

# Estatística 1

## Segunda lista de exercício

a) Estimar um modelo preliminar e apresentar os resultados;

```
> load("c:/Users/bruno/Documents/Facul/lista2/imoveiscwbav.RData")
> gc()
      used (Mb) gc trigger (Mb) max used (Mb)
Ncells 499840 26.7   1108625 59.3   638977 34.2
Vcells 778866  6.0    8388608 64.0  1631704 12.5
> resultados <- lm(price~age+parea+tarea+bath+ensuit+garag+plaz+park+
+                  trans+kidca+school+health+bike+barb+balc+elev+
+                  fitg+party+categ,data=imoveiscwbav)
>
>
> summary (resultados)
```

Call:

```
lm(formula = price ~ age + parea + tarea + bath + ensuit + garag +
    plaz + park + trans + kidca + school + health + bike + barb +
    balc + elev + fitg + party + categ, data = imoveiscwbav)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-495718	-134211	-2632	104528	2419265

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-420453.5	130052.5	-3.233	0.0013	**
age	-7839.1	1025.3	-7.645	1.01e-13	***
parea	2592.2	624.0	4.154	3.82e-05	***
tarea	1975.8	333.9	5.918	5.91e-09	***
bath	13452.6	14832.9	0.907	0.3649	
ensuit	125949.6	18560.7	6.786	3.15e-11	***
garag	169687.5	21756.1	7.800	3.41e-14	***
plaz	224393.0	94219.1	2.382	0.0176	*
park	-63439.6	27154.0	-2.336	0.0199	*
trans	26642.3	22718.5	1.173	0.2414	
kidca	10452.8	34899.8	0.300	0.7647	
school	-7975.8	56635.7	-0.141	0.8881	
health	1217.4	56216.5	0.022	0.9827	
bike	-85864.4	56073.0	-1.531	0.1263	
barb	-43925.7	22602.3	-1.943	0.0525	.
balc	65144.8	25242.3	2.581	0.0101	*
elev	-111743.4	25295.0	-4.418	1.21e-05	***
fitg	123052.7	28456.0	4.324	1.83e-05	***
party	36463.1	28481.1	1.280	0.2010	
categ	283061.5	55653.0	5.086	5.11e-07	***

---  
 signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 229400 on 521 degrees of freedom  
 Multiple R-squared: 0.8099, Adjusted R-squared: 0.803  
 F-statistic: 116.8 on 19 and 521 DF, p-value: < 2.2e-16

Carreguei a base e criei o modelo.

## b) Testar as variáveis para formulação do modelo;

### Teste Age

```
> formBase<-formula(price~parea+tarea+bath+ensuit+garag+plaz+park+
+                    trans+kidca+school+health+bike+barb+balc+elev+
+                    fitg+party+categ)
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-559997 -135850  -7282   108797 2360349

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -593909.9   134921.3  -4.402 1.30e-05 ***
parea         1643.3     644.3    2.550 0.011042 *
tarea         2396.9     346.9    6.909 1.43e-11 ***
bath        -8495.5    15332.4   -0.554 0.579756
ensuit       172325.9   18481.5    9.324 < 2e-16 ***
garag       215693.1    22027.9    9.792 < 2e-16 ***
plaz        250882.7    99201.5    2.529 0.011732 *
park       -51641.8    28563.1   -1.808 0.071183 .
trans       36393.6    23898.3    1.523 0.128401
kidca        4784.5    36762.0    0.130 0.896500
school      -2905.4    59667.0   -0.049 0.961182
health      35316.9    59042.6    0.598 0.549993
bike     -132282.7    58730.9   -2.252 0.024715 *
barb       -21661.4    23615.2   -0.917 0.359427
balc        91190.0    26351.8    3.460 0.000583 ***
elev       -91613.1    26505.9   -3.456 0.000592 ***
fitg       140020.5    29889.7    4.685 3.58e-06 ***
party       34036.1    30005.6    1.134 0.257178
categ       225297.9    58092.8    3.878 0.000119 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 241700 on 522 degrees of freedom
Multiple R-squared:  0.7886,    Adjusted R-squared:  0.7813
F-statistic: 108.2 on 18 and 522 DF,  p-value: < 2.2e-16

>
> Panjenage<-fform(imoveiscwbav,"age",formBase)
            AIC      BIC ranking (BIC)
smoothing 14879.74 14977.41           1
x^2        14897.14 14987.30           2
log(x)     14901.06 14991.22           3
x          14912.25 15002.42           4
x+x^2      14943.68 15033.85           5
sqr(x)     14944.35 15034.51           6
1/x        14957.80 15047.96           7
base       14967.78 15053.65           8
[1] "Smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
```

## Decisão: Incluir Age

```
> formBase<-formula(price~age+tarea+bath+ensuit+garag+plaz+park+
+                    trans+kidca+school+health+bike+barb+balc+elev+
+                    fitg+party+categ)
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-536220 -128848   1494   108580 2420400

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -345157.5   130773.1   -2.639  0.00855 **
age          -6991.9     1020.4   -6.852 2.06e-11 ***
tarea        2853.5       262.5   10.870 < 2e-16 ***
bath         23570.7    14857.7    1.586  0.11325
ensuit       139534.2   18552.6    7.521 2.39e-13 ***
garag        180717.9   21927.1    8.242 1.38e-15 ***
plaz         225240.4   95674.8    2.354  0.01893 *
park        -56223.2   27517.1   -2.043  0.04153 *
trans         41171.8   22794.5    1.806  0.07146 .
kidca         9002.4    35437.3    0.254  0.79957
school       23779.1    56984.6    0.417  0.67664
health        3818.0    57081.6    0.067  0.94670
bike       -105147.8   56744.0   -1.853  0.06444 .
barb        -41841.0   22945.9   -1.823  0.06881 .
balc         67611.1   25625.3    2.638  0.00858 **
elev       -110314.7   25683.5   -4.295 2.08e-05 ***
fitg         116193.4   28847.0    4.028 6.46e-05 ***
party        35352.9   28919.9    1.222  0.22209
categ        225210.7   54715.0    4.116 4.48e-05 ***
---
signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 232900 on 522 degrees of freedom
Multiple R-squared:  0.8036,    Adjusted R-squared:  0.7968
F-statistic: 118.7 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJenparea<-fform(imoveiscwbav,"parea",formBase)
              AIC      BIC ranking (BIC)
sqr(x)      14904.77 14994.94           1
x+x^2       14904.80 14994.96           2
x           14912.25 15002.42           3
smoothing   14881.96 15002.43           4
x^2         14916.70 15006.87           5
log(x)      14921.03 15011.19           6
base        14927.88 15013.75           7
1/x         14929.78 15019.94           8
[1] "Smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
> |
```

## Teste Parea

