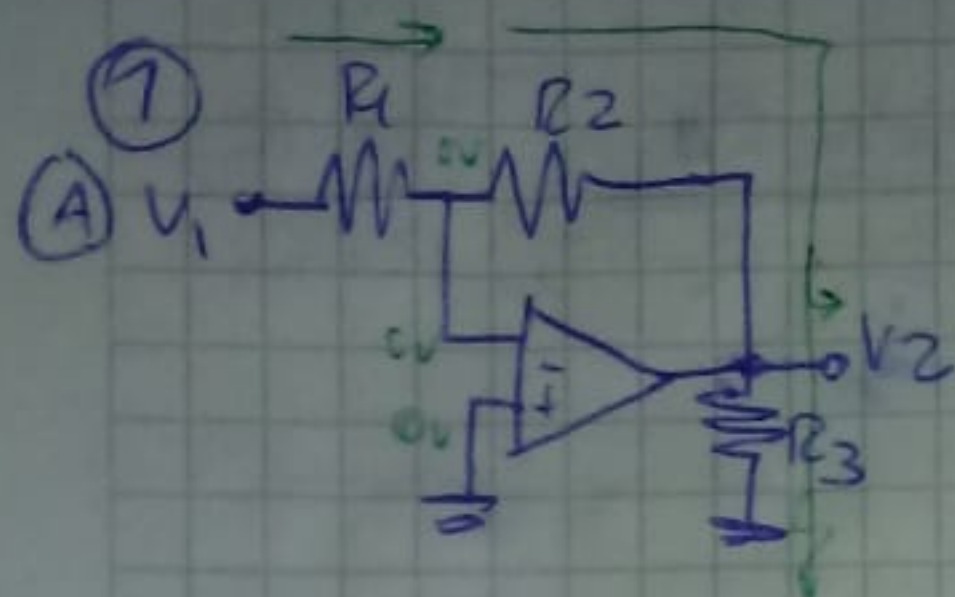


Trabajo práctico ①

$$R_1 = \frac{V_I}{I_1} = \boxed{R_1}$$



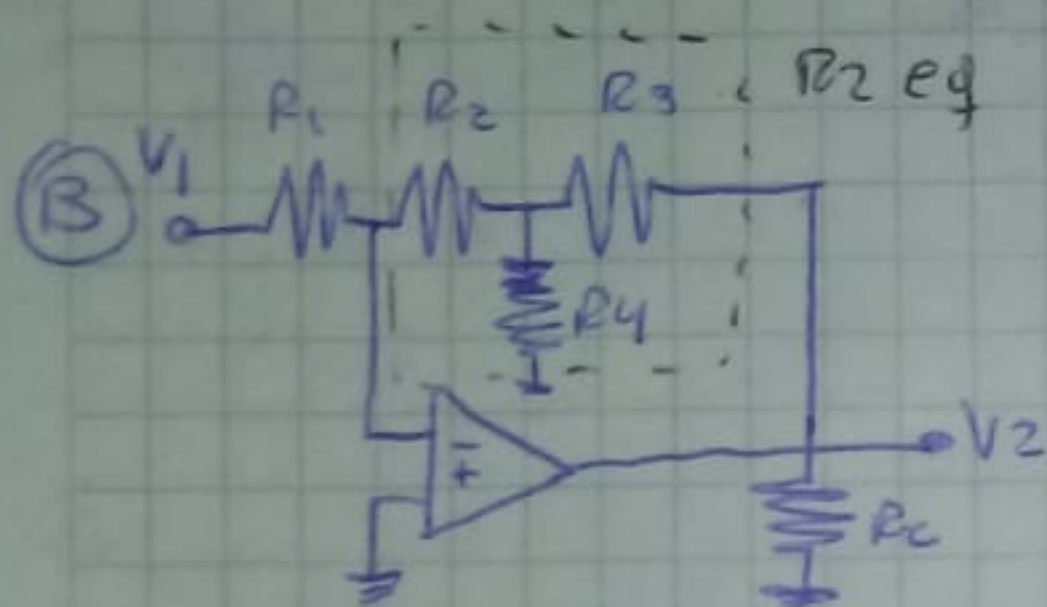
$$\frac{V_1}{R_1} = \frac{-V_2}{R_2} \Rightarrow \boxed{\frac{V_2}{V_1} = -\frac{R_2}{R_1}}$$

$$\frac{R_2}{R_1} \text{ debe ser } 3000 \text{ y } \boxed{R_1 \text{ debe ser } 10k}$$

$$\boxed{R_2 = 30M}$$

Demasiado grande

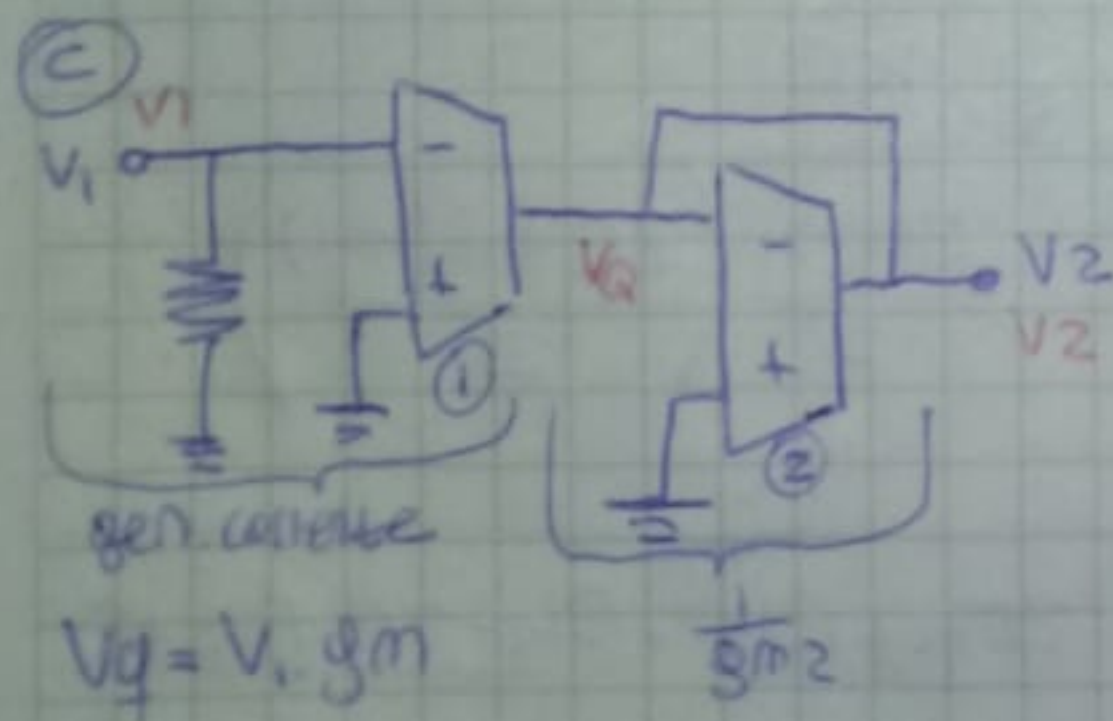
- mucho ruido
- valor complicado de manejar



$$R_1 = R_i$$

$$\frac{V_2}{V_1} = -\frac{R_{2eq}}{R_1}$$

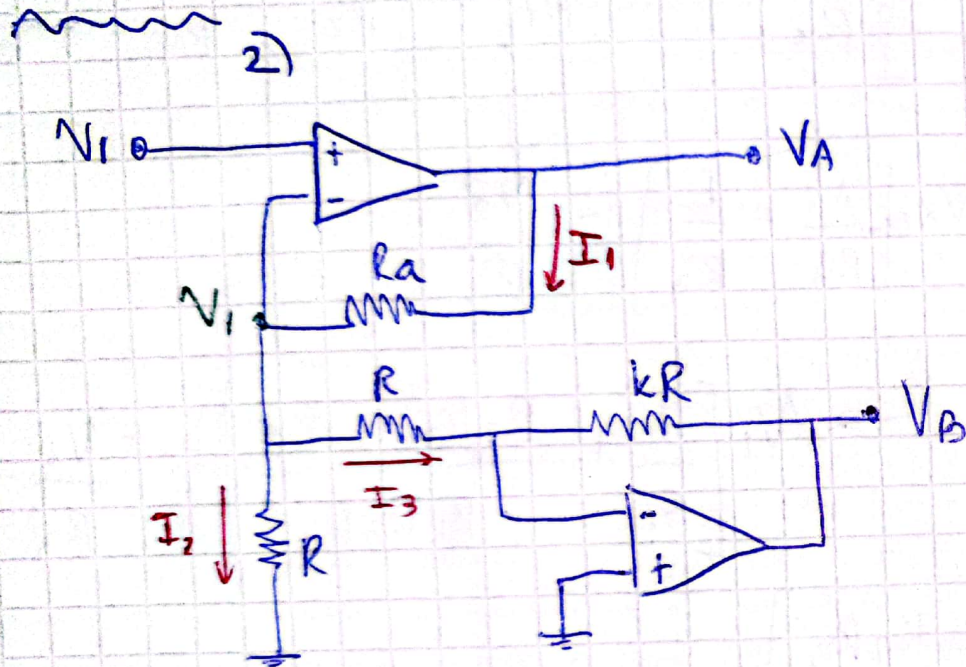
En este circuito, a diferencia del anterior, se puede repartir el valor de R_2 en 3 resistencias de menor valor, facilitando así el diseño y minimizando el ruido.



