

**2.** a. 
$$T(x, y) = (3x - 2y, -x + 4y)$$
 b.  $T(x, y) = \left(-\frac{x + y}{3}, \frac{2x + 2y}{3}\right)$ 

c. No existe una TL que cumpla lo pedido. d. 
$$T(x, y, z) = (8x + 9y + 6z, -5x-9y - 5z)$$
  
e.  $T(x, y, z) = (z, x - z, 0)$ .

**3.** a. 
$$T(x;y) = (-x; y)$$
 b.  $T(x;y) = (-y; -x)$  c.  $T(x;y) = (x + 3y; y)$ 

**4.** a. i. (0, 0) ∈ Nu T ii. (2, 3) ∈ Nu T iii. (3, -2) 
$$\notin$$
 Nu T iv.  $\left(1, \frac{1}{3}\right) \notin$  Nu T b. i. (3, -6) ∈ Im T ii. (2, 3)  $\notin$  Im T iii. (1, -2) ∈ Im T iv. (4, -3)  $\notin$  Im T

**5.** a. Nu T = 
$$\{(0\ 0)\}$$
 (no existe base del núcleo) Im T =  $gen\{(1\ 0\ 0)\ (-2\ -5\ 0)\}$   
b. Nu T =  $gen\{(0\ 1\ 1)\}$  Im T =  $gen\{(-2\ 0\ 1)\ (1\ -1\ 0)\}$   
c. Nu T =  $gen\{(3\ 0\ 1\ 0)(2\ 1\ 0\ 0)\}$  Im T =  $gen\{(3\ 0\ 1)\ (0\ 1\ 0)\}$ 

**6.** a. 
$$T(x, y) = (-x, 3x, 4x)$$
 b.  $T(x, y, z) = (-x + 2z - y, 0, 0)$  c. No existe

## 7. Verdadero

**8.** a. M (T) = 
$$\begin{pmatrix} \frac{1}{3} & \frac{2}{5} \\ -1 & 5 \end{pmatrix}$$
 b. M(T) =  $\begin{pmatrix} 1 & 1 & 1 \\ \frac{1}{2} & \frac{1}{2} & 0 \\ 0 & 0 & -\frac{1}{4} \\ 0 & 1 & -1 \end{pmatrix}$  c. M(T) =  $\begin{pmatrix} 1 & 1 \\ 2 & 1 \\ -4 & 0 \end{pmatrix}$ 

**9.** a. 
$$T(1 -5 3) = (7 13 21)$$
,  $T(0 0 0) = (0 0 0)$ ,  $T(1 -1 1) = (3 3 5)$   
b. Im  $T = R^3$ , base de Im  $T = \{(2,1,0), (-1,-3,-3), (0,-1,2)\}$  Nu  $T = \{(0 0 0)\}$ , no tiene base.  
c.  $T(x, y, z) = (2x - y, x - 3y - z, -3y + 2z)$ 

a. 
$$\sigma(T) = \{4, 2\}$$
 B =  $\{(1, 1)(-1, 1)\}$   
b.  $\sigma(T) = \{4\}$  B =  $\{(1, 0)\}$ 

c. 
$$\sigma(T) = \{-1, 1, 3\}$$
 B =  $\{(1, 0, 0), (-3/2, 1, -1), (2, 1, -2)\}$ 

d. 
$$\sigma(T) = \{1, 2, 3\}$$
 B =  $\{(1, 0, 0), (0, 1, 2), (1, 0, 1)\}$ 

## 13.

a. 
$$k = -2$$
 b  $\sigma(T) = \{1, -3\}$ 

## 14.

a. 
$$\sigma(A) = \{1, -1\} P = \begin{pmatrix} 1 & -1 \\ 0 & 1 \end{pmatrix}$$
 b.  $\sigma(A) = \{-1, 3, 2\}$   $P = \begin{pmatrix} 1 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{pmatrix}$ 



c. 
$$\sigma(A) = \{0, 6(doble)\}. P = \begin{pmatrix} 1 & -1 & 2 \\ 1 & 1 & 0 \\ -2 & 0 & 1 \end{pmatrix}$$

c. 
$$\sigma(A) = \{0, 6 \text{(doble)}\}. P = \begin{pmatrix} 1 & -1 & 2 \\ 1 & 1 & 0 \\ -2 & 0 & 1 \end{pmatrix}$$
 d.  $\sigma(A) = \{0, -\frac{3+\sqrt{41}}{2}, \frac{\sqrt{41}-3}{2}\}$   $P = \begin{pmatrix} 4 & \frac{3+\sqrt{41}}{4} & \frac{3-\sqrt{41}}{4} \\ 1 & 1 & 1 \\ 0 & -\frac{3+\sqrt{41}}{2} & \frac{-3+\sqrt{41}}{2} \end{pmatrix}$