

# **Circuit Theory and Electronics Fundamentals**

Department of Electrical and Computer Engineering, Técnico, University of Lisbon

## **Fifth Laboratory Report**

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# 1 Introduction

The aim of this laboratory assignment was to design and create a BandPass Filter using an OP-AMP with a central frequency of 1kHz and a gain of 40dB. The architecture of the circuit designed is the one showed in the following diagram of Figure 1. These diagram and circuit is heavily inspired by the one proposed in the "in person" lab class.

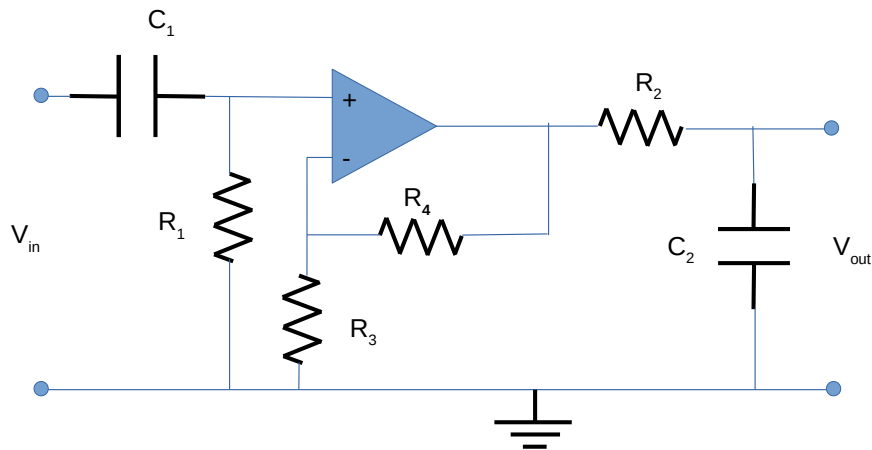


Figure 1: Basic circuit architecture of a BandPass Filter.

To determine the quality of the circuit built and to compare it with others, a Merit figure will be calculated based on the following equation:

$$MERIT = \frac{1}{cost * (GainDeviation + CentralFrequencyDeviation + 10^6)} \quad (1)$$

where the *cost* value states for sum of the tabulated cost of the components used, *GainDeviation* states for the gain deviation from 40dB and *CentralFrequencyDeviation* for the central frequency deviation from 1kHz, of the BandPass Filter.

The values chosen for the circuit components used can be seen in Table 1. These values were chosen after running some theoretical and simulation test analysis and are introduced here because they are the values that ended up being used in the last theoretical and simulation analysis, which are the ones shown in this report.

Name	Value
$R_1$	1.000000e+03 Ohm
$R_2$	1.000000e+03 Ohm
$R_3$	1.000000e+05 Ohm
$R_4$	1.000000e+03 Ohm
$C_1$	2.200000e-07 F
$C_2$	2.200000e-07 F

Table 1: Chosen values of the circuit components.

In this laboratory was used a 741 OPAMP model.

In this report, the results obtained in theoretical analysis made in OCTAVE and simulation made in NGSPICE will be shown in their respective sections and, ultimately, compared.

In Section 2, a theoretical analysis of the circuit built is presented using the values of Table 1. In this analysis Gain, input and output impedances at the Central Frequency and frequency response analysis will be done. In Section 3, the circuit is analysed by simulation in NGSPICE also using the values of Table 1. In Section 4 the results from theoretical and simulation analysis are compared. The conclusions of this study are outlined in Section 5.

## 2 Theoretical Analysis

In this section we will theoretically analyse the circuit of Figure 1 using OCTAVE tools. This analysis will start with the calculation of the output voltage gain and central frequency. Then, the input and output impedances at the central frequency previously calculated will be determined. Finally, a frequency response analysis is presented.

### 2.1 Output Voltage Gain and Central Frequency

To determine the central frequency, the angular upper ( $\omega_H$ ) and lower ( $\omega_L$ ) frequencies were calculated using the following expressions:

$$\omega_H = \frac{1}{R_2 * C_2} \quad (2)$$

$$\omega_L = \frac{1}{R_1 * C_1} \quad (3)$$

The central frequency is now given by:

$$centralfrequency = \frac{\sqrt{\omega_L * \omega_H}}{2\pi} \quad (4)$$

The output voltage gain, in dB, was obtained through the following expression

$$Gain = 20 * \log(|\frac{R_1 * C_1 * \sqrt{\omega_L * \omega_H} * j}{1 + R_1 * C_1 * \sqrt{\omega_L * \omega_H} * j} * (1 + \frac{R_3}{R_4}) * \frac{1}{1 + R_2 * C_2 * \sqrt{\omega_L * \omega_H} * j}|) \quad (5)$$

The values obtained are shown in Table 2.