```

> formBase<-formula(price~age+taarea+bath+ensuit+garag+plaz+park+
+                    trans+kidca+school+health+bike+barb+balc+elev+
+                    fitg+party+categ)
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-536220 -128848   1494  108580 2420400

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -345157.5   130773.1   -2.639  0.00855 **
age          -6991.9     1020.4   -6.852 2.06e-11 ***
taarea       2853.5       262.5   10.870 < 2e-16 ***
bath         23570.7    14857.7    1.586  0.11325
ensuit      139534.2    18552.6    7.521 2.39e-13 ***
garag       180717.9    21927.1    8.242 1.38e-15 ***
plaz        225240.4    95674.8    2.354  0.01893 *
park        -56223.2    27517.1   -2.043  0.04153 *
trans       41171.8     22794.5    1.806  0.07146 .
kidca       9002.4      35437.3    0.254  0.79957
school     23779.1     56984.6    0.417  0.67664
health      3818.0      57081.6    0.067  0.94670
bike       -105147.8    56744.0   -1.853  0.06444 .
barb       -41841.0    22945.9   -1.823  0.06881 .
balc        67611.1    25625.3    2.638  0.00858 **
elev      -110314.7    25683.5   -4.295 2.08e-05 ***
fitg        116193.4    28847.0    4.028 6.46e-05 ***
party       35352.9     28919.9    1.222  0.22209
categ      225210.7     54715.0    4.116 4.48e-05 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 232900 on 522 degrees of freedom
Multiple R-squared:  0.8036,    Adjusted R-squared:  0.7968
F-statistic: 118.7 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJenparea<-fform(imoveiscwbav,"parea",formBase)
              AIC      BIC ranking (BIC)
sqr(x)      14904.77 14994.94           1
x+x^2       14904.80 14994.96           2
x           14912.25 15002.42           3
smoothing   14881.96 15002.43           4
x^2         14916.70 15006.87           5
log(x)      14921.03 15011.19           6
base        14927.88 15013.75           7
1/x         14929.78 15019.94           8
[1] "Smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
>

```

## Decisão: Incluir Parea

## Teste Tarea

```
> formBase<-formula(price~age+parea+bath+ensuit+garag+plaz+park+
+                   trans+kidca+school+health+bike+barb+balc+elev+
+                   fitg+party+categ)
>
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-473778 -125283  -4964    95015  2459849

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -425254.9   134221.1   -3.168  0.00162 **
age          -8840.2     1043.7    -8.470  2.51e-16 ***
parea         4929.2       498.7     9.885  < 2e-16 ***
bath         22083.6     15234.5     1.450  0.14778
ensuit       122215.9    19144.9     6.384  3.82e-10 ***
garag       195599.8     21994.5     8.893  < 2e-16 ***
plaz        215182.2     97227.8     2.213  0.02732 *
park       -75332.0     27948.1    -2.695  0.00726 **
trans       19109.4     23410.3     0.816  0.41471
kidca       26619.7     35908.7     0.741  0.45884
school     -24685.9     58379.6    -0.423  0.67258
health     -7441.8      57999.9    -0.128  0.89796
bike      -74259.7     57836.1    -1.284  0.19972
barb     -44110.9     23327.2    -1.891  0.05918 .
balc       62890.8     26049.0     2.414  0.01611 *
elev     -119874.1     26067.8    -4.599  5.34e-06 ***
fitg       122237.3     29368.3     4.162  3.69e-05 ***
party       45371.6     29353.5     1.546  0.12278
categ      339852.4     56577.6     6.007  3.55e-09 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 236800 on 522 degrees of freedom
Multiple R-squared:  0.7971,    Adjusted R-squared:  0.7901
F-statistic: 113.9 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJentarea<-fform(imoveiscwbav,"tarea",formBase)
      AIC      BIC ranking (BIC)
smoothing 14863.46 14963.98          1
sqr(x)    14886.91 14977.07          2
x+x^2     14886.96 14977.12          3
x         14912.25 15002.42          4
x^2       14925.17 15015.33          5
log(x)    14935.80 15025.96          6
base      14945.45 15031.32          7
1/x       14947.12 15037.28          8
[1] "Smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
~|
```

Decisão: Incluir Tarea

## Teste Plaz

```
> formBase<-formula(price~age+parea+tarea+bath+ensuit+garag+park+
+                   trans+kidca+school+health+bike+barb+balc+elev+
+                   fitg+party+categ)
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-487535 -137496  -4432   108110 2436449

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -445551.8   130203.6   -3.422  0.00067 ***
age          -7928.9     1029.2   -7.704  6.69e-14 ***
parea        2595.4       626.8    4.141  4.04e-05 ***
tarea        1962.7       335.3    5.853  8.53e-09 ***
bath         14915.5     14886.4    1.002  0.31683
ensuit       123964.4     18624.7    6.656  7.14e-11 ***
garag       170152.7     21852.4    7.786  3.73e-14 ***
park        -42810.2     25850.3   -1.656  0.09831 .
trans       29699.8     22783.5    1.304  0.19296
kidca        5371.1     34990.1    0.154  0.87806
school       32969.5     54204.2    0.608  0.54329
health       4238.3     56453.1    0.075  0.94018
bike        -67380.9     55781.3   -1.208  0.22761
barb        -49106.4     22597.8   -2.173  0.03022 *
balc         67618.0     25333.6    2.669  0.00784 **
elev       -116076.3     25342.2   -4.580  5.81e-06 ***
fitg        121377.1     28574.3    4.248  2.56e-05 ***
party       39742.0     28574.8    1.391  0.16488
categ       294370.6     55697.6    5.285  1.85e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 230400 on 522 degrees of freedom
Multiple R-squared:  0.8078,    Adjusted R-squared:  0.8012
F-statistic: 121.9 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJenPlaz<-fform(imoveiscwbav,"plaz",formBase)
            AIC      BIC ranking (BIC)
log(x)      14910.84 15001.00           1
x^2          14911.34 15001.50           2
base         14916.11 15001.98           3
x            14912.25 15002.42           4
x+x^2        14912.90 15003.06           5
sqr(x)       14914.25 15004.41           6
1/x          14915.88 15006.04           7
smoothing    14904.11 15015.66           8
[1] "smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
```

Decisão: Não incluir Plaz

## Teste Park

```

> formBase<-formula(price~age+parea+tarea+bath+ensuit+garag+plaz+
+                   trans+kidca+school+health+bike+barb+balc+elev+
+                   fitg+party+categ)
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-485013 -143277 -12614  107799 2401659