$$\frac{V_2}{V_1} = \frac{1}{g_{m2}}$$

$$\frac{V_2}{V_1 \cdot g_{m1}} = \frac{1}{g_{m2}} \Rightarrow \boxed{\frac{V_2}{V_1} = \frac{g_{m1}}{g_{m2}}}$$

Este circuito es aún más sencillo, ya que la ganancia se controla con la corriente que genera el 1º OTA.



$$V_{AB} = ?$$

$$R_a = \frac{R(k-1)}{2}$$

$$\frac{V_A - V_1}{R_a} = \frac{V_1}{R} + \frac{V_1}{R} = \frac{2V_1}{R}$$

$$V_A - V_1 = \frac{2R_a}{R} V_1$$

$$V_A = V_1 \left(1 + \frac{2R_a}{R} \right) *$$

$$\frac{V_1}{R} = -\frac{V_B}{kR} \rightarrow V_B = -kV_1 *$$

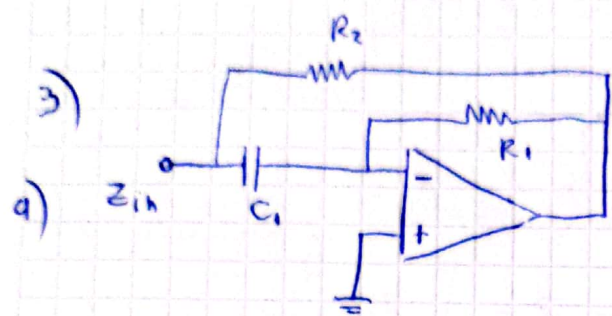
$$V_{AB} = V_A - V_B = V_1 \left(1 + \frac{2R_a}{R} - (-k) \right) = V_1 \left(\frac{R + 2R_a}{R} + k \right)$$

NOTA

$$V_{AB} = V \left(\frac{R + 2R_A + kR}{R} \right) = \left(\frac{R + R(k-1) + kR}{R} \right) V_1$$

$$V_{AB} = (1 + k - 1 + k) V_1$$

$$V_{AB} = 2k V_1$$



$$Z_{in} = \frac{V_1}{i_e} \rightarrow \text{generica}$$

$$i_e = V_1 \cdot sC_1 + \frac{V_1 - V_2}{R_2}$$

$$V_1 \cdot sC_1 = \frac{V_2 - V_1}{R_1}$$

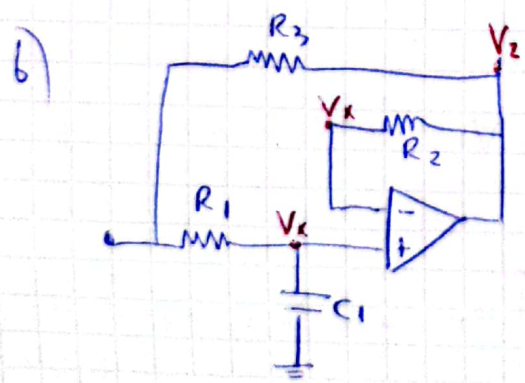
$$i_e = V_1 \cdot sC_1 + \frac{V_1}{R_2} + \frac{V_1 \cdot sC_1 R_1}{R_2}$$

$$V_2 = -V_1 \cdot sC_1 R_1$$

$$i_e = V_1 \left[\frac{sC_1 R_2 + 1 + sC_1 R_2}{R_2} \right]$$

$$\rightarrow Z_{in} = \frac{R_2}{sC_1(R_1 + R_2) + 1}$$

↑ No funciona así



$$Z_{in} = \frac{V_1}{i_e}$$

$$i_e = \frac{V_1 - V_2}{R_3} + \frac{V_x}{\frac{1}{sC_1}}$$

$$R_2 = 0 \rightarrow V_x = V_2$$

$$\frac{V_1 - V_2}{R_1} = V_2 \cdot sC_1$$

$$i_e = \frac{V_1 - V_1}{R_3} + \frac{V_1}{(1 + sC_1 R_1) R_3} + \frac{V_1}{(1 + sC_1 R_1)}$$

$$i_e = V_1 \left[\frac{1}{R_3} - \frac{1}{R_3 + sC_1 R_1 R_3} + \frac{sC_1}{1 + sC_1 R_1} \right]$$

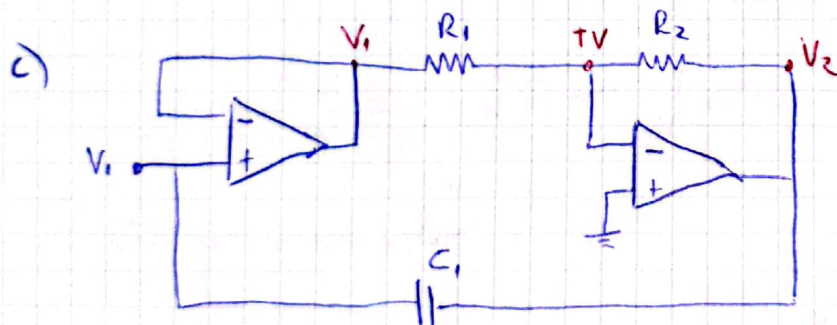
$$i_e = V_1 \left[\frac{1 + \frac{1}{\beta} C_1 R_1}{R_3 + \frac{1}{\beta} C_1 R_1 R_3} + \frac{\frac{1}{\beta} C_1 + \frac{1}{\beta} C_1^2 R_1}{1 + \frac{1}{\beta} C_1 R_1} - \frac{1}{\beta} C_1 \right]$$

$$= V_1 \left[\frac{\frac{1}{\beta} C_1 R_1}{R_3 + \frac{1}{\beta} C_1 R_1 R_3} + \frac{\frac{1}{\beta} C_1^2 R_1}{1 + \frac{1}{\beta} C_1 R_1} \right]$$

$$i_e = \left(\frac{\frac{1}{\beta} C_1 R_1 + 1 + \frac{1}{\beta} C_1 R_1}{R_3 + \frac{1}{\beta} C_1 R_1 R_3} - \frac{1}{\frac{1}{\beta} C_1 R_1 R_3 + R_3} \right) V_1$$

$$i_e = \frac{\frac{1}{\beta} C_1 (R_1 + R_3)}{\frac{1}{\beta} C_1 R_1 R_3 + R_3} V_1$$

$$\rightarrow \frac{V_1}{i_e} = \left[\frac{\frac{1}{\beta} C_1 R_1 R_3 + R_3}{\frac{1}{\beta} C_1 (R_1 + R_3)} \right] = Z_{in}$$

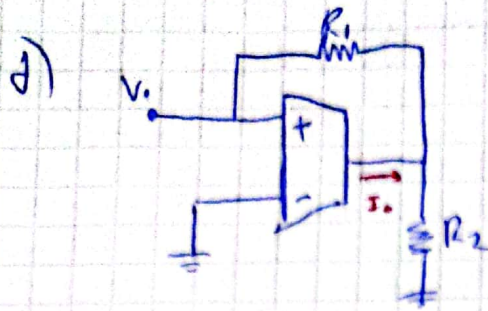


$$i_e = (V_1 - V_2) \frac{1}{R_1}$$

$$\frac{V_1}{R_1} = -\frac{V_2}{R_2} \rightarrow V_2 = -\frac{R_2}{R_1} V_1$$

$$i_e = V_1 \left(1 + \frac{R_2}{R_1} \right) \frac{1}{R_1} = \left(\frac{R_1 + R_2}{R_1} \right) \frac{1}{R_1} V_1$$

$$\rightarrow Z_{in} = \frac{R_1}{\frac{1}{R_1} (R_1 + R_2)} = \frac{1}{\frac{1}{R_1} \left(\frac{R_1 + R_2}{R_1} \right)} \rightarrow \text{módulo Capacitivo}$$



$$I_0 = V_i g_m$$

$$I_{R_2} = I_0 + I_1$$

$$V_{R_2} = (I_0 + I_1) R_2$$

$$V_{R_2} = V_i g_m R_2 + \frac{V_i R_2}{R_1} - \frac{V_{R_2} R_2}{R_1}$$

$$V_{R_2} \left[1 + \frac{R_2}{R_1} \right] = V_i \left[g_m R_2 + \frac{R_2}{R_1} \right]$$

$$V_{R_2} \left(\frac{R_1 + R_2}{R_1} \right) = V_i \left(\frac{g_m R_1 R_2 + R_2}{R_1} \right)$$

