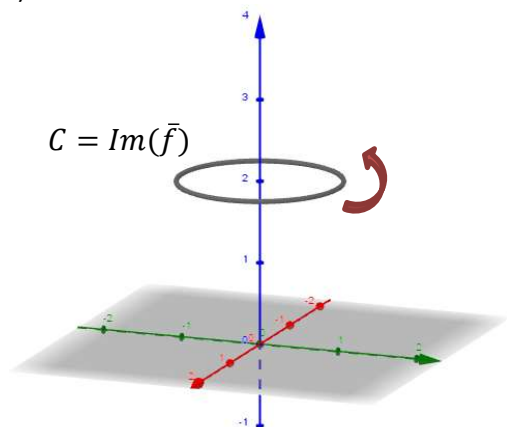


1. a) (0, 9); (9, 0) b) (4, 5) d) A los 2 segundos; nunca e) $y = -x + 9, 0 \leq x \leq 9$

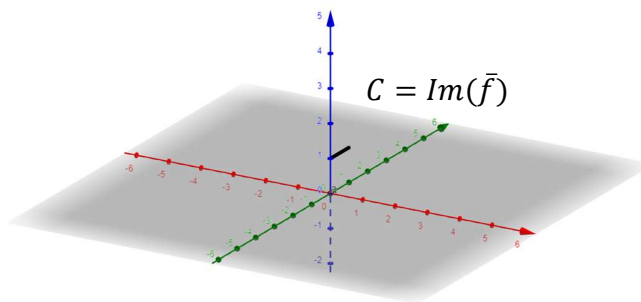
2. 1) $\frac{x^2}{4} + \frac{y^2}{9} = 1, y \geq 0$ 2) $y = x, x \geq 0$ 3) i. $x^2 + y^2 = 9$ ii. $x^2 + y^2 = 9, 0 \leq x \leq 3$

4) $y = -x^2 + 1, x > 0$ 5) $y = (x + 1)^2 + 2, x \geq -1$

8)



9)



3. La función 2) se corresponde con γ_2 ; la curva γ_1 con la función 4); la función 5) se corresponde con γ_3

4. a. $\bar{f}(t) = \begin{cases} (t, 2t) & 0 \leq t \leq 1 \\ (t, 2) & 1 < t \leq 3 \end{cases}$ b. $\bar{f}: \left[-\frac{\pi}{2}; \frac{\pi}{2}\right] \rightarrow \mathbb{R}^2 / \bar{f}(t) = (2 \cos t; 2 \sin t)$

c. $\bar{f}: [0; \pi] \rightarrow \mathbb{R}^2 / \bar{f}(t) = (-3 \cos t; 3 \sin t)$

5. a. $x(t) = \cos(2t), y(t) = \sin(2t)$ con $\frac{\pi}{4} \leq t \leq \frac{9\pi}{4}$

b. $x(t) = \cos t, y(t) = \sin t$ con $0 \leq t \leq \frac{\pi}{2}$

6. a. $\bar{f}(t) = (t; t^2 - 3t) \quad t \in \mathbb{R}$ b. $\bar{f}: \left[\frac{\pi}{2}; \frac{3\pi}{2}\right] \rightarrow \mathbb{R}^2 / \bar{f}(t) = (5 \cos t; 5 \sin t)$ c. $\bar{f}(t) = \left(\frac{1}{3} \cos t; \sin t\right) \quad t \in \mathbb{R}$

d. $\bar{f}: [-1; 1] \rightarrow \mathbb{R}^2 / \bar{f}(t) = (t^2; t)$

e. $\bar{f}: [0; 2\pi] \rightarrow \mathbb{R}^2 / \bar{f}(t) = (\cos(t) - 1; \sin(t))$ f. $\bar{f}: \left[\pi; \frac{3\pi}{2}\right] \rightarrow \mathbb{R}^2 / \bar{f}(t) = (\sqrt{2} \cos(t); \sqrt{3} \sin(t))$

g. $\bar{f}: (-\sqrt{5}; \sqrt{5}) \rightarrow \mathbb{R}^2 / \bar{f}(t) = (t; 2t)$

7. a. $\bar{f}: \mathbb{R} \rightarrow \mathbb{R}^3 / \bar{f}(t) = (\cos t; \sin t; 5)$ b. $\bar{f}: \mathbb{R} \rightarrow \mathbb{R}^3 / \bar{f}(t) = (3\sqrt{2} \cos t; 3\sqrt{2} \sin t; 3\sqrt{2})$

c. $\bar{f}: \mathbb{R} \rightarrow \mathbb{R}^3 / \bar{f}(t) = (t; 0; 1 - t)$ d. $\bar{f}: \mathbb{R} \rightarrow \mathbb{R}^3 / \bar{f}(t) = (t; 4 - t; 4 - t^2)$

e. $\bar{f}: [0; 2] \rightarrow \mathbb{R}^3 / \bar{f}(t) = (t; 4 - t; 4 - t^2)$

- 8.** a. $v(1) = (2; 1)$, $a(1) = (2; 0)$, b. $v(3) = (2; -1)$, $a(3) = (0; 0)$, c. $v(4) = (0; -32; 24)$, $a(4) = (0; -8; 6)$
9. No se encuentran en ningún instante t .

- 10.** Se encuentran en el instante $t = 1$

11.

- a. $(x; y) = (1; 1) + \lambda(1; 2)$, $\lambda \in \mathbb{R}$ b. $(x; y) = (\sqrt{2}; \sqrt{2}) + \lambda(-\sqrt{2}; \sqrt{2})$, $\lambda \in \mathbb{R}$
 c. $(x; y; z) = (r; 4; 0) + \lambda(0; 0; r)$, $\lambda \in \mathbb{R}$ d. $(x; y; z) = (\sqrt{2}; \sqrt{2}; 1) + \lambda(-\sqrt{2}; \sqrt{2}; 0)$, $\lambda \in \mathbb{R}$

a

- 12.** $g: \mathbb{R} \rightarrow \mathbb{R}^2 / g(t) = (-1 + 2\cos t, 3 + 2\sin t)$, $(x, y) = (1, 3) + \alpha(0, 2)$, $\alpha \in \mathbb{R}$

- 13.** a. $\bar{f}(t) = \left(-\frac{1}{t} + 4; -\frac{\cos(2t-2)+1}{2} \right)$, b. $\bar{f}(t) = \left(\frac{1}{2t^4} + \frac{1}{2}; \frac{3}{8}\sqrt[3]{(t^2+7)^4} + 1; t \ln t - t + 1 \right)$

- 14.** Área = 3.76 *aproximadamente*

- 15.** Área = 36.59