

# CGraph documentation

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## Abstract

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## 1 sorting

2 stat

**3** list

4 set

## 5 graph

## 6 graph\_metric

### 6.1 Constants

These constants are hard-coded to protect some numeric processes of hanging. They can be redefined during compilation, passing a flag such as  
-DGRAPH\_METRIC\_TOLERANCE=1E-3.

#### 6.1.1 GRAPH\_METRIC\_TOLERANCE

Error tolerance for numeric methods.

#### 6.1.2 GRAPH\_METRIC\_MAX\_ITERATIONS

Maximum number of iterations for numeric methods.

### 6.2 Component identification and extraction

#### 6.2.1 graph\_undirected\_components

Label vertices' components treating edges as undirected.

**Preconditions** `label` must have dimension  $n$ .

**Postconditions** `label[i]` is the component ID of vertex  $v_i$ .

**Return** Number of components

For directed graphs, considers adjacencies as incidences. Labels start from 0 and are sequential with step 1. Component IDs are not ordered according to size.

#### 6.2.2 graph\_directed\_components

Label vertices' components treating edges as directed. NOT IMPLEMENTED YET.

**Preconditions** `label` must have dimension  $n$ .

**Postconditions** `label[i]` is the component ID of vertex  $v_i$ .

**Return** Number of components

For undirected graphs, simply call `graph_undirected_components`. For directed graphs, two vertices  $v_i$  and  $v_j$  are in the same component if and only if

$$\begin{aligned}d(v_i, v_j) &\neq \infty \\d(v_j, v_i) &\neq \infty\end{aligned}$$

where  $d(u, v)$  is the geodesic distance between them. In other words, they are in the same component if they are mutually reachable.

Labels start from 0 and are sequential with step 1. Component IDs are not ordered according to size.



### 6.2.3 `graph_num_components`

Extract number of components from label vector.

#### **Preconditions**

$n > 0$   
`label` must have dimension  $n$ .  
`label` must contain sequential IDs starting from 0.

**Return** Number of components

### 6.2.4 `graph_components`

Map components to vertices from label vector.

#### **Preconditions**

$n > 0$   
`label` must have dimension  $n$ .  
`label` must contain sequential IDs starting from 0.  
`comp` must have size `num_comp` and all sets should be already initialized.  
`graph_num_components(g) == num_comp`

#### **Postconditions**

If  $v_i$  is in component  $c_j$ , then  
`label[i] == j` and  
`set_contains(comp[j], i)` is true.

**Return** Number of components

### 6.2.5 `graph_components`

Creates a new graph from `g`'s largest component.

The guarantee of vertices' order ID is the same as `graph_subset`. If two or more components have the same maximum size, one will be chosen in an undefined way.

**Return** A new graph isomorphic to `g`'s largest component.

#### **Memory deallocation**

```
graph_t *largest = graph_components(g);  
delete_graph(largest);
```

## 6.3 Degree metrics

### 6.3.1 `graph_degree`

List all vertices' degrees.

**Preconditions** `degree` must have dimension  $n$ .

**Postconditions** `degree[i]` is the degree of vertex  $v_i$ .

The degree of a directed graph's vertex is defined as the sum of incoming and outgoing edges.

### 6.3.2 graph\_directed\_degree

List all vertices' incoming and outgoing degrees.

#### Preconditions

`g` must be directed. `in_degree` must have dimension  $n$ . `out_degree` must have dimension  $n$ .

#### Postconditions

`in_degree[i]` is the number of incoming edges to vertex  $v_i$ . `out_degree[i]` is the number of outgoing edges from vertex  $v_i$ .

## 6.4 Clustering metrics

### 6.4.1 graph\_clustering

List all vertices' local clustering.

#### Preconditions

`g` must be undirected.  
`clustering` must have dimension  $n$ .

**Postconditions** `clustering[i]` is the local clustering coefficient of vertex  $v_i$ .

The local clustering coefficient is only defined for undirected graphs, and gives the ratio of edges between a vertex' neighbors and all possible edges.

Formally,

$$C_i = \frac{e_i}{\binom{k_i}{2}} = \frac{2e_i}{k_i(k_i - 1)}$$

where

$C_i$  is the local clustering coefficient of vertex  $v_i$ .

$e_i$  is the number of edges between  $v_i$ 's neighbors.

$k_i$  is the degree of  $v_i$ .

If a vertex  $v_i$  has 0 or 1 adjacents,  $C_i = 0$  by definition.

### 6.4.2 graph\_num\_triplets

Counts number of triplets and triangles ( $6 * \text{number of closed triplets}$ ).

### 6.4.3 graph\_transitivity

Compute the ratio between number of triangles and number of triplets.