Name	Value
Gain	3.406583e+01 dB
Centralfrequency	7.234316e+02 Hz

Table 2: Theoretical output voltage gain and central frequency.

### 2.2 Input and Output Impedances at Central Frequency

The input impedance at the central frequency determined previously was calculated using the following expression:

$$Z_{in} = |R_1 + \frac{1}{j * \sqrt{\omega_L * \omega_H} * C_1}| \quad (6)$$

And the output impedance at the central frequency was calculated using the following expression:

$$Z_{out} = |\frac{1}{j * \sqrt{\omega_L * \omega_H} * C_2 + \frac{1}{R_2}}| \quad (7)$$

Its values are shown in Table 3.

Name	Value
$Z_{input}$	1.414214e+03 Ohm
$Z_{output}$	7.071068e+02 Ohm

Table 3: Theoretical input and output impedances at central frequency.

## 2.3 Frequency Response

The graphic of Figure 2 shows the frequency response of the output voltage gain, in dB, of the BandPass Filter.

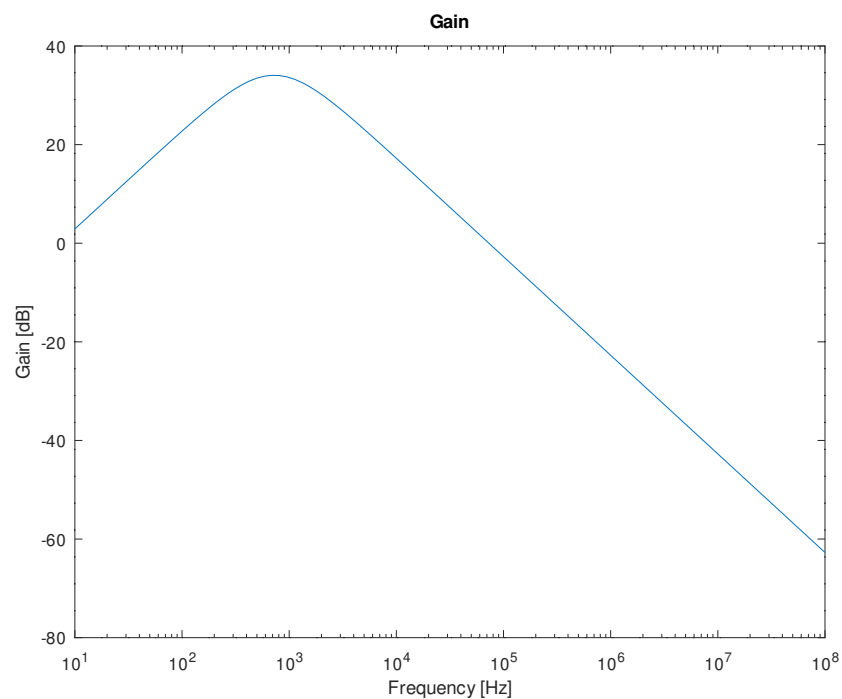


Figure 2: Frequency response of the output voltage gain. The  $x$  axis represents the frequency in Hertz (Hz) and the  $y$  axis the Gain in dB.

The graphic of Figure 3 shows the frequency response of the phase, in degrees.

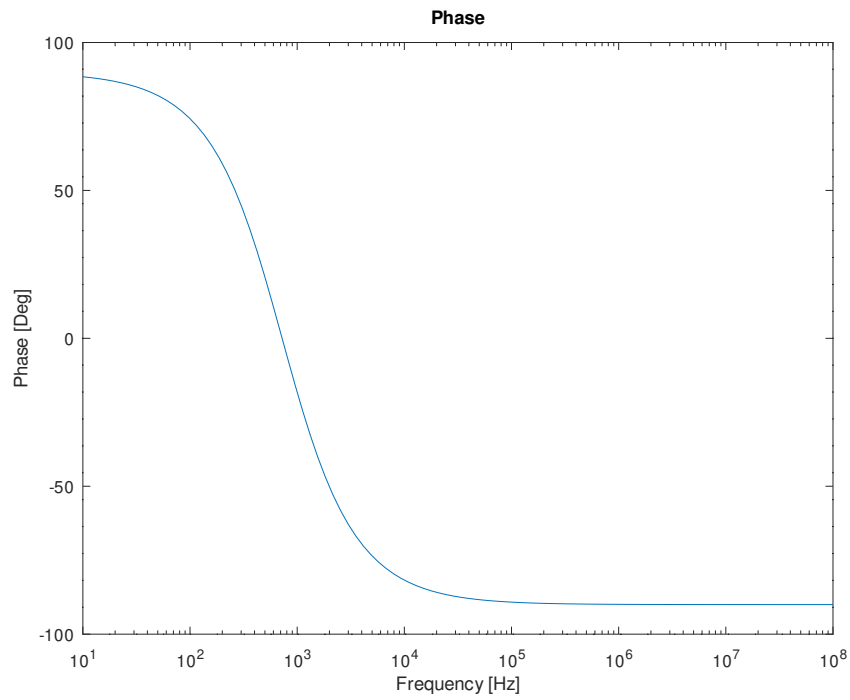


Figure 3: Frequency response of the phase. The *x axis* represents the frequency in Hertz (Hz) and the *y axis* the Phase in degrees.