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -619461.9   98692.8  -6.277 7.28e-10 ***
age          -7703.0    1028.1   -7.493 2.90e-13 ***
parea         2498.9     625.4    3.996 7.37e-05 ***
tarea        2033.5      334.4    6.082 2.30e-09 ***
bath         15777.2   14862.6    1.062 0.28894
ensuit       121628.3   18547.0    6.558 1.31e-10 ***
garag       173458.1   21788.6    7.961 1.07e-14 ***
plaz       154175.0   89677.3    1.719 0.08617 .
trans       52060.7   20028.9    2.599 0.00961 **
kidca       11610.9   35045.0    0.331 0.74054
school      55960.3   49796.4    1.124 0.26162
health     -10386.0   56235.3   -0.185 0.85354
bike      -133014.7   52538.1   -2.532 0.01164 *
barb      -42641.7   22691.9   -1.879 0.06078 .
balc       70770.2   25234.3    2.805 0.00523 **
elev     -112024.2   25402.5   -4.410 1.26e-05 ***
fitg       121885.1   28572.8    4.266 2.37e-05 ***
party       36010.5   28601.8    1.259 0.20858
categ      313021.2   54386.2    5.756 1.47e-08 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 230400 on 522 degrees of freedom
Multiple R-squared:  0.8079,    Adjusted R-squared:  0.8013
F-statistic: 122 on 18 and 522 DF,  p-value: < 2.2e-16

> PanJenpark<-fform(imoveiscwbav,"park",formBase)
      AIC      BIC ranking (BIC)
1/x      14905.25 14995.41         1
smoothing 14895.01 14995.66         2
log(x)    14906.77 14996.93         3
x^2       14909.76 14999.92         4
base      14915.89 15001.76         5
x         14912.25 15002.42         6
x+x^2     14914.73 15004.89         7
sqr(x)    14915.32 15005.48         8
[1] "Smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"

```



## Decisão: Incluir Park

## Teste Trans

```
> formBase<-formula(price~age+parea+tarea+bath+ensuit+garag+plaz+park+
+ kidca+school+health+bike+barb+balc+elev+
+ fitg+party+categ)
>
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-499136 -132980  -5716   104035 2418690

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -357200.0   118382.6  -3.017  0.00267 **
age          -7906.6     1024.1   -7.721 5.95e-14 ***
parea         2704.9       616.8    4.385 1.40e-05 ***
tarea        1953.9       333.5    5.859 8.24e-09 ***
bath         13235.2     14837.1    0.892  0.37279
ensuit       124875.6    18544.7    6.734 4.37e-11 ***
garag       170325.1     21757.1    7.828 2.77e-14 ***
plaz        230636.8     94102.4    2.451  0.01458 *
park       -78689.5     23846.3   -3.300  0.00103 **
kidca       25866.4     32341.9    0.800  0.42420
school     -21418.6     55483.5   -0.386  0.69963
health      10519.7     55674.0    0.189  0.85020
bike       -77781.5     55667.8   -1.397  0.16293
barb      -46944.8     22463.3   -2.090  0.03711 *
balc        64635.0     25247.6    2.560  0.01075 *
elev     -109777.7     25248.5   -4.348 1.65e-05 ***
fitg       119703.0     28322.4    4.226 2.80e-05 ***
party       35384.5     28476.4    1.243  0.21458
categ      271600.5     54807.8    4.956 9.76e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 229500 on 522 degrees of freedom
Multiple R-squared:  0.8094,    Adjusted R-squared:  0.8028
F-statistic: 123.2 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJentrans<-fform(imoveiscwbav,"trans",formBase)
      AIC      BIC ranking (BIC)
1/x      14906.86 14997.02         1
base      14911.68 14997.55         2
log(x)     14910.50 15000.66         3
x^2        14911.49 15001.65         4
smoothing  14901.64 15001.97         5
x          14912.25 15002.42         6
x+x^2      14912.98 15003.14         7
sqr(x)     14913.14 15003.31         8
[1] "Smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
```

Decisão: Não incluir Trans

## Teste Kidca

```
> formBase<-formula(price~age+parea+taarea+bath+ensuit+garag+plaz+park+
+                    trans+school+health+bike+barb+balc+elev+
+                    fitg+party+categ)
>
> summary(lm(formBase, data=imoveiscwbav))

call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-502179 -133678  -1484   105125 2419604

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -414146.4   128224.3   -3.230  0.00132 **
age          -7832.6     1024.2   -7.647  9.94e-14 ***
parea        2590.3       623.4    4.155  3.80e-05 ***
taarea       1983.6       332.6    5.965  4.52e-09 ***
bath         13727.7     14791.5    0.928  0.35380
ensuit       126023.1     18542.8    6.796  2.94e-11 ***
garag        169361.9     21710.0    7.801  3.36e-14 ***
plaz         222667.7     93960.8    2.370  0.01816 *
park        -63555.1     27127.6   -2.343  0.01951 *
trans        29204.9     21027.5    1.389  0.16546
school      -8130.1      56584.0   -0.144  0.88581
health      -3562.0      53857.1   -0.066  0.94729
bike        -82185.7     54663.6   -1.503  0.13332
barb        -43846.3     22581.0   -1.942  0.05271 .
balc         64650.0     25166.2    2.569  0.01048 *
elev       -111936.0     25264.8   -4.431  1.15e-05 ***
fitg         123800.3     28321.5    4.371  1.49e-05 ***
party        36872.0     28423.5    1.297  0.19512
categ       285093.1     55189.8    5.166  3.41e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 229200 on 522 degrees of freedom
Multiple R-squared:  0.8099,    Adjusted R-squared:  0.8033
F-statistic: 123.5 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJenkidca<-fform(imoveiscwbav,"kidca",formBase)
      AIC      BIC ranking (BIC)
base    14910.35 14996.22         1
log(x)   14912.07 15002.23         2
x^2      14912.13 15002.29         3
x        14912.25 15002.42         4
sqr(x)   14912.32 15002.48         5
1/x      14912.34 15002.50         6
x+x^2    14912.35 15002.51         7
smoothing 14887.98 15005.85         8
[1] "smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
```

Decisão: Não incluir Kidca

## Teste School

```
> formBase<-formula(price~age+parea+tarea+bath+ensuit+garag+plaz+park+
+                    trans+kidca+health+bike+barb+balc+elev+
+                    fitg+party+categ)
>
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-496324 -134050  -1325   103641 2419050

