02.01-statistic models

March 21, 2021

1 Modelos estatísticos

Neste notebook tem os seguintes modelos estatísticos: - AR - ARIMA - SARIMA

1.1 Importações

```
[29]: # Data analysis and data wrangling
      import numpy as np
      import pandas as pd
      # Metrics
      from sklearn.metrics import mean_squared_error
      # Plotting
      import seaborn as sns
      import matplotlib.pyplot as plt
      # statsmodels
      from statsmodels.tsa.ar_model import AutoReg
      from statsmodels.tsa.arima_model import ARIMA
      from statsmodels.tsa.statespace.sarimax import SARIMAX
      import statsmodels.api as sm
      # autoarima
      import pmdarima as pm
      # Other
      from IPython.display import Image
      import warnings
      import pprint
      import datetime
      import itertools
      import os
```

1.2 Preparação do Diretório Principal

```
[30]: def prepare_directory_work(end_directory: str='notebooks'):
    # Current path
    curr_dir = os.path.dirname(os.path.realpath("__file__"))

if curr_dir.endswith(end_directory):
    os.chdir('..')
    return curr_dir

return f'Current working directory: {curr_dir}'
```

```
[31]: prepare_directory_work(end_directory='notebooks')
```

[31]: 'Current working directory: /home/campos/projects/tcc'

1.3 Formatação das células

```
[32]: # OPTIONAL: Load the "autoreload" extension so that code can change
%load_ext autoreload

# Guarantees visualization inside the jupyter
%matplotlib inline

# Print xxxx rows and columns
pd.set_option('display.max_rows', None)
pd.set_option('display.max_columns', None)
pd.set_option('float_format', '{:f}'.format)

# Supress unnecessary warnings so that presentation looks clean
warnings.filterwarnings('ignore')

# pretty print
pp = pprint.PrettyPrinter(indent=4)
```

The autoreload extension is already loaded. To reload it, use: %reload_ext autoreload

```
palette='deep',
    color_codes=True)

# graph style
sns.set(style='dark', palette='deep')

plt.style.use('fivethirtyeight')
```

1.4 Carregamento dos dados

```
[34]: %%time
     df_vale3 = pd.read_csv('data/cleansing/df_vale3_cleansing.csv',
                                   encoding='utf8',
                                   delimiter=',',
                                   parse_dates=True,
                                   index_col=0,
                                   verbose=True)
     Tokenization took: 2.10 ms
     Type conversion took: 2.88 ms
     Parser memory cleanup took: 0.01 ms
     CPU times: user 14.6 ms, sys: 635 µs, total: 15.2 ms
     Wall time: 14 ms
[35]: df_vale3.head()
[35]:
                    preco residuos tendencia sazonalidade
                                                                diff_1
                                                                          diff_2 \
     data
     2010-07-12 40.000000 1.002310 41.827333
                                                    1.000149 -0.600000 -0.460000
                                                    0.998563 0.070000 -0.530000
     2010-07-13 40.070000 1.036654 41.910833
     2010-07-14 40.080000 1.028377 41.977833
                                                    1.000439 0.010000 0.080000
     2010-07-15 39.760000 1.044658 42.045833
                                                    1.000935 -0.320000 -0.310000
     2010-07-16 38.880000 1.028132 42.123500
                                                    1.001784 -0.880000 -1.200000
                   diff_3
                             diff_4
                                       diff_5
     data
     2010-07-12 0.490000 0.980000 0.420000
     2010-07-13 -0.390000 0.560000 1.050000
     2010-07-14 -0.520000 -0.380000 0.570000
     2010-07-15 -0.240000 -0.840000 -0.700000
     2010-07-16 -1.190000 -1.120000 -1.720000
```