## **6.5 Geodesic distance metrics**

### **6.5.1 Definitions**

**6.5.2** `graph_geodesic_distance`

**6.5.3** `graph_geodesic_vertex`

**6.5.4** `graph_geodesic_all`

**6.5.5** `graph_geodesic_distribution`

## **6.6 Centrality measures**

**6.6.1** `graph_betweenness`

**6.6.2** `graph_eigenvector`

**6.6.3** `graph_pagerank`

**6.6.4** `graph_kcore`

## **6.7 Correlation measures**

**6.7.1** `graph_degree_matrix`

**6.7.2** `graph_neighbor_degree_vertex`

**6.7.3** `graph_neighbor_degree_all`

**6.7.4** `graph_knn`

**6.7.5** `graph_assortativity`

## 7 graph\_layout

### 7.1 Types

#### 7.1.1 coord\_t

Euclidean coordinates in 2D.

#### 7.1.2 box\_t

Box (rectangle) definition in 2D, given by its SW and NE vertices in a positively oriented world frame, such as the screen. Images may have a negatively oriented frame, with  $y$  pointing down. It is necessary that `box.sw.y < box.ne.y` and `box.sw.x < box.ne.x`.

#### 7.1.3 color\_t

Array with 4 colors between 0 and 255, inclusive: red ( $R$ ), green ( $G$ ), blue ( $B$ ) and alpha ( $A$ ).  $A = 0$  means totally transparent, and  $A = 255$  means totally opaque.

#### 7.1.4 circle\_style\_t

SVG circle style.

`radius` Circle radius in pixels.

`width` Stroke width in pixels. This is added to the radius for total size.

`fill` Color of the fill.

`stroke` Color of the stroke.

#### 7.1.5 path\_style\_t

SVG path style.

`type` Path type.

`from`, `to` Path origin and destination.

`control` Control point

`width` Stroke width in pixels.

`color` Stroke color.

For `style.type == GRAPH_STRAIGHT`, draws a straight line from origin to destination.

For `style.type == GRAPH_PARABOLA`, draws a parabola from origin to destination using the control point.

For `style.type == GRAPH_CIRCULAR`, draws the arc of a circle from origin to destination using the control point as the circle center.

## 7.2 Layout

### 7.2.1 `graph_layout_random`

Place points uniformly inside specified box.

#### Preconditions

`box` must be a valid box.

`p` must have dimension  $n$ .

**Postconditions** `p[i]` is a random coordinate inside `box`.

### 7.2.2 `graph_layout_random_wout_overlap`

Place points with specified radius uniformly avoiding overlap with probability  $t$ .

#### Preconditions

`radius` must be positive.

$t$  must be a valid probability ( $0 \geq t \geq 1$ ).

`p` must have dimension  $n$ .

**Postconditions** `p[i]` is a random coordinate.

The algorithm determines a box with size  $l$  such that, if  $n$  points with radius  $r$  are thrown within it, will not have any collision with probability  $t$ . The formula is derived in Math Exchange.

$$l = \frac{nr}{2} \sqrt{\frac{2\pi}{-\log(1-t)}}$$

## 7.3 Printing

### 7.3.1 `graph_print_svg`

Prints graph as SVG to file, using vertex coordinates given in `p` and with a style for each point and edge.

#### Preconditions

`p` must have dimension  $n$ . `point_style` must have dimension  $n$ . `edge_style` must have dimension  $m$ .

**Postconditions** `filename` is a valid SVG file.

Edges are ordered according to vertices' order. In undirected graphs, an edge  $E_{ij}$  is considered only if  $i < j$ . In directed graphs, mutual edges will superimpose if `edge_style.type == GRAPH_STRAIGHT`.

### 7.3.2 `graph_print_svg_one_style`

Prints graph as SVG to file, using vertex coordinates given in `p` and with a single style for all points and edges.

**Preconditions**

`p` must have dimension  $n$ .

**Postconditions** `filename` is a valid SVG file.

The edge style type is ignored, using only `GRAPH_STRAIGHT`.

**7.3.3 graph\_print\_svg\_some\_styles**

Prints graph as SVG to file, using vertex coordinates given in `p` and with a number of styles given. The mapping vertex→style is given in `ps`, and the mapping edge→style is given in `es`.

**Preconditions**

`p` must have dimension  $n$ .

`ps` must have dimension  $n$ .

`es` must have dimension  $m$ .

`point_style` must have dimension `num_point_style`.

`edge_style` must have dimension `num_edge_style`.

**Postconditions** `filename` is a valid SVG file.

This function tries to avoid extensive memory utilization one just some styles are desired. If vertex  $v_i$  should have style  $S_j$ , then `ps[i] = j`. Ditto for edges.

Edge order is based on vertices order. In undirected edges, edge  $E_{ij}$  is considered only if  $i < j$ .

## 8 graph\_model

### 8.1 Graph creation

8.1.1 new\_erdos\_renyi

8.1.2 new\_watts\_strogatz

8.1.3 new\_barabasi\_albert