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -430263.7   109719.3   -3.921 9.97e-05 ***
age          -7837.4     1024.3    -7.651 9.66e-14 ***
parea        2580.4       617.7     4.177 3.46e-05 ***
tarea        1978.2       333.1     5.938 5.27e-09 ***
bath         13506.2    14814.1     0.912 0.36234
ensuit       126058.6    18527.1     6.804 2.80e-11 ***
garag       169846.7    21706.3     7.825 2.84e-14 ***
plaz        220365.2    89688.8     2.457 0.01433 *
park        -61591.8    23751.2    -2.593 0.00978 **
trans       27289.8     22227.4     1.228 0.22009
kidca       10497.5     34865.6     0.301 0.76347
health       3229.0     54320.3     0.059 0.95262
bike       -87242.5     55160.7    -1.582 0.11435
barb       -43472.0     22350.6    -1.945 0.05231 .
balc        65403.6     25151.7     2.600 0.00958 **
elev      -111690.8     25268.5    -4.420 1.20e-05 ***
fitg        122548.0    28202.9     4.345 1.67e-05 ***
party       36431.2     28453.4     1.280 0.20098
categ       284684.4     54395.5     5.234 2.41e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 229200 on 522 degrees of freedom
Multiple R-squared:  0.8099,    Adjusted R-squared:  0.8033
F-statistic: 123.6 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJenschool<-fform(imoveiscwbav,"school",formBase)
      AIC      BIC ranking (BIC)
base    14910.28 14996.14         1
1/x      14908.59 14998.75         2
log(x)   14912.09 15002.26         3
x^2      14912.21 15002.38         4
x        14912.25 15002.42         5
x+x^2    14912.27 15002.43         6
sqr(x)   14912.27 15002.44         7
smoothing 14902.71 15024.09         8
[1] "Smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
```

Decisão: Não incluir School

## Teste Heath

```
> formBase<-formula(price~age+parea+taea+bath+ensuit+garag+plaz+park+
+                   trans+kidca+school+bike+barb+balc+elev+
+                   fitg+party+categ)
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-495906 -134106  -2849   104632 2419065

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -419586.4   123616.3   -3.394  0.00074 ***
age          -7840.9     1021.1    -7.679  7.99e-14 ***
parea         2592.4       623.4     4.159  3.74e-05 ***
taea          1975.6       333.4     5.925  5.67e-09 ***
bath          13448.6    14817.6     0.908  0.36450
ensuit       125913.1    18466.1     6.819  2.55e-11 ***
garag       169707.3    21716.0     7.815  3.05e-14 ***
plaz        224439.0    94104.9     2.385  0.01744 *
park        -63387.7    27021.9    -2.346  0.01936 *
trans        26711.7    22469.7     1.189  0.23506
kidca       10238.3     33432.2     0.306  0.75954
school      -8287.5     54724.4    -0.151  0.87969
bike        -85972.2    55798.1    -1.541  0.12398
barb        -43910.8    22570.1    -1.946  0.05225 .
balc         65104.2    25148.2     2.589  0.00990 **
elev       -111748.8    25269.6    -4.422  1.19e-05 ***
fitg        123050.8    28428.6     4.328  1.80e-05 ***
party       36511.1     28367.5     1.287  0.19864
categ       283006.2    55541.1     5.095  4.87e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 229200 on 522 degrees of freedom
Multiple R-squared:  0.8099,    Adjusted R-squared:  0.8034
F-statistic: 123.6 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJenhealth<-fform(imoveiscwbav,"health",formBase)
            AIC          BIC ranking (BIC)
base      14910.26 14996.12             1.0
1/x       14911.26 15001.42             2.0
sqr(x)    14912.08 15002.24             3.0
x+x^2     14912.21 15002.37             4.5
log(x)    14912.21 15002.37             4.5
x^2       14912.23 15002.39             6.0
x         14912.25 15002.42             7.0
smoothing 14911.60 15004.47             8.0
[1] "smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
```

Decisão: Não incluir Heath

## Teste Bike

```
> formBase<-formula(price~age+parea+tarea+bath+ensuit+garag+plaz+park+
+                    trans+kidca+school+health+barb+balc+elev+
+                    fitg+party+categ)
>
> summary(lm(formBase, data=imoveiscwbav))

Call:
lm(formula = formBase, data = imoveiscwbav)

Residuals:
    Min       1Q   Median       3Q      Max
-510703 -134525      33  104312 2420136

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -399412.6   129491.1  -3.084  0.00215 **
age          -8009.1     1020.6   -7.847 2.42e-14 ***
parea         2671.3      622.7    4.290 2.13e-05 ***
tarea         1957.9      334.1    5.860 8.19e-09 ***
bath         14345.4     14840.5    0.967  0.33418
ensuit       126035.0     18584.5    6.782 3.22e-11 ***
garag       168530.2     21771.0    7.741 5.15e-14 ***
plaz        204424.0     93432.4    2.188  0.02912 *
park       -78405.3     25366.9   -3.091  0.00210 **
trans       22366.0     22575.3    0.991  0.32228
kidca       -1253.1     34096.2   -0.037  0.97070
school     -23111.0     55838.4   -0.414  0.67912
health       8860.3     56066.6    0.158  0.87449
barb      -50094.9     22269.0   -2.250  0.02489 *
balc        64100.9     25265.6    2.537  0.01147 *
elev     -113025.0     25313.7   -4.465 9.82e-06 ***
fitg       125879.2     28432.6    4.427 1.16e-05 ***
party       34485.7     28488.4    1.211  0.22663
categ      288705.2     55602.3    5.192 2.98e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 229700 on 522 degrees of freedom
Multiple R-squared:  0.8091,    Adjusted R-squared:  0.8025
F-statistic: 122.9 on 18 and 522 DF,  p-value: < 2.2e-16

>
> PanJenbike<-fform(imoveiscwbav,"bike",formBase)
      AIC      BIC ranking (BIC)
base    14912.68 14998.55         1
log(x)   14910.52 15000.68         2
x^2      14911.06 15001.22         3
x        14912.25 15002.42         4
x+x^2    14912.97 15003.13         5
sqr(x)   14913.65 15003.82         6
1/x      14914.12 15004.28         7
smoothing 14909.28 15007.97         8
[1] "Smoothing is a semi-parametric and data-driven transformation, please see wood (2006) for an elaboration"
> |
```

Decisão: Não incluir Bike

Resultado

```

> imoveiscwbav$age <- (imoveiscwbav$age^2)
> imoveiscwbav$parea <- sqrt(imoveiscwbav$parea)
> imoveiscwbav$tarea <- sqrt(imoveiscwbav$tarea)
> imoveiscwbav$plaz <- log(imoveiscwbav$plaz)
> imoveiscwbav$park <- 1/(imoveiscwbav$park)
> imoveiscwbav$trans <- 1/(imoveiscwbav$trans)
>
>
> save(imoveiscwbav, file="imoveiscwbav1.RData" )
> resultados <- lm(price~age+parea+tarea+bath+ensuit+garag+plaz+park+
+                  trans+kidca+school+health+bike+barb+balc+elev+
+                  fitg+party+categ,data=imoveiscwbav)
>
>
> summary (resultados)

```

Call:

```
lm(formula = price ~ age + parea + tarea + bath + ensuit + garag +
    plaz + park + trans + kidca + school + health + bike + barb +
    balc + elev + fitg + party + categ, data = imoveiscwbav)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-575422	-132235	-1347	98967	2408789

