

# BrunoFBessa\_5881890\_P8\_results

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## 0.1 SFI5904 - Complex Networks

Project 8: Centrality and acessibility measures in complex networks First Semester of 2021

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A: Obtain the accessibility values for  $h=2, 3$  and  $4$  for each node of geographic, ER, BA, WS (with  $3$  probabilities of reconnection). Show the respective histograms for relative frequency.

B: Identify the borders of the networks using thresholding of the accessibility for each node and visuaize the network border marking it with different color.

## 0.2 Results (A)

For this experiment the following synthetic networks were used (all with  $N=300$  nodes and tuned so that their average degree lied between  $5$  and  $7$ ):

ER = Erdos-Renyi (prob=0.02)

BA = Barabási-Albert (m=4, plot=False)

VO = Voronoi

RA = Spatial with Radius (radius=0.079)

WX = Waxman (alpha=0.048)

WS\_1 = Watts-Strogatz (prob=0.1)

WS\_2 = Watts-Strogatz (prob=0.2)

WS\_3 = Watts-Strogatz (prob=1.0)

We calculated  $a_i$  for a node  $i$  the accessibility [1] according to:

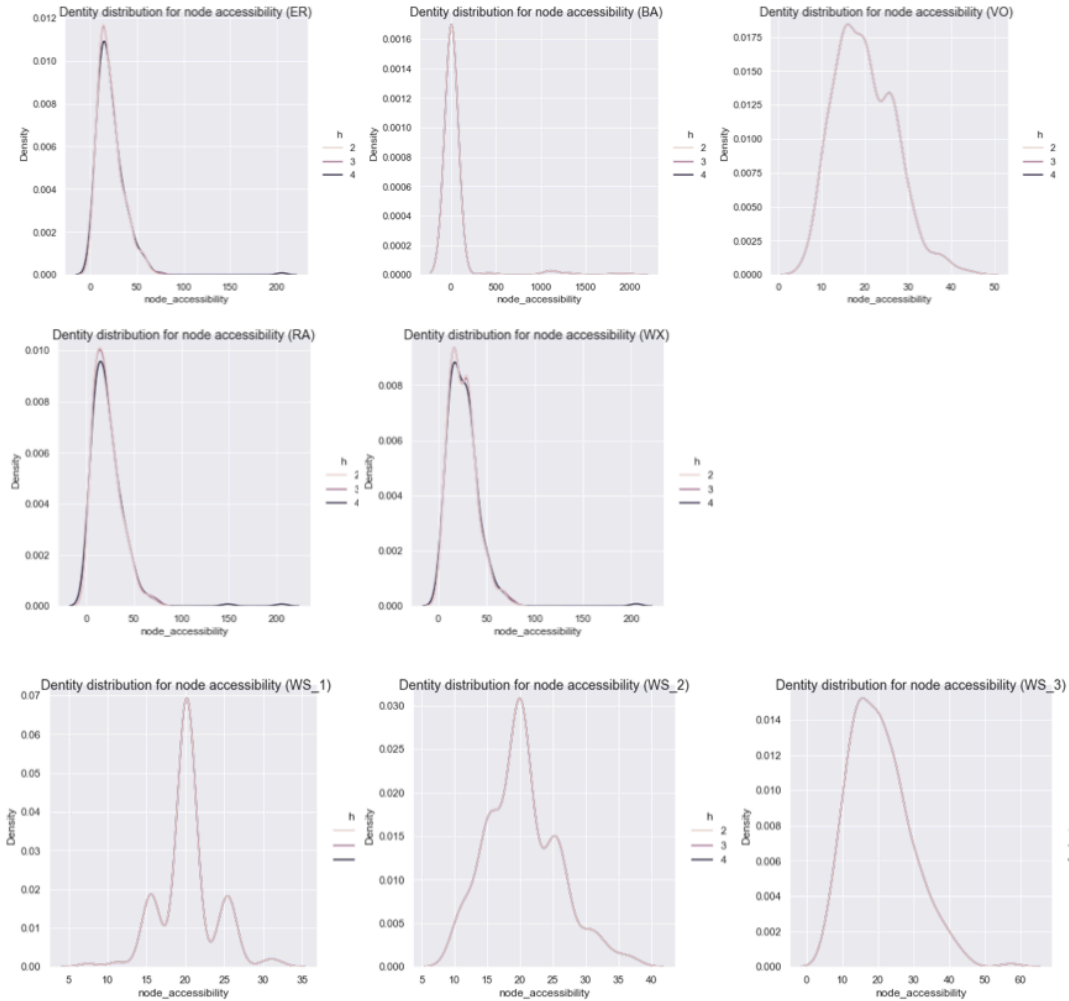
$$H_i = \sum_j p_j \log(p_j) a_i = e^{(H_i)}$$

where  $p$  is the transition probability from node  $i$  to node  $j$ . We calculated this metric for different values of distances from  $i$  ( $h$  parameter).