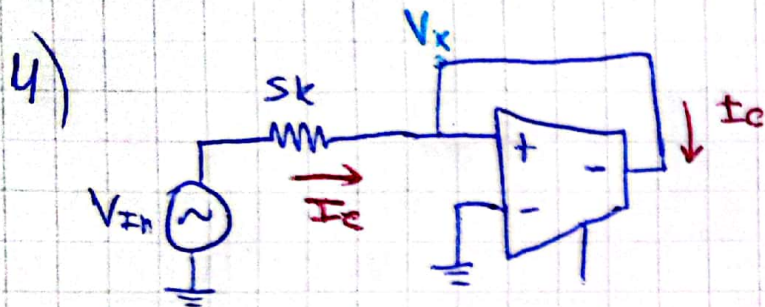
$$V_{R_2} = \left(\frac{g_m R_1 R_2 + R_2}{R_1 + R_2} \right) V_i$$

$$I_e = \frac{V_i}{R_1} - V_i \left(\frac{g_m R_1 R_2 + R_2}{R_1^2 + R_1 R_2} \right)$$

$$= V_i \left(\frac{1}{R_1} - \frac{g_m R_1 R_2 + R_2}{R_1^2 + R_1 R_2} \right) = \frac{R_1^2 + R_1 R_2 - g_m R_1^2 R_2 - R_1 R_2}{R_1^2 + R_1 R_2} V_i$$

$$I_e = \frac{R_1 - g_m R_1 R_2}{R_1^2 + R_1 R_2} V_i = \frac{1 - g_m R_2}{R_1 + R_2} V_i$$

$$Z_i = \frac{V_i}{I_e} = \left[\frac{R_1 + R_2}{1 - g_m R_2} \right]$$



$$I_e = V_x g_m$$

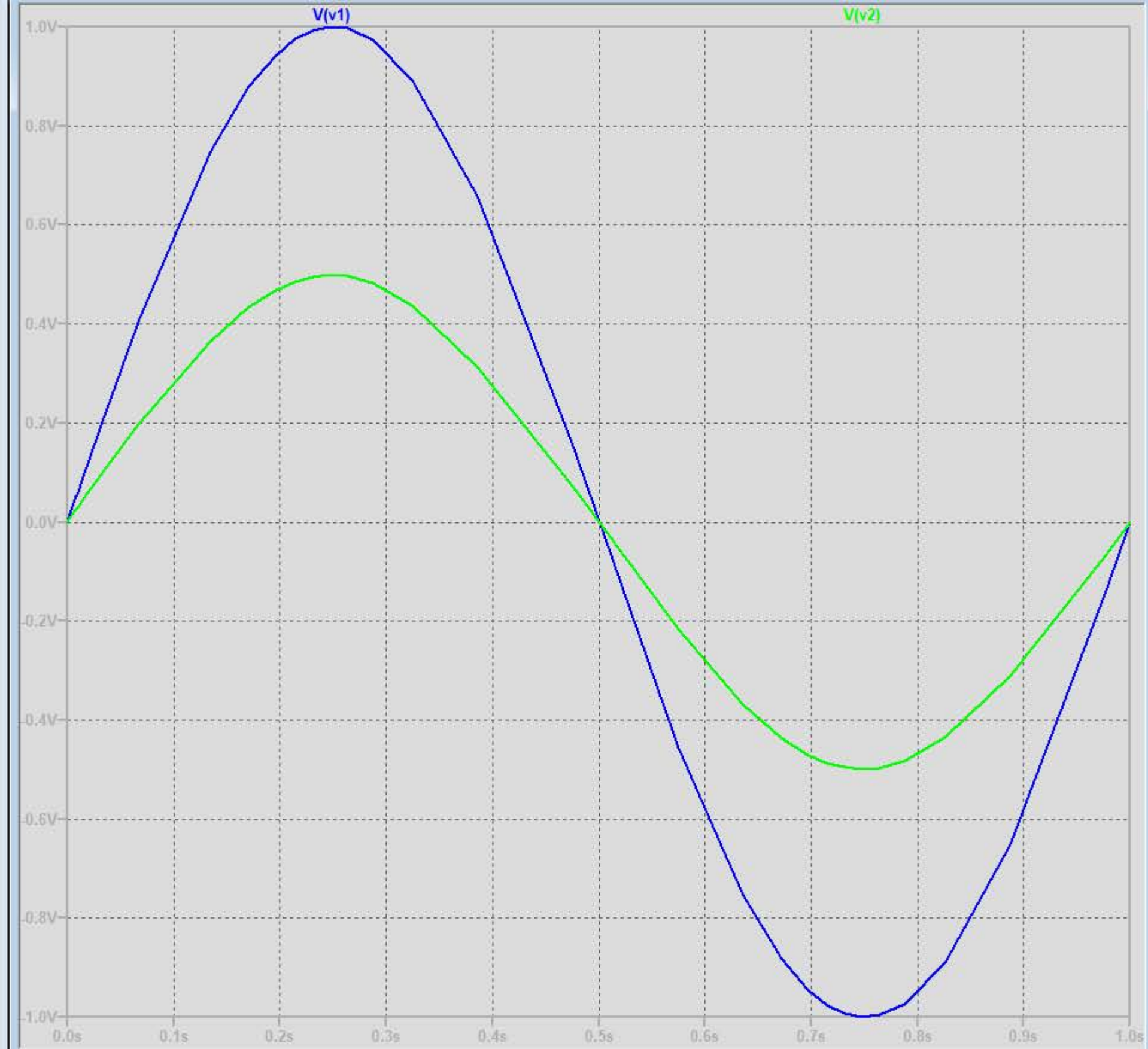
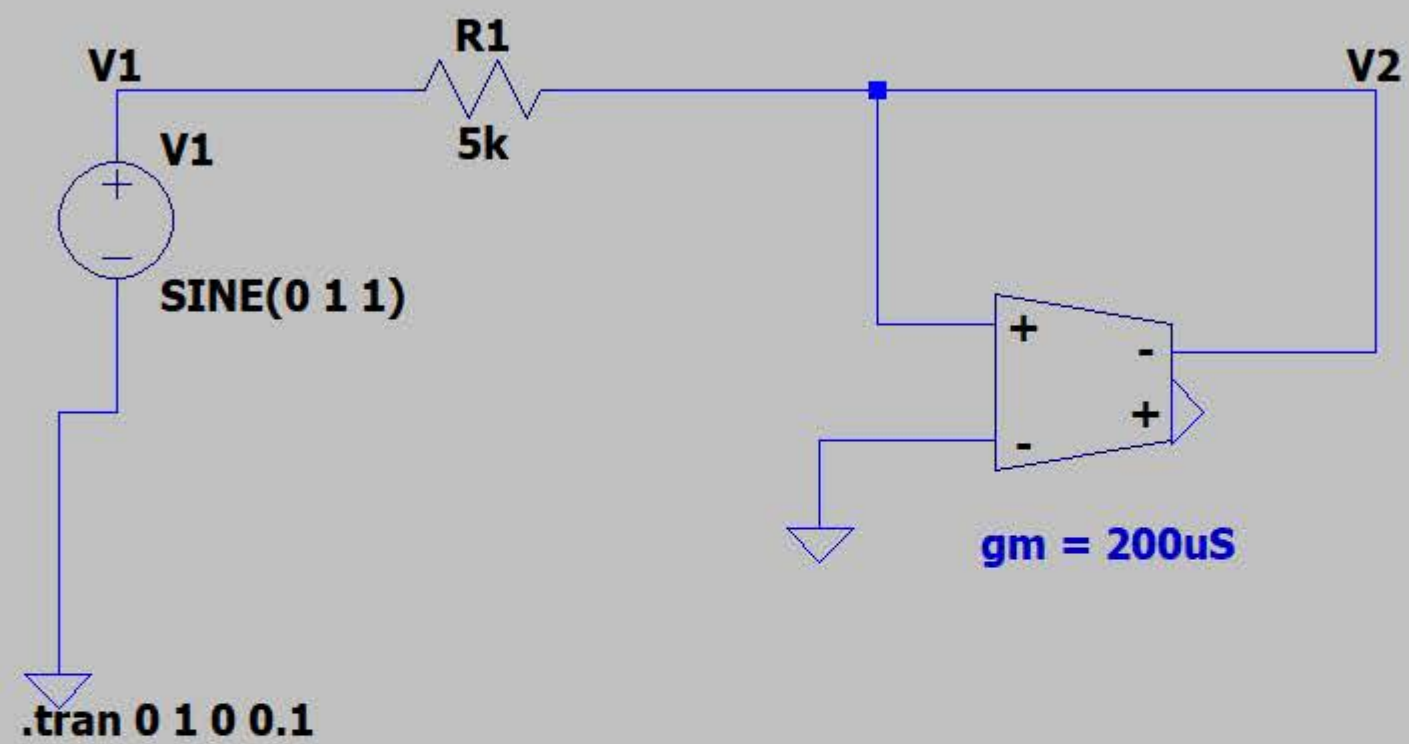
$$Z_{in} = \frac{V_x}{I_e} = \frac{1}{g_m}$$