1.5 Divisão dos Dados

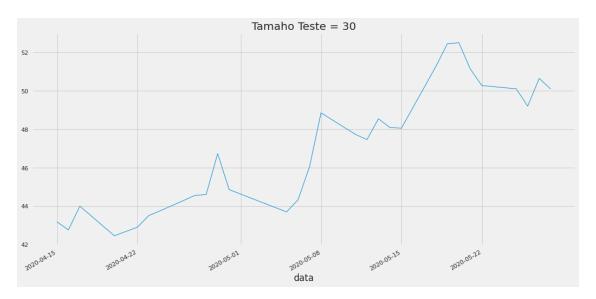
```
[36]: size_train = 2415
      size\_test = 30
      print(size_train)
      print(size_test)
      df_train = df_vale3['preco'].iloc[:size_train]
      df_test = df_vale3['preco'].iloc[size_train:]
     2415
     30
[37]: df_train.tail()
[37]: data
      2020-04-07
                   43.780000
      2020-04-08
                  43.510000
      2020-04-09 43.280000
      2020-04-13 44.570000
     2020-04-14
                  44.530000
     Name: preco, dtype: float64
[38]: df_train.plot(linewidth=1)
      plt.grid(True)
      plt.title(f'Tamaho Treinamento = {len(df_train)}')
```

[38]: Text(0.5, 1.0, 'Tamaho Treinamento = 2415')



```
[39]: df_test.head()
```

[40]: Text(0.5, 1.0, 'Tamaho Teste = 30')



1.5.1 Manipulação do índice

```
[42]: DatetimeIndex(['2020-04-15', '2020-04-16', '2020-04-17', '2020-04-20',
                     '2020-04-22', '2020-04-23', '2020-04-24', '2020-04-27',
                     '2020-04-28', '2020-04-29', '2020-04-30', '2020-05-04',
                     '2020-05-05', '2020-05-06', '2020-05-07', '2020-05-08',
                     '2020-05-11', '2020-05-12', '2020-05-13', '2020-05-14',
                     '2020-05-15', '2020-05-18', '2020-05-19', '2020-05-20',
                     '2020-05-21', '2020-05-22', '2020-05-25', '2020-05-26',
                     '2020-05-27', '2020-05-28'],
                    dtype='datetime64[ns]', name='data', freq=None)
[43]: df_train.reset_index(drop=True, inplace=True)
      df train.index
[43]: RangeIndex(start=0, stop=2415, step=1)
[44]: df test.reset index(drop=True, inplace=True)
      df test.index
[44]: RangeIndex(start=0, stop=30, step=1)
[45]: df_train.index = pd.RangeIndex(start=0, stop=len(df_train), step=1)
      df_train.index
[45]: RangeIndex(start=0, stop=2415, step=1)
[46]: df_test.index = pd.RangeIndex(start=2415, stop=len(df_vale3), step=1)
      df test.index
[46]: RangeIndex(start=2415, stop=2445, step=1)
     1.6 Métrica de Avaliação
[47]: def mean_absolute_percentage_error(y_true, y_pred):
          y true, y pred = np.array(y true), np.array(y pred)
          return np.mean(np.abs((y_true - y_pred) / y_true)) * 100
     1.7 Dicionário de Resultados
[48]: dict_results = {}
```