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-1011256.2	141686.1	-7.137	3.21e-12	***
age	-129.3	25.3	-5.110	4.54e-07	***
parea	46751.5	14519.8	3.220	0.00136	**
tarea	55178.0	9758.0	5.655	2.58e-08	***
bath	4079.9	15284.1	0.267	0.78962	
ensuit	153095.5	18852.5	8.121	3.37e-15	***
garag	184403.4	22478.4	8.204	1.84e-15	***
plaz	53988.2	18080.8	2.986	0.00296	**
park	190747.3	50923.4	3.746	0.00020	***
trans	-89961.3	44710.8	-2.012	0.04473	*
kidca	-27557.6	37516.0	-0.735	0.46294	
school	-67472.8	62015.7	-1.088	0.27710	
health	16456.8	57633.3	0.286	0.77534	
bike	-45288.4	61323.6	-0.739	0.46053	
barb	-36985.5	23387.1	-1.581	0.11438	
balc	79093.6	25959.3	3.047	0.00243	**
elev	-106901.9	26176.1	-4.084	5.12e-05	***
fitg	139061.0	29377.3	4.734	2.85e-06	***
party	23647.6	29530.0	0.801	0.42361	
categ	259957.1	56205.5	4.625	4.73e-06	***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 237200 on 521 degrees of freedom

Multiple R-squared: 0.7967, Adjusted R-squared: 0.7893

F-statistic: 107.5 on 19 and 521 DF, p-value: < 2.2e-16

c) Verifique a presença de outliers;

```
> outlierTest(resultados)
      rstudent unadjusted p-value Bonferroni p
393 11.549391      1.2643e-27    6.8401e-25
13   4.413506      1.2374e-05    6.6942e-03
```

d) Teste a especificação do modelo e altere se necessário;

```
> resettest(price~age+parea+tarea+bath+ensuit+garag+plaz+park+
+ trans+kidca+school+health+bike+barb+balc+elev+
+ fitg+party+categ,power=2:3,type="regressor", data=imoveiscwbav)

RESET test

data: price ~ age + parea + tarea + bath + ensuit + garag + plaz + park + trans + kidca + school + health + bike + barb + balc + elev + fitg + party + categ
RESET = 5.2815, df1 = 38, df2 = 483, p-value < 2.2e-16

>
>
> # F tabelado:
>
> qf(0.95, df1=38, df2=483)
[1] 1.429987
```

Como o F calculado (5.2815) é maior que o F tabelado (1,429987), existe erro de especificação do modelo

e) Teste a presença de multicolinearidade e exclua variáveis se necessário;

```
> cor(imoveiscwbav[,c("age", "parea", "tarea", "bath", "ensuit", "garag", "plaz", "park",
+ "trans", "kidca", "school", "health", "bike")],
+ use="complete")
      age      parea      tarea      bath      ensuit      garag      plaz      park      trans
age  1.000000000 -0.23698282 -0.31657436 -0.26037524 -0.41131287 -0.448491700  0.007897195  0.04544181 -0.05481368
parea -0.236982819  1.00000000  0.83631214  0.68030305  0.59703635  0.603548940 -0.103245172  0.21597209 -0.24465672
tarea -0.316574355  0.83631214  1.00000000  0.65178059  0.56702436  0.645854936 -0.137222512  0.21515484 -0.20718875
bath -0.260375235  0.68030305  0.65178059  1.00000000  0.73616242  0.574197743 -0.112992339  0.18807029 -0.16147897
ensuit -0.411312872  0.59703635  0.56702436  0.73616242  1.00000000  0.531151588 -0.083877169  0.04924212 -0.04513610
garag -0.448491700  0.60354894  0.64585494  0.57419774  0.53115159  1.000000000 -0.080390991  0.15699883 -0.13018970
plaz  0.007897195 -0.10324517 -0.13722251 -0.11299234 -0.08387717 -0.080390991  1.000000000 -0.32462706  0.01029101
park  0.045441811  0.21597209  0.21515484  0.18807029  0.04924212  0.156998830 -0.324627059  1.00000000 -0.29767701
trans -0.054813684 -0.24465672 -0.20718875 -0.16147897 -0.04513610 -0.130189703  0.010291011 -0.29767701  1.00000000
kidca -0.007034162  0.23719013  0.26214005  0.23256465  0.15681143  0.131592614 -0.100390573  0.29848179 -0.50283754
school 0.096298011  0.15219562  0.09328829  0.07286173  0.02216520  0.005902974  0.160404566  0.46081487 -0.11388155
health -0.097090851 -0.12890024 -0.13439880 -0.14426728 -0.12274559 -0.022402611  0.009381361 -0.24700544  0.15173518
bike  0.070154638 -0.06615144 -0.06336755 -0.06967850 -0.05244026 -0.068895267  0.222888734 -0.38994669 -0.08404754
      kidca      school      health      bike
age -0.007034162  0.096298011 -0.097090851  0.07015464
parea 0.237190133  0.152195617 -0.128900236 -0.06615144
tarea 0.262140051  0.093288289 -0.134398800 -0.06336755
bath 0.232564655  0.072861730 -0.144267282 -0.06967850
ensuit 0.156811432  0.022165200 -0.122745589 -0.05244026
garag 0.131592614  0.005902974 -0.022402611 -0.06889527
plaz -0.100390573  0.160404566  0.009381361  0.22288873
park 0.298481791  0.460814867 -0.247005445 -0.38994669
trans -0.502837545 -0.113881554  0.151735185 -0.08404754
kidca 1.000000000  0.146596839 -0.349252096  0.18358136
school 0.146596839  1.000000000 -0.373524820  0.07078386
health -0.349252096 -0.373524820  1.000000000 -0.11611012
bike 0.183581360  0.070783858 -0.116110122  1.000000000
> library(car)
> vif(lm(price~age+parea+tarea+bath+ensuit+garag+plaz+park+trans+kidca+school+health+bike,data=imoveiscwbav), type="high-order")
```



Parece que o pareia e tarea são correlacionadas pela matriz de correlação. Pelo valor de inflação de variancia nota-se que que o pareia e o tarea tem score alto, quase atingindo valor quatro, então estão consideravelmente correlacionados, a sugestão é excluir o tarea. mas serão feitas exclusões após o stepwise.