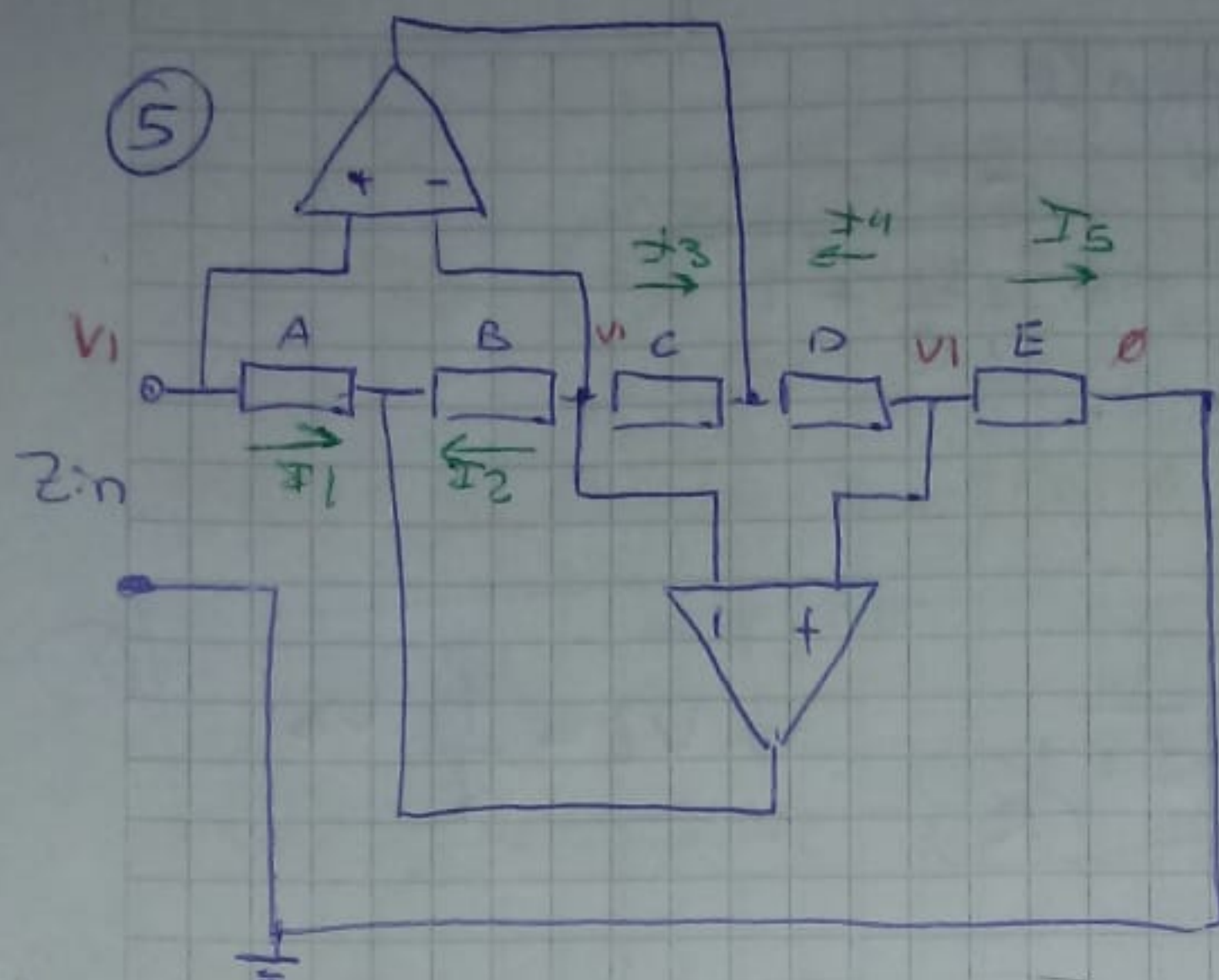
$$\frac{1}{g_m} = 5k \rightarrow g_m = 200 \mu S$$

b) $I_{ABC} \cong 15 \mu A$ (región gráfica)

$$V_{in} = I_e \cdot 5k + V_o \cdot \frac{g_m}{g_m} = V_o g_m \cdot 5k + V_o \frac{g_m}{g_m} =$$

$$V_{in} = V_o (1 + 1) \rightarrow \frac{V_o}{V_{in}} = \frac{1}{2}$$





$$Z_A \cdot I_1 = Z_B \cdot I_2$$

$$I_1 = \frac{Z_B}{Z_A} \cdot I_2$$

$$I_2 = -I_3$$

$$I_1 = -\frac{Z_B}{Z_A} \cdot I_3$$

$$Z_C \cdot I_3 = Z_D \cdot I_4$$

$$I_3 = \frac{Z_D}{Z_C} \cdot I_4$$

$$I_4 = -I_5 \rightarrow I_1 = \frac{Z_B \cdot Z_D}{Z_A \cdot Z_C} \cdot I_5$$

$$\rightarrow I_3 = \frac{V}{Z_E}$$

$$Z_1 = -\frac{Z_B}{Z_A} \cdot \frac{Z_D}{Z_C} \cdot I_4 = \frac{Z_B \cdot Z_D}{Z_A \cdot Z_C} \cdot I_5 = V$$

$$V \frac{Z_B \cdot Z_D}{Z_A \cdot Z_C \cdot Z_E} = I \rightarrow$$

$$Z = \frac{Z_A \cdot Z_C \cdot Z_E}{Z_B \cdot Z_D}$$

en ⑤ $\rightarrow Z_L = \frac{R_1 R_2 R_4}{\frac{1}{sC} R_3}$

$$Z_L = \frac{sC R_1 R_2 R_4}{R_3}$$

"Inductor"