1.8 Impressão dos Resutados

1.9 Busca dos Melhores Parâmetros

Grid Search

```
[50]: # Define the p, d and q parameters to take any value between 0 and 2
      p = q = range(0, 3)
      d = range(0, 3)
      # Generate all different combinations of p, q and q triplets
      list_pdq = list(itertools.product(p, d, q))
      print(f'All different combinations of p, q and q:\n {list_pdq}')
      # Generate all different combinations of seasonal p, q and q triplets
      seasonal_pdq = [(x[0], x[1], x[2], 12) for x in list(itertools.product(p, d,__
      -q))]
      print(f'\n\nAll different combinations of seasonal p, q and q:\n_{\sqcup}
       →{seasonal_pdq}')
     All different combinations of p, q and q:
      [(0, 0, 0), (0, 0, 1), (0, 0, 2), (0, 1, 0), (0, 1, 1), (0, 1, 2), (0, 2, 0),
     (0, 2, 1), (0, 2, 2), (1, 0, 0), (1, 0, 1), (1, 0, 2), (1, 1, 0), (1, 1, 1), (1, 1, 1)
     1, 2), (1, 2, 0), (1, 2, 1), (1, 2, 2), (2, 0, 0), (2, 0, 1), (2, 0, 2), (2, 1,
     0), (2, 1, 1), (2, 1, 2), (2, 2, 0), (2, 2, 1), (2, 2, 2)]
     All different combinations of seasonal p, q and q:
      [(0, 0, 0, 12), (0, 0, 1, 12), (0, 0, 2, 12), (0, 1, 0, 12), (0, 1, 1, 12), (0, 1, 1, 12)]
     1, 2, 12), (0, 2, 0, 12), (0, 2, 1, 12), (0, 2, 2, 12), (1, 0, 0, 12), (1, 0, 1,
     12), (1, 0, 2, 12), (1, 1, 0, 12), (1, 1, 1, 12), (1, 1, 2, 12), (1, 2, 0, 12),
```

```
(1, 2, 1, 12), (1, 2, 2, 12), (2, 0, 0, 12), (2, 0, 1, 12), (2, 0, 2, 12), (2,
1, 0, 12), (2, 1, 1, 12), (2, 1, 2, 12), (2, 2, 0, 12), (2, 2, 1, 12), (2, 2, 2,
12)]

def search_best_params_arima_model(df_train: 'Dataframe', pdq: list) -> list:
    best_model = 99999
    host_params = (0, 0, 0)
```

```
[51]: def search_best_params_arima_model(df_train: 'Dataframe', pdq: list) -> list:
    best_model = 99999
    best_params = (0, 0, 0)
    param = ()

for param in pdq:
    try:
        arima_model = ARIMA(df_train, order=param)
        results = arima_model.fit()
        print(f'pdq = {param} | AIC = {results.aic}')

    if results.aic < best_model:
        best_model = results.aic
        best_params = param
    except:
        continue

print(f'best_ARIMA: {best_params} | AIC:{best_model}')
    return [best_params, best_model]</pre>
```

```
[52]: def search_best_params_sarima_model(df_train, trend, pdq):
          best_model = 99999
          best_param_seasonal = ()
          param = ()
          param_seasonal = ()
          for param_seasonal in seasonal_pdq:
              try:
                  sarima_model = SARIMAX(df_train,
                                          order=pdq,
                                          seasonal_order=param_seasonal,
                                          trend=trend,
                                          enforce_stationarity=True,
                                          enforce_invertibility=False)
                  results = sarima_model.fit()
                  print(f'pdq = {pdq} | param_seasonal = {param_seasonal} | AIC = |
       →{results.aic}')
                  if results.aic < best model:
                      best_model = results.aic
                      best_param_seasonal = param_seasonal
              except:
                  continue
```

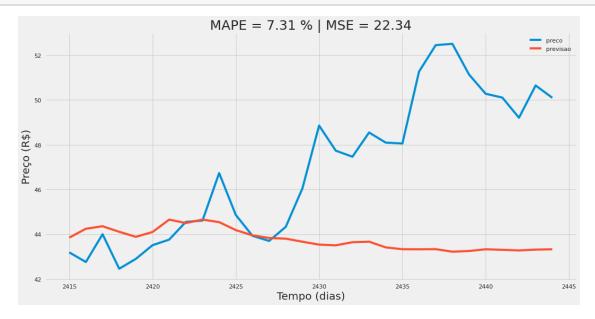
```
print(f'\n\nBest SARIMA: {pdq}x{param_seasonal}12 | AIC:{best_model}')
return [best_param_seasonal, best_model]
```