### 3 Simulation Analysis

In this section, the circuit built (Figure 1) will be analyzed and simulated using NGSPICE.

Before simulating the circuit shown before, we used NGSPICE tools to simulate different circuit configurations and combinations of values for the various components of the circuit to obtain a decent merit value, while trying to get the central frequency and gain asked.

#### 3.1 Output Voltage Gain and Central Frequency

The gain in dB units is given in the Table 4.

Name	Value [dB]
gain	3.642084e+01

Table 4: Value of simulated output voltage gain.

The Upper, Lower and Central Frequencies are given by the Table 5. These values will be further discussed in the comparison section of this report, but just by observing we can tell these values are within the values expected, especially the central frequency value which is close to the expected 1kHz.

Name	Value [Hz]
lowerfreq	3.999743e+02
upperfreq	2.499041e+03
centralfreq	9.997761e+02

Table 5: Simulated upper, lower and central frequencies

#### 3.2 Input and Output Impedances at Central Frequency

The Table 6 shows the Input Impedance at central frequency from simulation analysis.

Name	Value [kOhm]
zin	9.990174e+02

Table 6: Simulated Input Impedance at central frequency.

The Table 7 shows the Output Impedance at central frequency from simulation analysis.

Name	Value [kOhm]
zout	2.708959e+00

Table 7: Simulated Output Impedance at central frequency.

#### 3.3 Merit Figure

To calculate the merit figure, the values of the output voltage gain deviation from 40dB, the central frequency deviation from 1kHz and the cost of the components used were calculated and can be seen in Table 8, as well as the resulting merit figure.

Name	Value
gaindev	3.579164e+00
centraldev	2.239378e-01
cost	1.342644e+04
merit	1.958399e-05

Table 8: Values obtained for the merit figure calculation.

### 3.4 Frequency Response

The simulated output voltage gain in terms of frequency is shown in Figure 4.

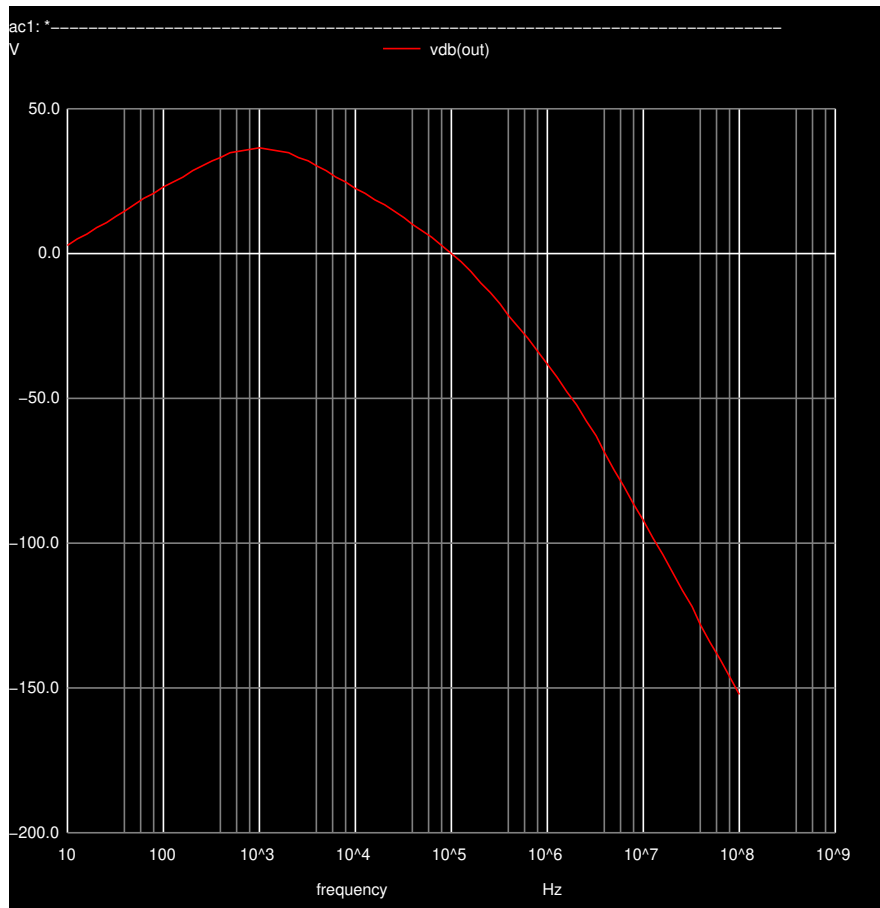


Figure 4: Frequency response of the gain in dB scale. The  $x$  axis represents the frequency in Hertz (Hz) and the  $y$  axis the gain in Volts.