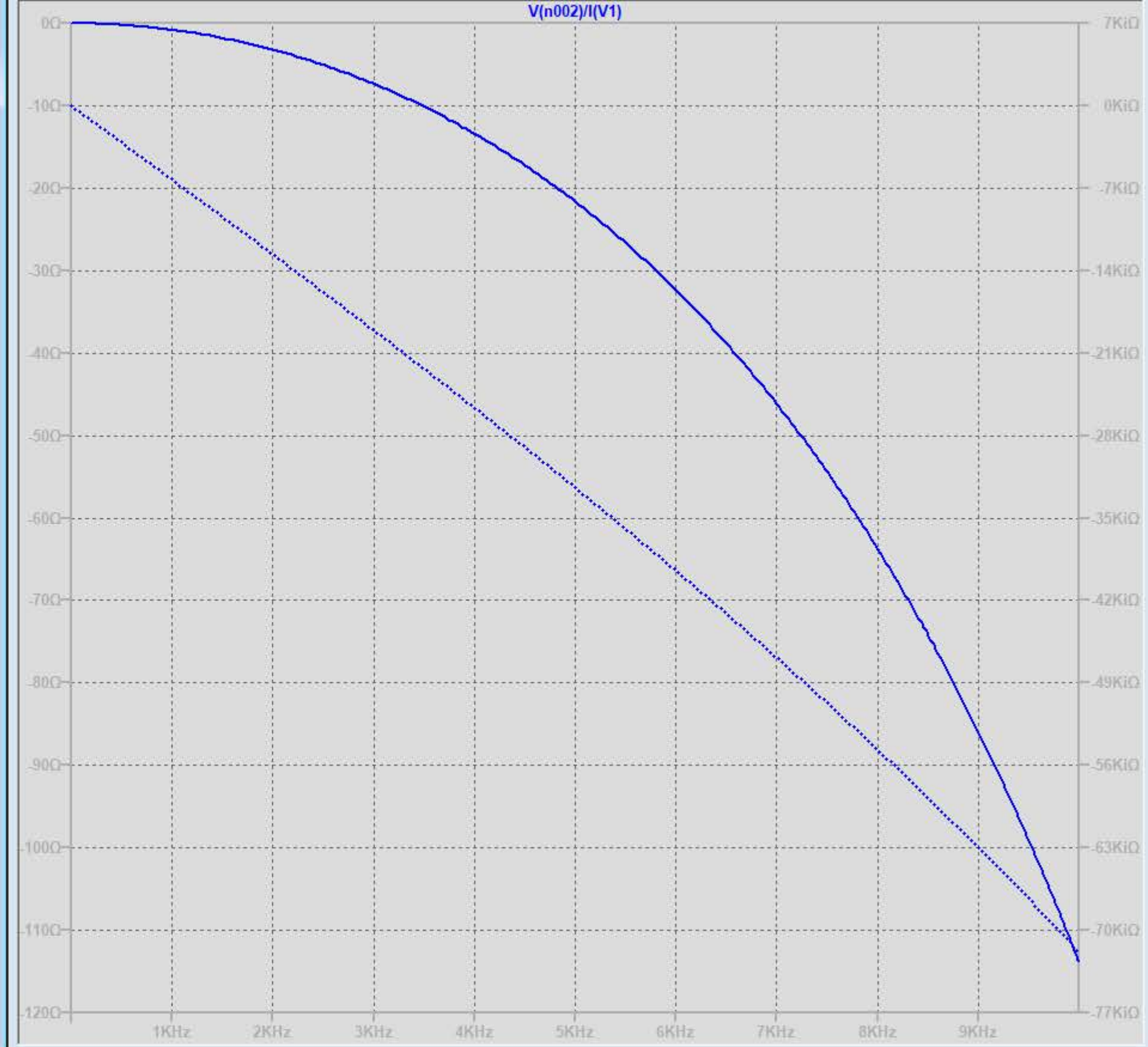
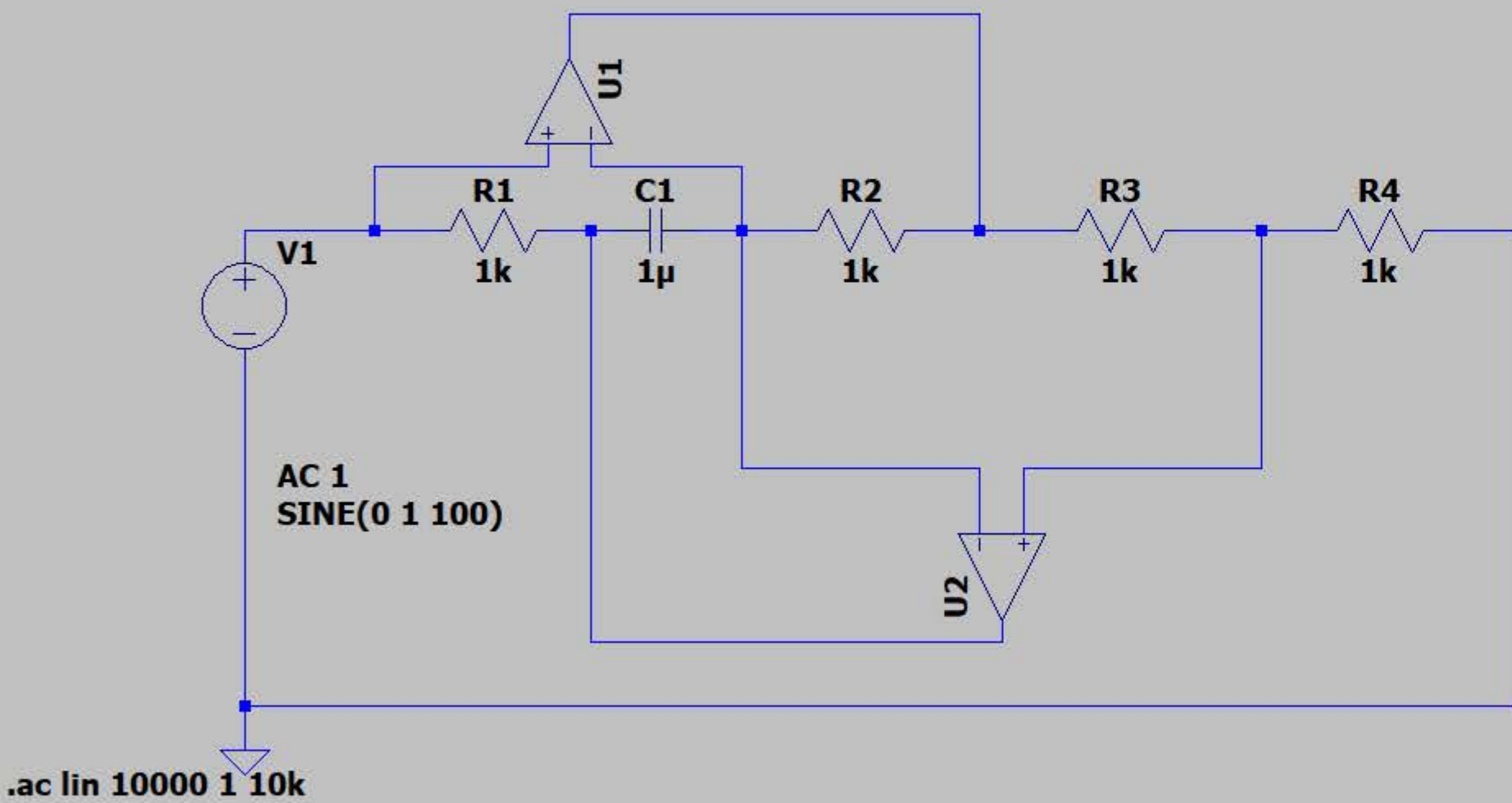
en ⑥ $\rightarrow Z_L = \frac{\frac{1}{sC_1} \cdot \frac{1}{sC_2} R_4}{R_1 R_3}$

~~Inductor~~

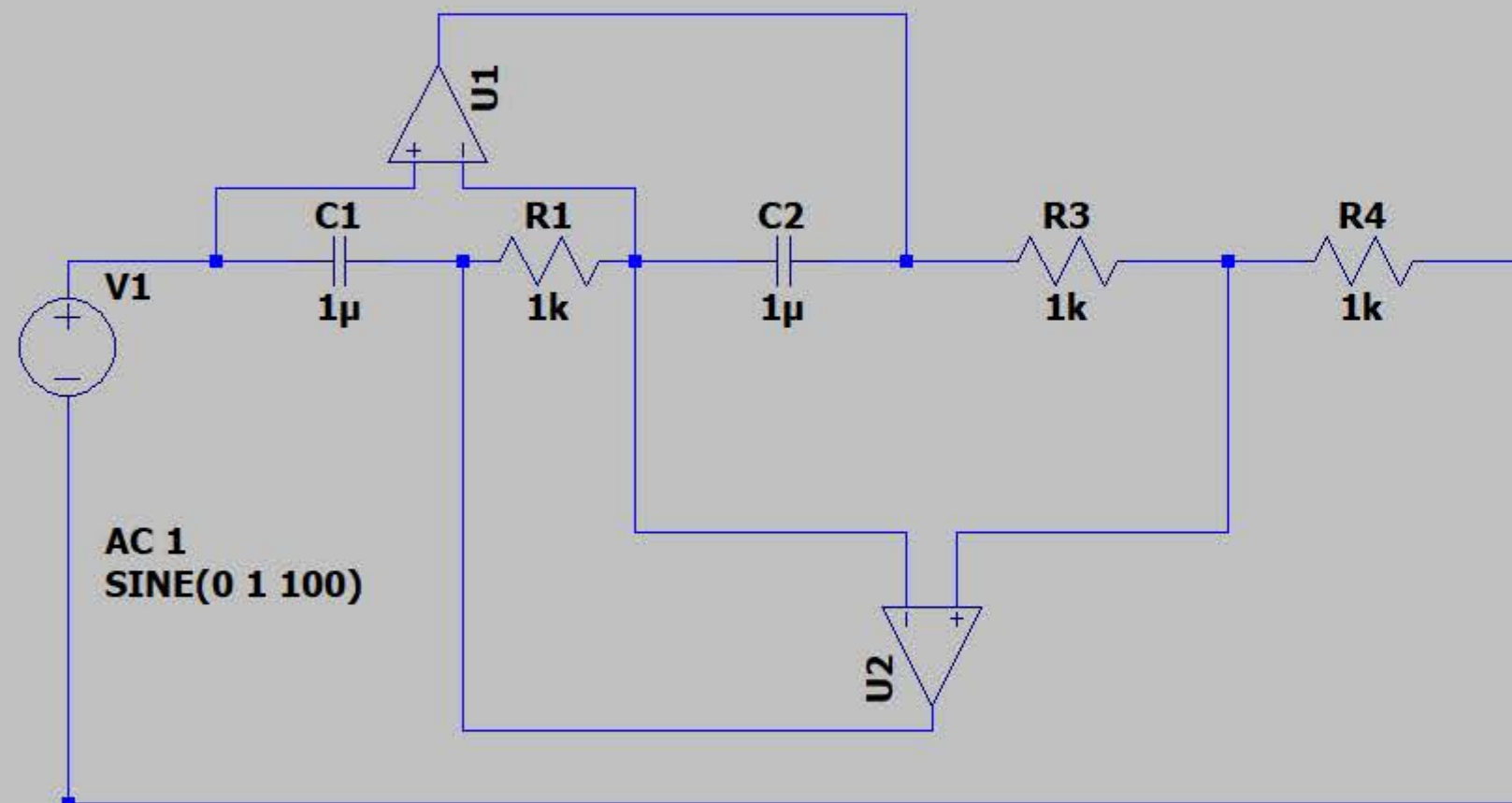
$$= \frac{R_4}{R_1 R_3 s^2 C_1 C_2} = Z_L$$