1.10 Modelos Estatísticos

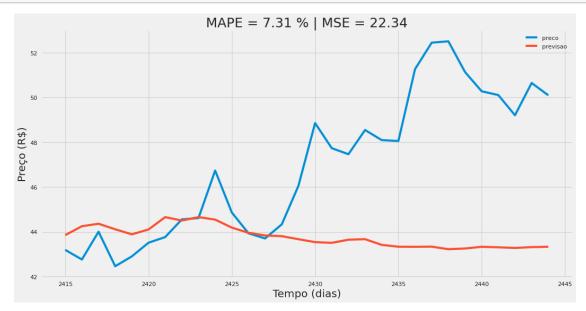
1.11 AR

- A ST não é estacionária
- Não há tendência, (trend='n')
- Não aá sazonalidade, (seasonal=False) no período de 30 dias

```
[54]: # forecast
y_ar_forecast = ar_fit.predict(start=(df_test.index[0]), end=df_test.index[-1])
```



zoom



1.11.1 ARIMA

1.12 Librarie: pmdarima

• Tips: https://alkaline-ml.com/pmdarima/tips_and_tricks.html

```
pdq = (0, 0, 0) | AIC = 18974.159932736322

pdq = (0, 0, 1) | AIC = 15847.637275064231

pdq = (0, 0, 2) | AIC = 13561.154466403974

pdq = (0, 1, 0) | AIC = 6352.768252799672

pdq = (0, 1, 1) | AIC = 6350.524624394297

pdq = (0, 1, 2) | AIC = 6340.313542113301

pdq = (0, 2, 0) | AIC = 8115.886934606986

pdq = (0, 2, 1) | AIC = 6360.642759046002

pdq = (0, 2, 2) | AIC = 6359.287622193227

pdq = (1, 0, 0) | AIC = 6358.62505633127
```

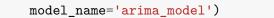
```
pdq = (1, 0, 1) \mid AIC = 6356.660857064225
     pdq = (1, 0, 2) | AIC = 6346.8611580606375
     pdq = (1, 1, 0) \mid AIC = 6351.105797529564
     pdq = (1, 1, 1) | AIC = 6343.033761417953
     pdq = (1, 1, 2) | AIC = 6336.2914261760225
     pdq = (1, 2, 0) | AIC = 7467.9662234387815
     pdq = (1, 2, 1) \mid AIC = 6359.034728262
     pdq = (2, 0, 0) \mid AIC = 6357.196557476122
     pdq = (2, 0, 1) | AIC = 6349.8852699168365
     pdq = (2, 0, 2) \mid AIC = 6342.645188065021
     pdq = (2, 1, 0) | AIC = 6341.3047553815495
     pdq = (2, 1, 1) \mid AIC = 6337.075186435318
     pdq = (2, 2, 0) | AIC = 7092.466407612979
     pdq = (2, 2, 1) | AIC = 6349.331988280079
     pdq = (2, 2, 2) | AIC = 6345.944394704168
     best ARIMA: (1, 1, 2) | AIC:6336.2914261760225
     [(1, 1, 2), 6336.2914261760225]
     CPU times: user 22.8 s, sys: 11.8 s, total: 34.5 s
     Wall time: 12.8 s
[58]: %%time
      autoarima_model = pm.auto_arima(df_train,
                                       stepwise=True,
                                       suppress_warnings=True,
                                       error_action="ignore",
                                       information_criterion='aic',
                                       start_p=1,
                                       start_d=1,
                                       start_q=2,
                                       \max_{p=30}
                                       \max_{d=30}
                                       \max_{q=30}
                                       # trend=False,
                                       seasonal=False,
                                       trace=True)
     Performing stepwise search to minimize aic
      ARIMA(1,1,2)(0,0,0)[0] intercept
                                           : AIC=6336.291, Time=0.89 sec
```