## f) Selecione um modelo pela técnica de stepwise;

```
> resultados <- lm(price~age+pareia+tarea+bath+ensuit+garag+plaz+park+trans+kidca+school+health+bike+barb+balc+elev+
+               fitg+party+categ,
+               data=imoveiscwbav)
> summary (resultados)
```

Call:  
lm(formula = price ~ age + pareia + tarea + bath + ensuit + garag + plaz + park + trans + kidca + school + health + bike + barb + balc + elev + fitg + party + categ, data = imoveiscwbav)

Residuals:

	Min	1Q	Median	3Q	Max
	-575422	-132235	-1347	98967	2408789

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-1011256.2	141686.1	-7.137	3.21e-12	***
age	-129.3	25.3	-5.110	4.54e-07	***
pareia	46751.5	14519.8	3.220	0.00136	**
tarea	55178.0	9758.0	5.655	2.58e-08	***
bath	4079.9	15284.1	0.267	0.78962	
ensuit	153095.5	18852.5	8.121	3.37e-15	***
garag	184403.4	22478.4	8.204	1.84e-15	***
plaz	53988.2	18080.8	2.986	0.00296	**
park	190747.3	50923.4	3.746	0.00020	***
trans	-89961.3	44710.8	-2.012	0.04473	*
kidca	-27557.6	37516.0	-0.735	0.46294	
school	-67472.8	62015.7	-1.088	0.27710	
health	16456.8	57633.3	0.286	0.77534	
bike	-45288.4	61323.6	-0.739	0.46053	
barb	-36985.5	23387.1	-1.581	0.11438	
balc	79093.6	25959.3	3.047	0.00243	**
elev	-106901.9	26176.1	-4.084	5.12e-05	***
fitg	139061.0	29377.3	4.734	2.85e-06	***
party	23647.6	29530.0	0.801	0.42361	
categ	259957.1	56205.5	4.625	4.73e-06	***

---  
signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 237200 on 521 degrees of freedom  
Multiple R-squared: 0.7967, Adjusted R-squared: 0.7893  
F-statistic: 107.5 on 19 and 521 DF, p-value: < 2.2e-16

```
> step <- stepwise(resultados, direction= 'backward/forward', criterion ='AIC')
```

```
Direction: backward/forward
```

```
Criterion: AIC
```

```
Start: AIC=13411.33
```

```
price ~ age + parea + tarea + bath + ensuit + garag + plaz +  
      park + trans + kidca + school + health + bike + barb + balc +  
      elev + fitg + party + categ
```

	Df	Sum of Sq	RSS	AIC
- bath	1	4.0103e+09	2.9326e+13	13409
- health	1	4.5889e+09	2.9327e+13	13409
- kidca	1	3.0367e+10	2.9353e+13	13410
- bike	1	3.0696e+10	2.9353e+13	13410
- party	1	3.6092e+10	2.9358e+13	13410
- school	1	6.6621e+10	2.9389e+13	13411
<none>			2.9322e+13	13411
- barb	1	1.4076e+11	2.9463e+13	13412
- trans	1	2.2785e+11	2.9550e+13	13414
- plaz	1	5.0179e+11	2.9824e+13	13418
- balc	1	5.2246e+11	2.9845e+13	13419
- parea	1	5.8349e+11	2.9906e+13	13420
- park	1	7.8966e+11	3.0112e+13	13424
- elev	1	9.3869e+11	3.0261e+13	13426
- categ	1	1.2039e+12	3.0526e+13	13431
- fitg	1	1.2611e+12	3.0583e+13	13432
- age	1	1.4693e+12	3.0792e+13	13436
- tarea	1	1.7996e+12	3.1122e+13	13442
- ensuit	1	3.7115e+12	3.3034e+13	13474
- garag	1	3.7876e+12	3.3110e+13	13475

```
Step: AIC=13409.4
```

```
price ~ age + parea + tarea + ensuit + garag + plaz + park +  
      trans + kidca + school + health + bike + barb + balc + elev +  
      fitg + party + categ
```

	Df	Sum of Sq	RSS	AIC
- health	1	4.4490e+09	2.9331e+13	13408
- kidca	1	2.9571e+10	2.9356e+13	13408
- bike	1	3.1098e+10	2.9357e+13	13408
- party	1	3.8460e+10	2.9365e+13	13408
- school	1	6.7651e+10	2.9394e+13	13409
<none>			2.9326e+13	13409
- barb	1	1.3893e+11	2.9465e+13	13410
+ bath	1	4.0103e+09	2.9322e+13	13411
- trans	1	2.2931e+11	2.9556e+13	13412
- plaz	1	5.0337e+11	2.9830e+13	13417
- balc	1	5.2621e+11	2.9852e+13	13417
- parea	1	6.1896e+11	2.9945e+13	13419
- park	1	8.0168e+11	3.0128e+13	13422
- elev	1	9.3556e+11	3.0262e+13	13424
- categ	1	1.2047e+12	3.0531e+13	13429
- fitg	1	1.2589e+12	3.0585e+13	13430
- age	1	1.4838e+12	3.0810e+13	13434
- tarea	1	1.8270e+12	3.1153e+13	13440
- garag	1	3.8980e+12	3.3224e+13	13475
- ensuit	1	5.3272e+12	3.4653e+13	13498

Step: AIC=13407.48

price ~ age + parea + tarea + ensuit + garag + plaz + park +  
trans + kidca + school + bike + barb + balc + elev + fitg +  
party + categ

	Df	Sum of Sq	RSS	AIC
- bike	1	3.2891e+10	2.9364e+13	13406
- kidca	1	3.7660e+10	2.9368e+13	13406
- party	1	4.0511e+10	2.9371e+13	13406
- school	1	8.2675e+10	2.9413e+13	13407
<none>			2.9331e+13	13408
- barb	1	1.3826e+11	2.9469e+13	13408
+ health	1	4.4490e+09	2.9326e+13	13409
+ bath	1	3.8704e+09	2.9327e+13	13409
- trans	1	2.3217e+11	2.9563e+13	13410
- plaz	1	5.0507e+11	2.9836e+13	13415
- balc	1	5.2189e+11	2.9853e+13	13415
- parea	1	6.2309e+11	2.9954e+13	13417
- park	1	7.9895e+11	3.0130e+13	13420
- elev	1	9.3610e+11	3.0267e+13	13422
- categ	1	1.2004e+12	3.0531e+13	13427
- fitg	1	1.2575e+12	3.0588e+13	13428
- age	1	1.5159e+12	3.0847e+13	13433
- tarea	1	1.8227e+12	3.1153e+13	13438
- garag	1	3.9163e+12	3.3247e+13	13473
- ensuit	1	5.3684e+12	3.4699e+13	13496

Step: AIC=13406.09

price ~ age + parea + tarea + ensuit + garag + plaz + park +  
trans + kidca + school + barb + balc + elev + fitg + party +  
categ