c

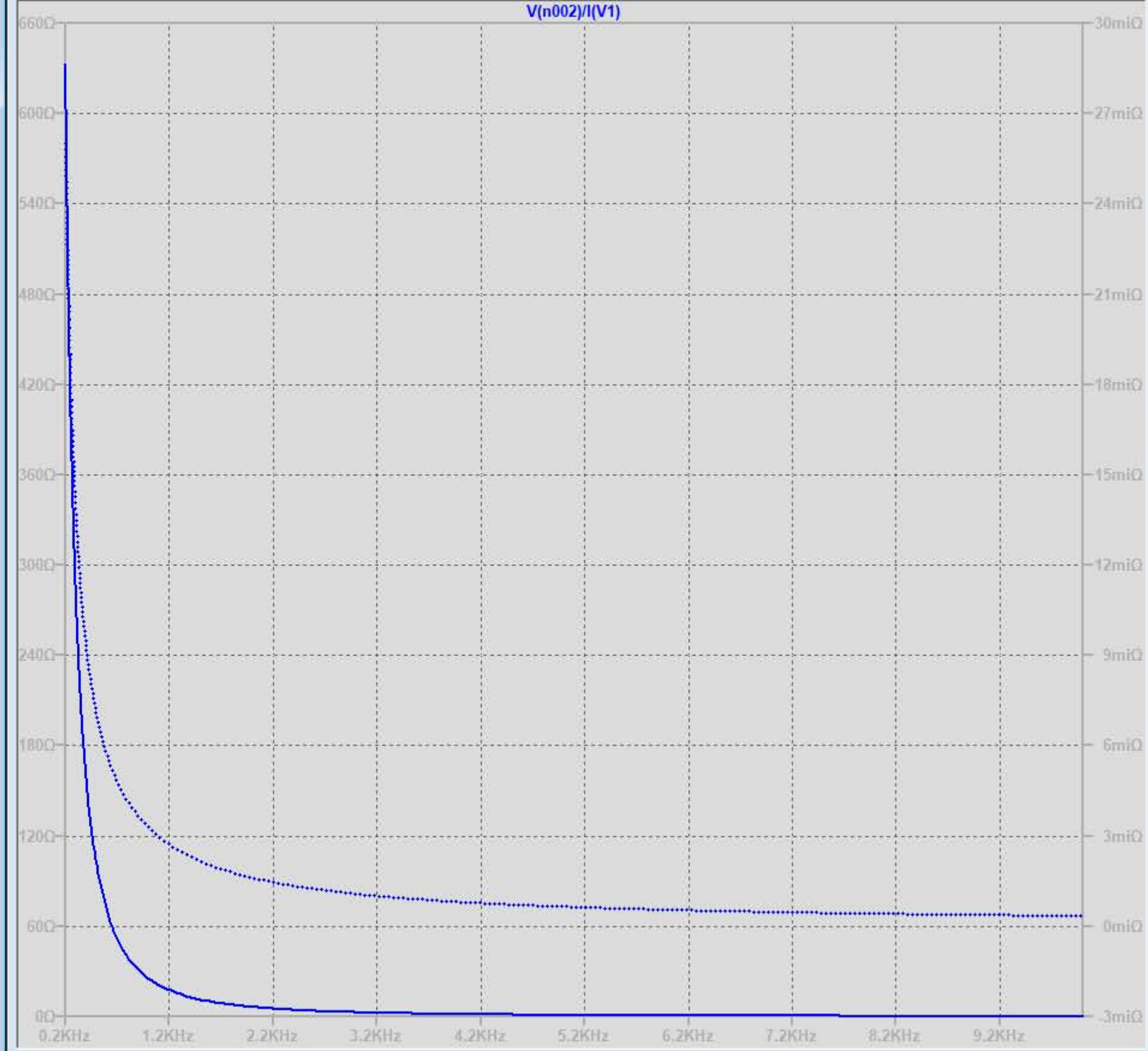
.inc opamp.sub

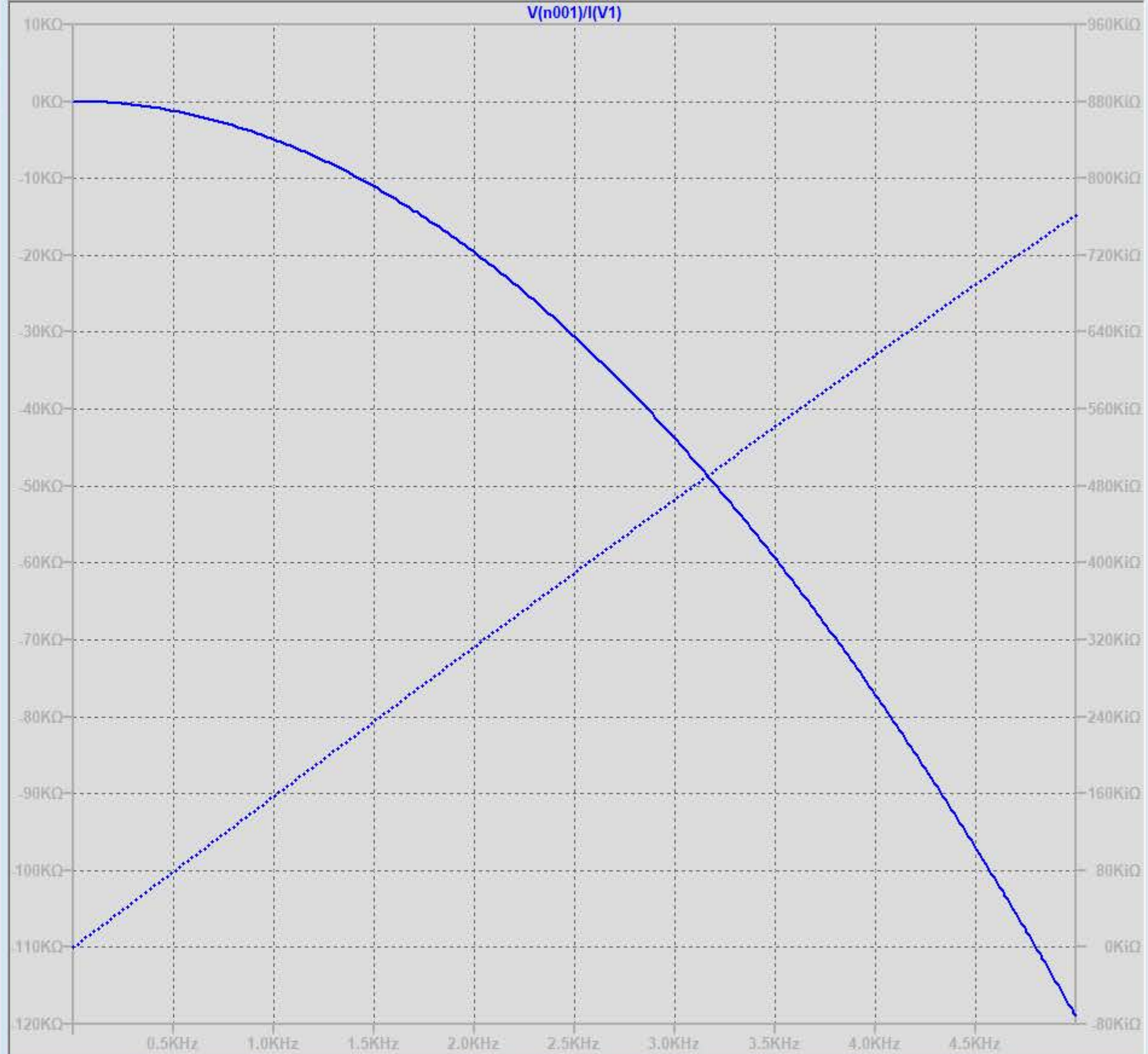
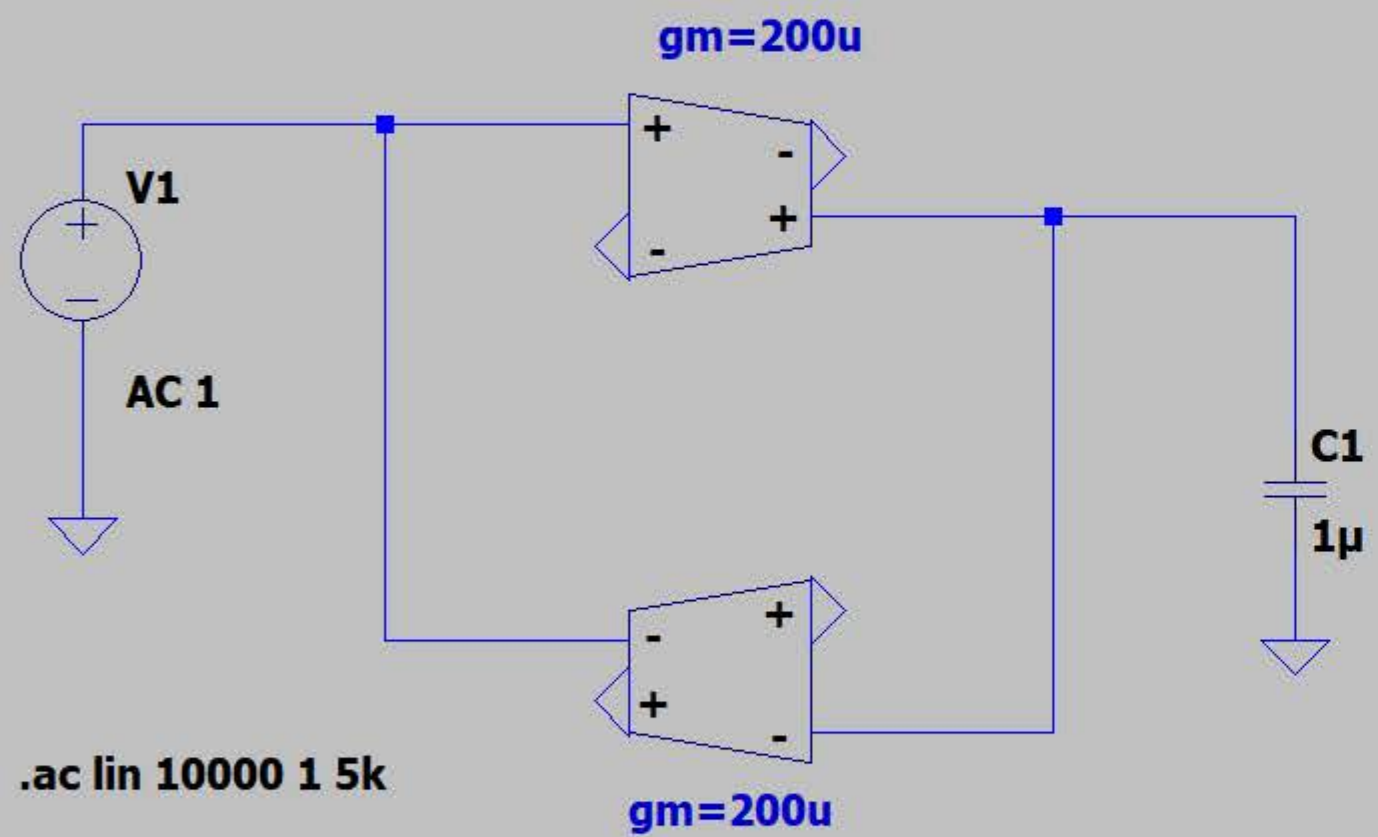