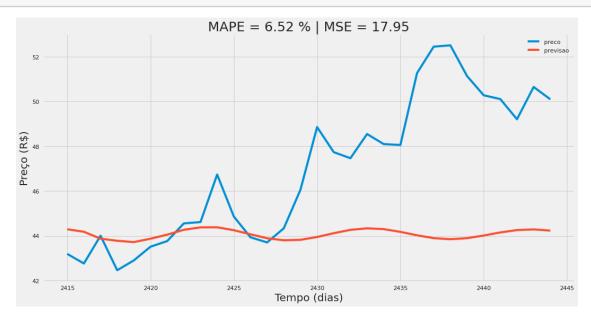
ARIMA(0,1,0)(0,0,0)[0] intercept : AIC=6352.768, Time=0.84 sec : AIC=6351.106, Time=0.13 sec ARIMA(1,1,0)(0,0,0)[0] intercept : AIC=6350.525, Time=0.20 sec ARIMA(0,1,1)(0,0,0)[0] intercept : AIC=6350.779, Time=0.05 sec ARIMA(0,1,0)(0,0,0)[0]: AIC=6340.314, Time=0.29 sec ARIMA(0,1,2)(0,0,0)[0] intercept ARIMA(1,1,1)(0,0,0)[0] intercept : AIC=6343.034, Time=0.84 sec : AIC=6335.575, Time=2.29 sec ARIMA(2,1,2)(0,0,0)[0] intercept ARIMA(2,1,1)(0,0,0)[0] intercept : AIC=6337.075, Time=1.47 sec

ARIMA(3,1,2)(0,0,0)[0] intercept

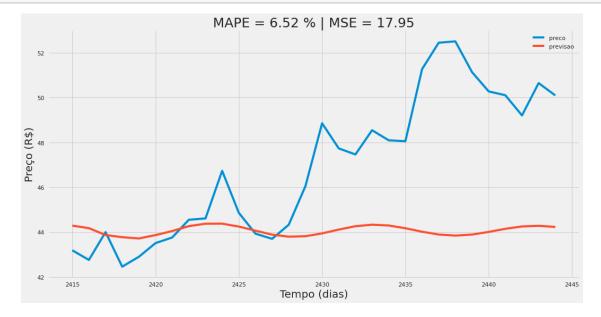
: AIC=6336.166, Time=1.74 sec

```
ARIMA(2,1,3)(0,0,0)[0] intercept
                                          : AIC=6334.093, Time=3.54 sec
      ARIMA(1,1,3)(0,0,0)[0] intercept
                                         : AIC=6337.673, Time=1.21 sec
      ARIMA(3,1,3)(0,0,0)[0] intercept
                                         : AIC=6336.181, Time=2.87 sec
      ARIMA(2,1,4)(0,0,0)[0] intercept
                                          : AIC=6337.758, Time=4.31 sec
      ARIMA(1,1,4)(0,0,0)[0] intercept
                                         : AIC=6336.944, Time=1.93 sec
                                         : AIC=6321.479, Time=5.36 sec
      ARIMA(3,1,4)(0,0,0)[0] intercept
      ARIMA(4,1,4)(0,0,0)[0] intercept
                                         : AIC=6325.029, Time=5.96 sec
                                         : AIC=6323.272, Time=12.73 sec
      ARIMA(3,1,5)(0,0,0)[0] intercept
      ARIMA(2,1,5)(0,0,0)[0] intercept
                                         : AIC=6339.721, Time=8.50 sec
                                         : AIC=6336.502, Time=4.15 sec
      ARIMA(4,1,3)(0,0,0)[0] intercept
                                          : AIC=6323.836, Time=13.31 sec
      ARIMA(4,1,5)(0,0,0)[0] intercept
                                          : AIC=6319.397, Time=3.36 sec
      ARIMA(3,1,4)(0,0,0)[0]
                                          : AIC=6335.771, Time=1.87 sec
      ARIMA(2,1,4)(0,0,0)[0]
                                          : AIC=6334.044, Time=1.90 sec
      ARIMA(3,1,3)(0,0,0)[0]
                                         : AIC=6322.980, Time=4.12 sec
      ARIMA(4,1,4)(0,0,0)[0]
      ARIMA(3,1,5)(0,0,0)[0]
                                         : AIC=6321.422, Time=5.42 sec
      ARIMA(2,1,3)(0,0,0)[0]
                                         : AIC=6332.106, Time=0.84 sec
      ARIMA(2,1,5)(0,0,0)[0]
                                         : AIC=6337.734, Time=10.79 sec
      ARIMA(4,1,3)(0,0,0)[0]
                                         : AIC=6334.328, Time=2.35 sec
                                         : AIC=6321.854, Time=2.45 sec
      ARIMA(4,1,5)(0,0,0)[0]
     Best model: ARIMA(3,1,4)(0,0,0)[0]
     Total fit time: 105.743 seconds
     CPU times: user 5min 39s, sys: 3min 18s, total: 8min 58s
     Wall time: 1min 45s
[59]: print(autoarima_model.order)
      print(autoarima_model.aic())
     (3, 1, 4)
     6319.39685000518
[60]: # fit
      autoarima_model_fit = autoarima_model.fit(y=df_train)
      autoarima_model_fit
[60]: ARIMA(order=(3, 1, 4), scoring_args={}, suppress_warnings=True,
            with_intercept=False)
[61]: # forecast
      y_forecast = autoarima_model_fit.predict(n_periods=len(df_test[:50]))
      len(y_forecast)
[61]: 30
[62]: show_result_model(df_train=df_train,
                        df_test=df_test,
                        y_forecast=y_forecast,
```