	Df	Sum of Sq	RSS	AIC
- party	1	3.6727e+10	2.9400e+13	13405
- kidca	1	6.6838e+10	2.9430e+13	13405
<none>			2.9364e+13	13406
- school	1	1.3381e+11	2.9497e+13	13406
- barb	1	1.6076e+11	2.9524e+13	13407
+ bike	1	3.2891e+10	2.9331e+13	13408
+ health	1	6.2424e+09	2.9357e+13	13408
+ bath	1	4.2513e+09	2.9359e+13	13408
- trans	1	2.1733e+11	2.9581e+13	13408
- plaz	1	5.0627e+11	2.9870e+13	13413
- balc	1	5.1341e+11	2.9877e+13	13414
- parea	1	6.4815e+11	3.0012e+13	13416
- elev	1	9.4566e+11	3.0309e+13	13421
- categ	1	1.2264e+12	3.0590e+13	13426
- park	1	1.2947e+12	3.0658e+13	13427
- fitg	1	1.3032e+12	3.0667e+13	13428
- age	1	1.5804e+12	3.0944e+13	13432
- tarea	1	1.8139e+12	3.1177e+13	13436
- garag	1	3.8921e+12	3.3256e+13	13471
- ensuit	1	5.3953e+12	3.4759e+13	13495

Step: AIC=13404.77

price ~ age + parea + tarea + ensuit + garag + plaz + park +  
trans + kidca + school + barb + balc + elev + fitg + categ

	Df	Sum of Sq	RSS	AIC
- kidca	1	6.2555e+10	2.9463e+13	13404
<none>			2.9400e+13	13405
- school	1	1.3636e+11	2.9537e+13	13405
- barb	1	1.5616e+11	2.9556e+13	13406
+ party	1	3.6727e+10	2.9364e+13	13406
+ bike	1	2.9108e+10	2.9371e+13	13406
+ health	1	8.3752e+09	2.9392e+13	13407
+ bath	1	6.5661e+09	2.9394e+13	13407
- trans	1	2.1281e+11	2.9613e+13	13407
- plaz	1	5.3543e+11	2.9936e+13	13412
- balc	1	6.2350e+11	3.0024e+13	13414
- parea	1	6.5043e+11	3.0051e+13	13415
- elev	1	9.3541e+11	3.0336e+13	13420
- categ	1	1.2883e+12	3.0689e+13	13426
- park	1	1.2959e+12	3.0696e+13	13426
- age	1	1.5926e+12	3.0993e+13	13431
- fitg	1	1.7557e+12	3.1156e+13	13434
- tarea	1	1.8491e+12	3.1249e+13	13436
- garag	1	3.8819e+12	3.3282e+13	13470
- ensuit	1	5.3846e+12	3.4785e+13	13494

Step: AIC=13403.92

price ~ age + parea + tarea + ensuit + garag + plaz + park +  
trans + school + barb + balc + elev + fitg + categ

	Df	Sum of Sq	RSS	AIC
<none>			2.9463e+13	13404
- school	1	1.4668e+11	2.9610e+13	13405
- trans	1	1.5192e+11	2.9615e+13	13405
+ kidca	1	6.2555e+10	2.9400e+13	13405
+ bike	1	5.6072e+10	2.9407e+13	13405
- barb	1	1.6682e+11	2.9630e+13	13405
+ party	1	3.2445e+10	2.9430e+13	13405
+ health	1	2.4191e+10	2.9439e+13	13406
+ bath	1	4.8823e+09	2.9458e+13	13406
- plaz	1	5.5372e+11	3.0017e+13	13412
- balc	1	6.3695e+11	3.0100e+13	13414
- parea	1	6.5574e+11	3.0119e+13	13414
- elev	1	9.2837e+11	3.0391e+13	13419
- categ	1	1.2392e+12	3.0702e+13	13424
- park	1	1.2586e+12	3.0721e+13	13424
- age	1	1.6042e+12	3.1067e+13	13431
- fitg	1	1.7060e+12	3.1169e+13	13432
- tarea	1	1.8031e+12	3.1266e+13	13434
- garag	1	3.9794e+12	3.3442e+13	13470
- ensuit	1	5.3259e+12	3.4789e+13	13492

> step

Call:

```
lm(formula = price ~ age + parea + tarea + ensuit + garag + plaz +  
    park + trans + school + barb + balc + elev + fitg + categ,  
    data = imoveiscwbav)
```

```
call:
lm(formula = price ~ age + parea + tarea + ensuit + garag + plaz +
    park + trans + school + barb + balc + elev + fitg + categ,
    data = imoveiscwbav)

Coefficients:
(Intercept)      age      parea      tarea      ensuit      garag      plaz      park      trans
-1064753.1    -131.8    48645.0    54666.4    154017.8    186255.6    56407.1    207115.1    -64673.1
  school      barb      balc      elev      fitg      categ
  -91266.3   -39758.7   84156.9  -99341.2   147195.1   259282.7
```

## Melhor Modelo

```
> resultados <- lm(price ~ age + parea + tarea + ensuit + garag + plaz +
+                   park + trans + bike + barb + balc + elev + fitg + categ, data = imoveiscwbav)
> summary(resultados)
```

```
call:
lm(formula = price ~ age + parea + tarea + ensuit + garag + plaz +
    park + trans + bike + barb + balc + elev + fitg + categ,
    data = imoveiscwbav)
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-553655 -145325  -1028   106340  2394627
```

```
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.046e+06  1.252e+05  -8.352 5.98e-16 ***
age          -1.302e+02  2.476e+01  -5.258 2.12e-07 ***
parea        4.591e+04  1.420e+04   3.234 0.001297 **
tarea        5.525e+04  9.650e+03   5.725 1.74e-08 ***
ensuit       1.543e+05  1.580e+04   9.763 < 2e-16 ***
garag        1.894e+05  2.200e+04   8.610 < 2e-16 ***
plaz         4.858e+04  1.681e+04   2.889 0.004024 **
park         1.480e+05  3.955e+04   3.743 0.000202 ***
trans       -8.332e+04  3.999e+04  -2.084 0.037684 *
bike        -8.097e+04  5.513e+04  -1.469 0.142511
barb        -3.314e+04  2.316e+04  -1.431 0.153088
balc         8.671e+04  2.495e+04   3.475 0.000553 ***
elev       -9.766e+04  2.443e+04  -3.998 7.30e-05 ***
fitg         1.414e+05  2.640e+04   5.354 1.29e-07 ***
categ        2.699e+05  5.435e+04   4.966 9.26e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 236800 on 526 degrees of freedom
Multiple R-squared:  0.7955,    Adjusted R-squared:  0.7901
F-statistic: 146.2 on 14 and 526 Df, p-value: < 2.2e-16
```

g) Faça o teste de homocedasticidade e faça correção da heterocedasticidade se necessário;

H0 - homocedástico(variáveis constantes)

HA - Heterocedástico(variáveis não constantes)

## Breusch-Pagan

```
> bptest(price ~ age + parea + tarea + ensuit + garag + plaz +
+         park + trans + bike + barb + balc + elev + fitg + categ, studentize=FALSE, data=imoveiscwbav)
```

Breusch-Pagan test

```
data: price ~ age + parea + tarea + ensuit + garag + plaz + park + trans + bike + barb + balc + elev + fitg + categ
BP = 282.15, df = 14, p-value < 2.2e-16
```