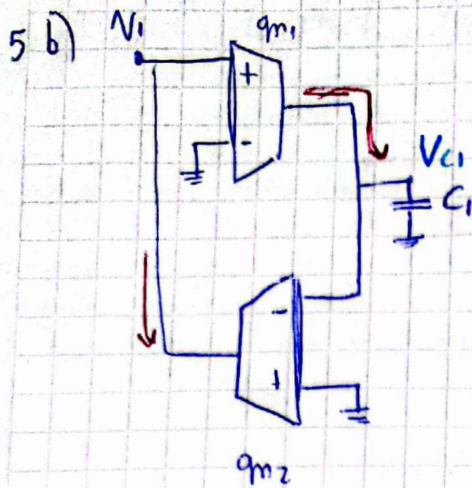
.inc opamp.sub



.ac lin 10000 200 10k







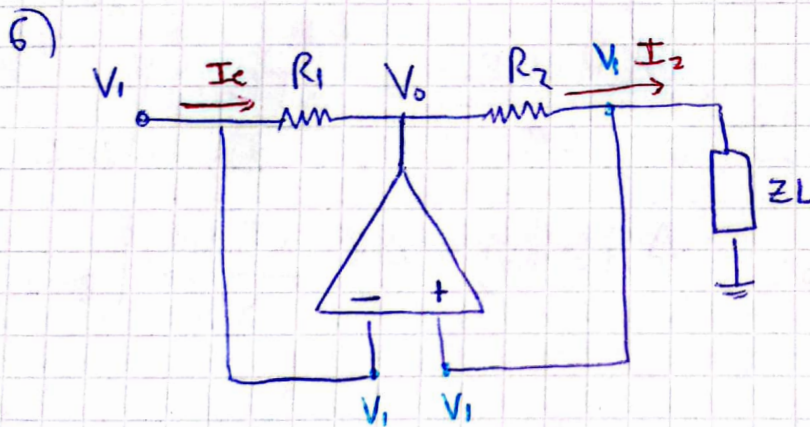
$$\frac{V_i}{I_e} = Z_i$$

$$I_e = I_2 = g_{m2} \cdot V_{C1}$$

$$V_{C1} = \frac{I_{C1}}{sC} = \frac{I_1}{sC} = \frac{V_i \cdot g_{m1}}{sC}$$

$$I_e = \frac{g_{m2} \cdot g_{m1} \cdot V_i}{sC_1}$$

$$Z_{in} = \frac{sC_1}{g_{m1} g_{m2}}$$



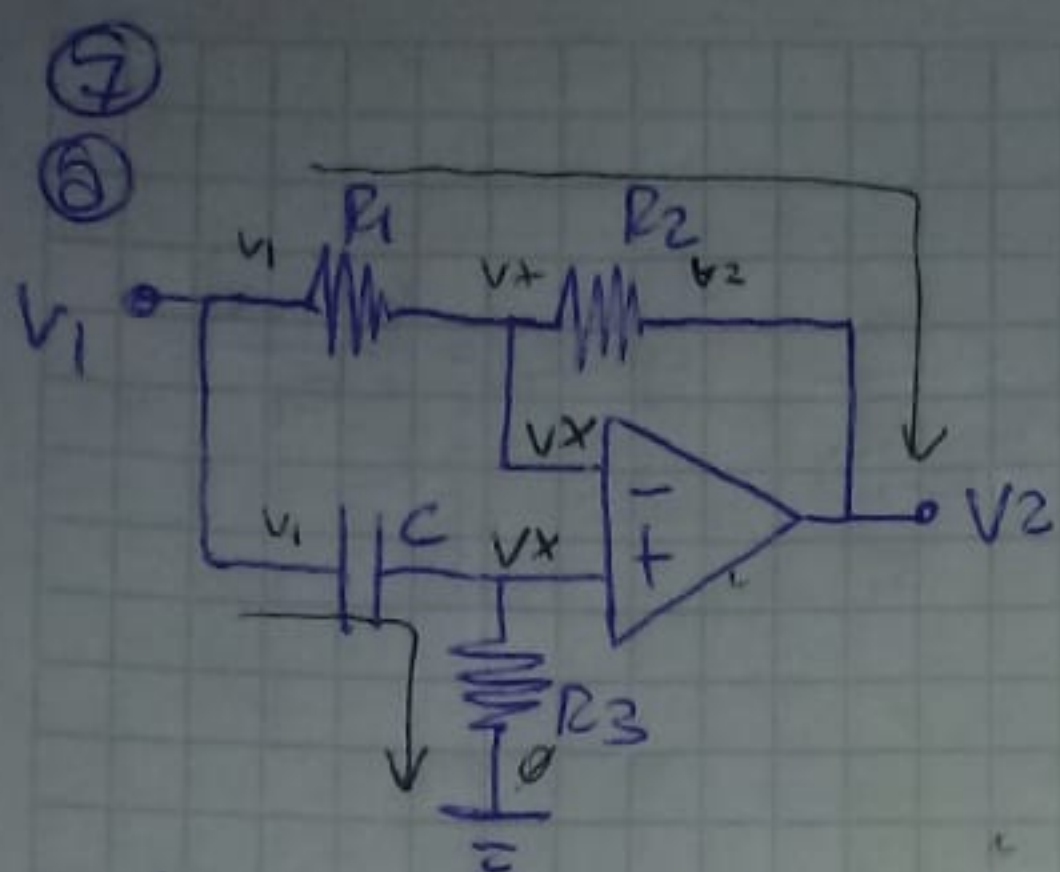
$$I_e = \frac{V_i - V_o}{R_1}$$

$$\frac{V_o - V_i}{R_2} = \frac{V_i}{Z_L}$$

$$V_o = V_i \left(1 + \frac{R_2}{Z_L} \right)$$

$$I_e = \frac{V_i}{R_1} - V_i \left(\frac{Z_L + R_2}{Z_L R_1} \right) = V_i \left[\frac{1}{R_1} - \frac{Z_L + R_2}{R_1 Z_L} \right] = V_i \left[\frac{Z_L - Z_L - R_2}{R_1 Z_L} \right]$$