Zoom

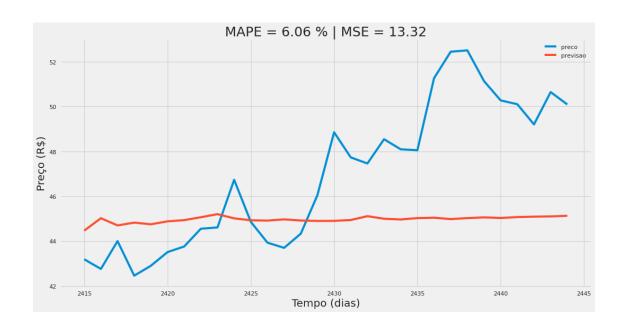


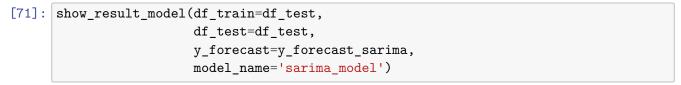
1.13 **SARIMA**

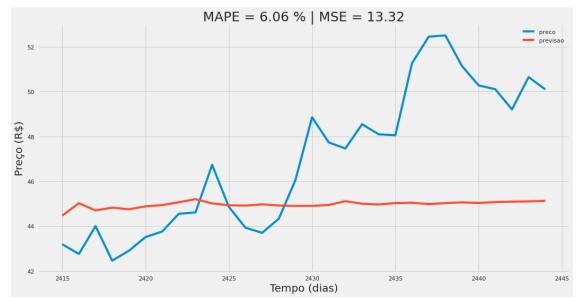
```
[64]: %%time
     list_order_seasonal aic = search_best_params_sarima_model(df_train=df_train,
                                                                trend='t',
                                                                pdq=(3, 1, 3))
     print(list_order_seasonal_aic)
     pdq = (3, 1, 3) | param_seasonal = (0, 0, 0, 12) | AIC = 6339.124621859275
     pdq = (3, 1, 3) | param_seasonal = (0, 0, 1, 12) | AIC = 6338.031419311456
     pdq = (3, 1, 3) | param_seasonal = (0, 0, 2, 12) | AIC = 6336.018124144093
     pdq = (3, 1, 3) | param_seasonal = (0, 1, 0, 12) | AIC = 8059.09988429914
     pdq = (3, 1, 3) | param_seasonal = (0, 1, 1, 12) | AIC = 7004.804412774307
     pdq = (3, 1, 3) | param_seasonal = (0, 1, 2, 12) | AIC = 6912.811466815344
     pdq = (3, 1, 3) | param seasonal = (0, 2, 0, 12) | AIC = 10631.931835186979
     pdq = (3, 1, 3) | param_seasonal = (0, 2, 1, 12) | AIC = 9840.03632141267
     pdq = (3, 1, 3) | param seasonal = (0, 2, 2, 12) | AIC = 8910.811939479154
     pdq = (3, 1, 3) | param_seasonal = (1, 0, 0, 12) | AIC = 6338.128198280105
     pdq = (3, 1, 3) | param seasonal = (1, 0, 1, 12) | AIC = 6335.981000287489
     pdq = (3, 1, 3) | param seasonal = (1, 0, 2, 12) | AIC = 6336.456711085466
     pdq = (3, 1, 3) | param seasonal = (1, 1, 0, 12) | AIC = 7440.089436402188
     pdq = (3, 1, 3) | param_seasonal = (1, 1, 1, 12) | AIC = 7021.478686571869
     pdq = (3, 1, 3) | param_seasonal = (1, 1, 2, 12) | AIC = 6919.713727034271
     pdq = (3, 1, 3) | param_seasonal = (1, 2, 0, 12) | AIC = 9539.404449558362
     pdq = (3, 1, 3) | param_seasonal = (1, 2, 1, 12) | AIC = 8963.305012269524
     pdq = (3, 1, 3) | param_seasonal = (1, 2, 2, 12) | AIC = 9679.523799182765
     pdq = (3, 1, 3) | param_seasonal = (2, 0, 0, 12) | AIC = 6336.465787506138
     pdq = (3, 1, 3) | param_seasonal = (2, 0, 1, 12) | AIC = 6335.857132528785
     pdq = (3, 1, 3) | param_seasonal = (2, 0, 2, 12) | AIC = 6338.7335421307
     pdq = (3, 1, 3) | param_seasonal = (2, 1, 0, 12) | AIC = 7250.051289167632
     pdq = (3, 1, 3) | param_seasonal = (2, 1, 1, 12) | AIC = 7037.807659090762
     pdq = (3, 1, 3) | param seasonal = (2, 1, 2, 12) | AIC = 6919.0597162293125