The results for the suggested networks are as follows:

```
[2]: display.Image("images/results_accessibility.png")
```

[2]:



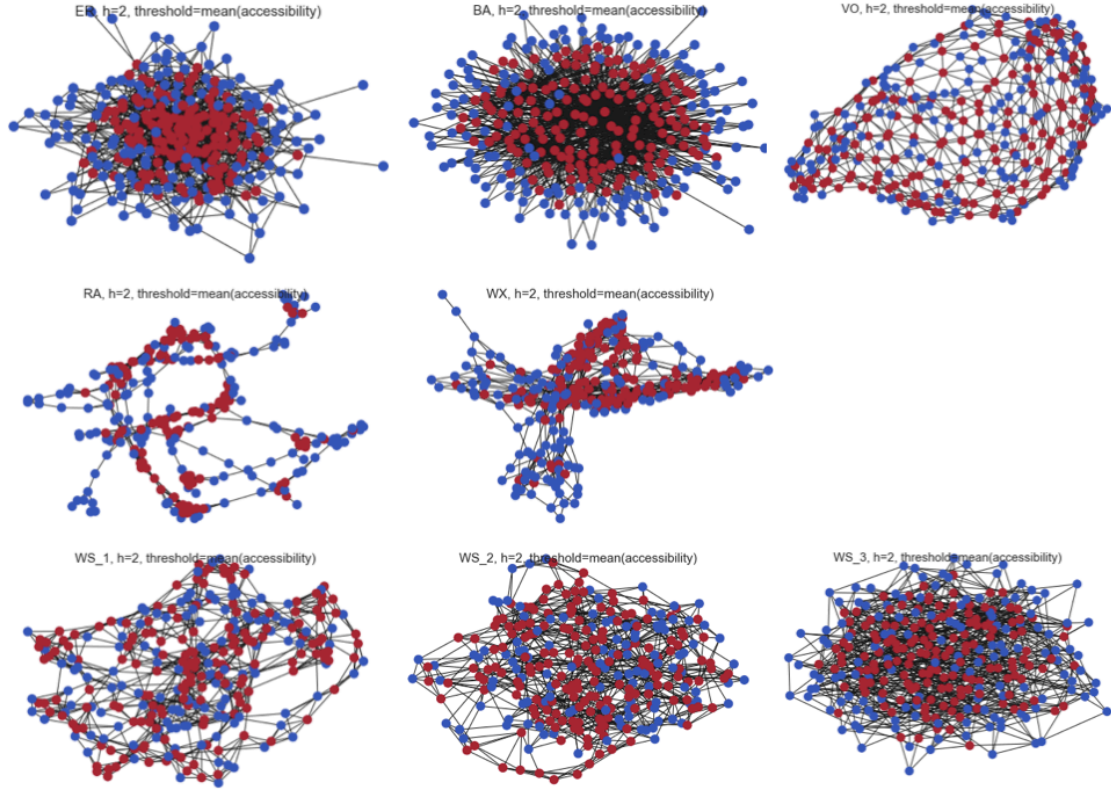
### 0.3 Results (B)

We used the accessibility values for all the nodes of the networks (for  $h=2$ ) and set a threshold for it to be considered high or low (the mean value).

The borders of the networks could be spotted as those nodes with low value for accessibility.

```
[3]: display.Image("images/centrality_accessibility.png")
```

[3]:



<sup>1</sup> Blue: low accessibility, Red: high accessibility

## 0.4 Conclusion

The accessibility value accordingly to this implementation converges rapidly to a stable value and does not change much for  $h > 1$ .

The accessibility is a good metric to detect borders of a network.

## 0.5 References

- [1] Travençolo, B. A., Viana, M. P., Costa, L. F., Border detection in complex networks, New Journal of Physics, March, 2009