And the plot of the phase function is given by the graphic of Figure 5.



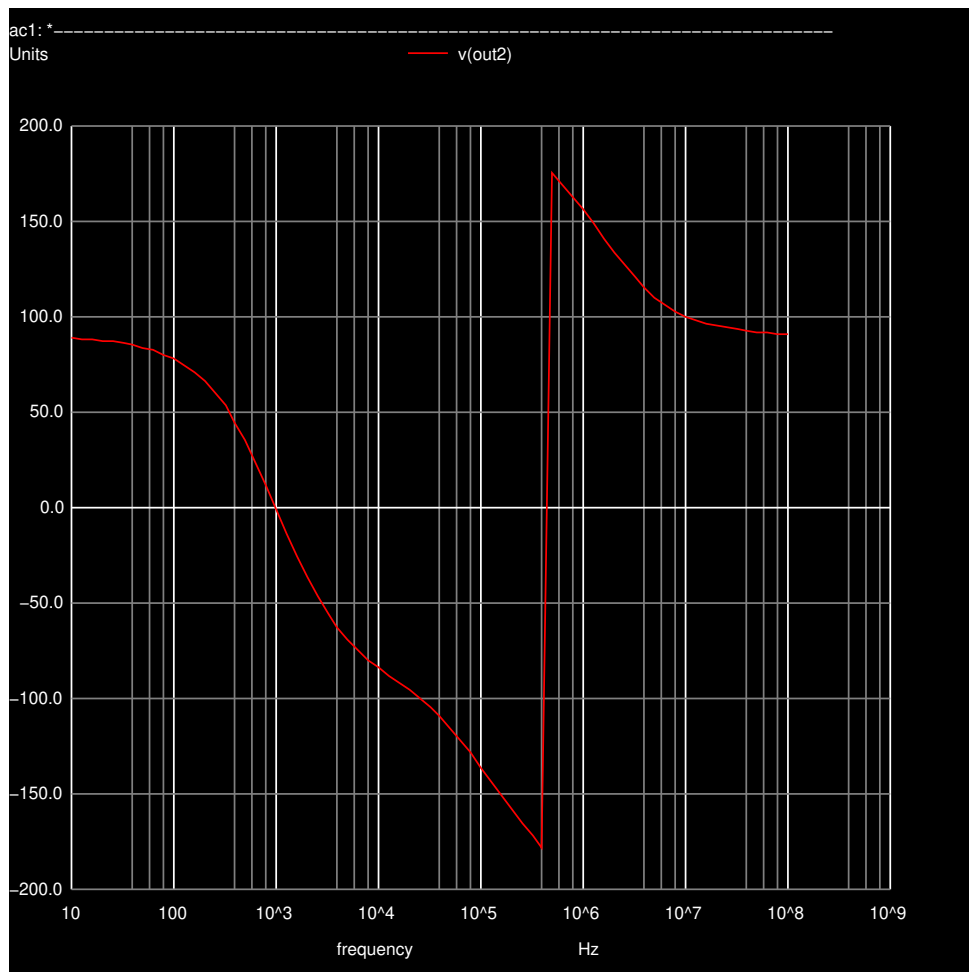


Figure 5: Phase in degrees in terms of Frequency in Hz.

## 4 Comparison

We will now compare the results of more interest obtained in the theoretical analysis and the simulation analysis.

For the impedance values, the Theoretical Results were the following:

And the Simulation results obtained were:

In both cases the Output Impedance is under enough to prevent signal loss when connecting the circuit to a speaker of 8Ohm.

For the Gain Frequency Response this is the graphic obtained theoretically:

And the simulation one is:

Analyzing these values we notice that there is some difference between the theoretical prediction and the simulation. But we can also notice that, besides the differences, the results obtained were relatively good in both analysis. The simulation analysis gave the best results.

The differences seen in the results can be attributed to diverse causes. The differences between the values of impedance can be due to the fact that in the Simulation, these are not calculated for the intermediate stages of the circuit, while that was done in the theoretical analysis.

These differences also can be given to the fact that the circuit is quite complex, and contains non linear elements like transistors which always influences the accuracy of the results obtained, especially in the Simulation Analysis, so it explains the differences in the results obtained.

## **5 Conclusion**

Given the comparison made previously and the results obtained along the work, including a merit figure of more than one thousand, we can say that the objectives for this laboratory assignment were achieved and an Audio Amplifier circuit was built successfully.