     pdq = (3, 1, 3) | param_seasonal = (2, 2, 0, 12) | AIC = 9235.612146737145
     pdq = (3, 1, 3) | param seasonal = (2, 2, 1, 12) | AIC = 8983.171488430893
     pdq = (3, 1, 3) | param_seasonal = (2, 2, 2, 12) | AIC = 9260.152640966668
     Best SARIMA: (3, 1, 3)x(2, 2, 12)12 | AIC:6335.857132528785
     [(2, 0, 1, 12), 6335.857132528785]
     CPU times: user 1h 32min 33s, sys: 1h 5min 34s, total: 2h 38min 8s
     Wall time: 29min 54s
[65]: list_order_seasonal_aic
```

[65]: [(2, 0, 1, 12), 6335.857132528785]

```
[66]: # autosarima_model = pm.auto_arima(df_train,
                                          stepwise=True,
      #
                                          suppress_warnings=True,
      #
                                          error_action="ignore",
      #
                                          information_criterion='aic',
      #
                                          start_p=3,
      #
                                          start_d=1,
      #
                                          start_q=3,
      #
                                          max_p=30,
      #
                                          max_d=30,
      #
                                          max_q=30,
      #
                                          seasonal=True,
      #
                                          stationary=False,
      #
                                          trace=True)
[67]: sarima_model = SARIMAX(df_train,
                              order=(6, 2, 6),
                              seasonal_order=list_order_seasonal_aic[0],
                              trend='c',
                              enforce_stationarity=False,
                              enforce_invertibility=False)
[68]: # fit
      sarima_fit = sarima_model.fit()
      print(sarima_fit)
     <statsmodels.tsa.statespace.sarimax.SARIMAXResultsWrapper object at</pre>
     0x7fe7585edac0>
[69]: # forecast
      y_forecast_sarima = sarima_fit.predict(start=df_test.index[0], end=df_test.
       \rightarrowindex[-1])
      print(len(y_forecast_sarima))
     30
[70]: show_result_model(df_train=df_train,
                         df_test=df_test,
                         y_forecast=y_forecast_sarima,
                         model_name='sarima_model')
```







1.14 Resultados