## Qui-quadrático

```
> qchisq(0.95, df=14, lower.tail = TRUE)
[1] 23.68479
```

O valor de 290 está muito acima do tabelado, então rejeita-se a hipótese de homocedasticidade. Será feita regressão robusta.

```
> resultrob <- lmRob(price ~ age + pareo + tarea + ensuit + garagem + plaz +
+ park + trans + bike + barb + balc + elev + fitq + cateq, data=imoveiscwbav)
```

h) Obtenha os indicadores de desempenho do modelo;

```
> AIC(resultados)
[1] 14941.68
> BIC(resultados)
[1] 15010.38
> library(AICcmodavg)
> AICc(resultados)
[1] 14942.72
> library(performance)
> model_performance(resultados)
# Indices of model performance
```

AIC	BIC	R2	R2 (adj.)	RMSE	Sigma
14912.255	15002.416	0.810	0.803	2.251e+05	2.294e+05

```
> model_performance(resultrob)
# Indices of model performance
```

R2	RMSE	Sigma
0.791	2.363e+05	2.396e+05

i) Estime os intervalos de confiança para os parâmetros do modelo;

```
> confint(resultados, level = 0.95)
```

	2.5 %	97.5 %
(Intercept)	-1291817.4425	-799842.52225
age	-178.8353	-81.55662
parea	18022.3061	73795.65298
tarea	36288.4021	74202.61980
ensuit	123220.9512	185299.01289
garag	146177.6906	232606.90880
plaz	15544.6432	81607.73100
park	70328.3483	225731.71107
trans	-161872.4267	-4760.74702
bike	-189265.0873	27331.53781
barb	-78648.8733	12362.97252
balc	37691.7022	135723.22050
elev	-145646.3242	-49675.84270
fitg	89483.5383	193218.38150
categ	163122.9125	376665.68768

```
> confint(resultrob, level=0.95)
```

	2.5 %	97.5 %
(Intercept)	-647091.1924	-320777.322
age	-8746.0011	-5840.952
parea	1733.4274	3628.755
tarea	991.0716	2107.736
ensuit	108310.7009	160089.136
garag	113680.5160	179170.787
plaz	188620.6910	454926.198
park	-67028.1510	1928.786
trans	6647.7359	65755.211
bike	-176836.4768	-18368.795
barb	-42461.7478	26605.673
balc	17244.2960	91460.756
elev	-102680.7428	-27299.923
fitg	60802.5216	140534.528
categ	289785.2257	452885.540

j) Faça predição de um imóvel hipotético: apresente seus parâmetros de simulação e o resultado.

```
> ##### Fazendo predições no modelos OLS
> #Para:
> #age = 5 anos = 1.609438
> log(5)
[1] 1.609438
> #educ = 150 pareia = 5.010635
> log(150)
[1] 5.010635
> #earns = 190 tarea = 5.247024
> log(250)
[1] 5.521461
> # plaz
> log(0.08)
[1] -2.525729
> #kidlt6 = 1 --> tem filhos com menos de 6 anos

> predict(object = resultrob,
+         data.frame(age=1.60, pareia=5.01, tarea=5.24, ensuit = 1, garag = 1, plaz = -2.525729,
+         park = -2.525729, trans = -2.525729, bike = -2.525729, categ = 1,
+         barb=0, balc=0, elev=0, fitg=0))
      1
-397509.9
>
> #o salario por hora é:
> exp(14.11198)
[1] 1345101
>
> anova.lmrob(resultrob)
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left
00:00:00 left

Terms added sequentially (first to last)
```

	Chisq	Df	RobustF	Pr(F)
(Intercept)		1		
age	1	205.08	< 2.2e-16	***
pareia	1	410.03	< 2.2e-16	***
tarea	1	84.91	< 2.2e-16	***
ensuit	1	77.37	< 2.2e-16	***
garag	1	58.07	8.105e-15	***
plaz	1	11.58	0.0005245	***
park	1	14.02	0.0001358	***
trans	1	1.72	0.1813986	
bike	1	12.32	0.0003474	***
barb	1	0.07	0.7886646	
balc	1	5.49	0.0169267	*
elev	1	5.11	0.0212121	*
fitg	1	28.85	4.414e-08	***
categ	1	55.34	3.431e-14	***

```
---
signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Warning messages:
1: In lmRob.fit.compute(x, y, x1.idx = x1.idx, nrep = nrep, robust.control = robust.control, :
  Max iteration for refinement reached.
2: In lmRob.fit.compute(x, y, x1.idx = x1.idx, nrep = nrep, robust.control = robust.control, :
  Max iteration for refinement reached.
3: In lmRob.fit.compute(x, y, x1.idx = x1.idx, nrep = nrep, robust.control = robust.control, :
  Max iteration for refinement reached.
4: In lmRob.fit.compute(x, y, x1.idx = x1.idx, nrep = nrep, robust.control = robust.control, :
  Max iteration for refinement reached.
```



```
> anova(resultados)
```

```
Analysis of Variance Table
```

```
Response: price
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
age	1	4.1181e+13	4.1181e+13	782.5857	< 2.2e-16	***
parea	1	4.9625e+13	4.9625e+13	943.0548	< 2.2e-16	***
tarea	1	7.5864e+12	7.5864e+12	144.1677	< 2.2e-16	***
bath	1	4.3846e+12	4.3846e+12	83.3224	< 2.2e-16	***
ensuit	1	2.8791e+12	2.8791e+12	54.7126	5.616e-13	***
garag	1	3.9279e+12	3.9279e+12	74.6439	< 2.2e-16	***
plaz	1	7.8541e+10	7.8541e+10	1.4925	0.222375	
park	1	1.9113e+12	1.9113e+12	36.3214	3.168e-09	***
trans	1	2.2340e+10	2.2340e+10	0.4245	0.514964	
kidca	1	7.6335e+10	7.6335e+10	1.4506	0.228973	
school	1	5.2679e+10	5.2679e+10	1.0011	0.317514	
health	1	2.5533e+05	2.5533e+05	0.0000	0.998243	
bike	1	2.9858e+11	2.9858e+11	5.6741	0.017575	*
barb	1	5.9962e+10	5.9962e+10	1.1395	0.286254	
balc	1	8.5169e+11	8.5169e+11	16.1850	6.596e-05	***
elev	1	4.1658e+11	4.1658e+11	7.9165	0.005084	**
fitg	1	1.9156e+12	1.9156e+12	36.4025	3.047e-09	***
party	1	1.7862e+11	1.7862e+11	3.3944	0.065986	.
categ	1	1.3613e+12	1.3613e+12	25.8693	5.106e-07	***
Residuals	521	2.7416e+13	5.2622e+10			

```
---
```

```
signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```