$$\frac{I_e}{V_i} = \frac{-R_2}{R_1 Z_L} \rightarrow Z_{in} = \frac{-R_1 Z_L}{R_2}$$



$$\cancel{V_x = V_1 R_3 \cancel{\$C}}$$

$$\frac{V_1 - V_x}{R_1} = \frac{V_x - V_2}{R_2}$$

$$V_x = \frac{V_1 R_3}{R_3 + \frac{1}{\$C}}$$

$$V_x = \frac{V_1 R_3 \$C}{\$C R_3 + 1}$$

$$\cancel{\frac{V_1}{R_1} - \frac{V_1 R_3 \$C}{R_1} = \frac{V_1 R_3 \$C}{R_2} - \frac{V_2}{R_2} \Rightarrow V_1 \left(\frac{1}{R_1} - \frac{R_3 \$C}{R_1} - \frac{R_3 \$C}{R_2} \right) = \frac{V_2}{R_2}}$$

$$\cancel{V_1 \left(\frac{-R_2 + R_2 R_3 \$C + R_3 R_2 \$C}{R_1 R_2} \right) = V_2 \Rightarrow V_1 \left(\frac{-R_2^2 + R_2^2 R_3 \$C + R_3 R_2 R_1 \$C}{R_1 R_2} \right) = V_2}$$

$$\cancel{\frac{V_2}{V_1} = \frac{-R_2^2 + R_2^2 R_3 \$C + R_3 R_2 R_1 \$C}{R_1 R_2}}$$

$$\frac{V_1 - \frac{V_1 R_3 \$C}{R_1 (\$C R_3 + 1)}}{R_1} = \frac{\frac{V_1 R_3 \$C}{R_2 (\$C R_3 + 1)} - \frac{V_2}{R_2}}{R_2}$$

$$V_1 \left(\frac{-R_2}{R_1} + \frac{R_3 \$C R_2}{R_1 (\$C R_3 + 1)} + \frac{R_3 \$C R_2}{R_2 (\$C R_3 + 1)} \right) = V_2$$

$$\frac{V_2}{V_1} = \frac{-R_2 (\$C R_3 + 1) + R_3 \$C R_2 + R_3 \$C R_2 R_1}{R_1 R_2 (\$C R_3 + 1)} = T(\$)$$

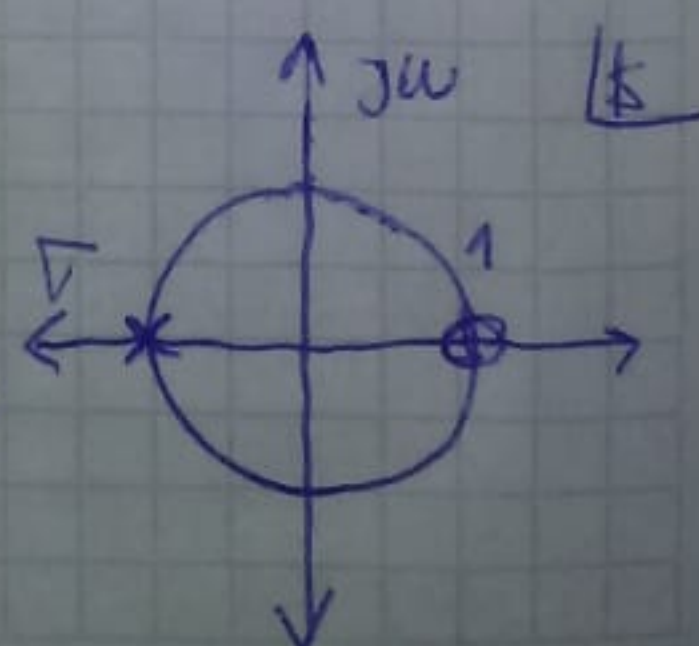
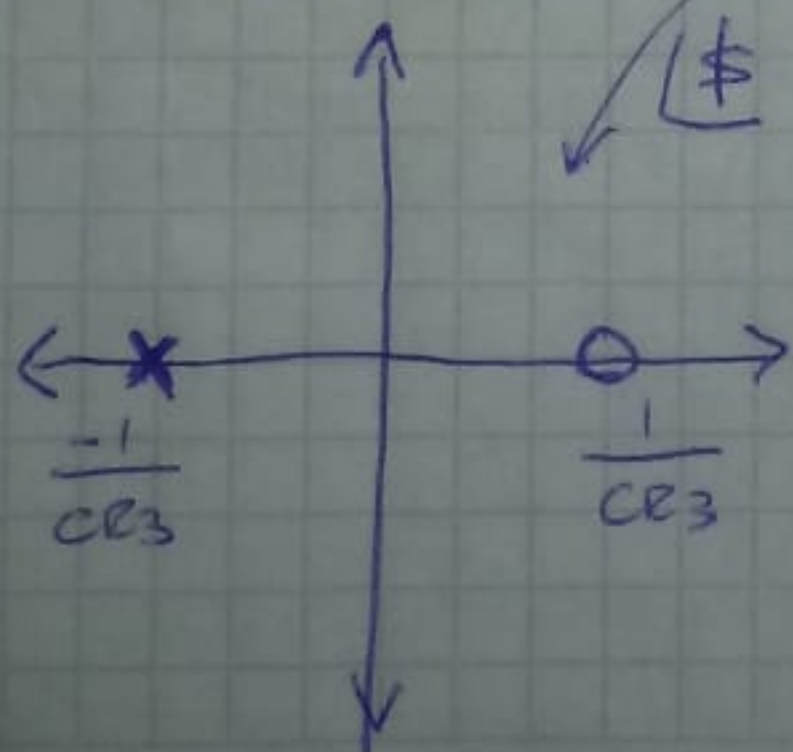
$$T(\$) = \frac{-R_2 \$C R_3 + R_2 + R_3 \$C R_2 + R_3 \$C R_1}{R_1 \$C R_3 + R_1} = \frac{\$ (R_2 C R_3 + R_2 C R_2 + R_3 C R_1) + R_2}{\$ (C R_3 R_1) + R_1}$$

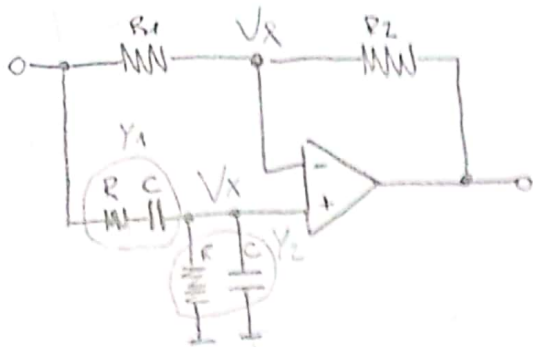
$$T(\$) = \frac{\$ \left(\frac{R_2}{C R_3 R_1} \right) + \frac{R_2}{C R_3 R_1}}{\$ + \frac{1}{C R_3}} = \frac{\$ + \frac{R_2}{C R_3 R_1}}{\$ + \frac{1}{C R_3}}$$

Assumiendo $R_2 = R_1$

$$\text{norm} = \omega_0^2 = \frac{1}{C R_2}$$

$$T(\$) = \frac{\$ - 1}{\$ + 1}$$





$$Z_1 = R + \frac{1}{sC} = \frac{sCR + 1}{sC} = \frac{sC + G}{sCG}$$

$$Y_1 = \frac{sC}{sCR + 1} = \frac{sCG}{sC + G}$$

$$\frac{1}{Z_2} = Y_2 = \frac{1}{R} + sC = \frac{sCR + 1}{R} = \frac{sC + G}{R}$$

$$V_x (G_1 + G_2) - V_1 G_1 - V_2 G_2 = 0 \quad (1) \quad V_x = V_1 \cdot \frac{Y_1}{Y_1 + Y_2} \quad (2)$$

$$\frac{V_2}{V_1} = \frac{Y_1 (G_1 + G_2) - G_1 (Y_1 + Y_2)}{(Y_1 + Y_2) G_2} = \frac{\frac{sCG}{sC + G} (G_1 + G_2) - G_1 \left(\frac{sCG}{sC + G} + \frac{sC + G}{R} \right)}{\left[\frac{sCG}{sC + G} + \frac{sC + G}{R} \right] G_2}$$

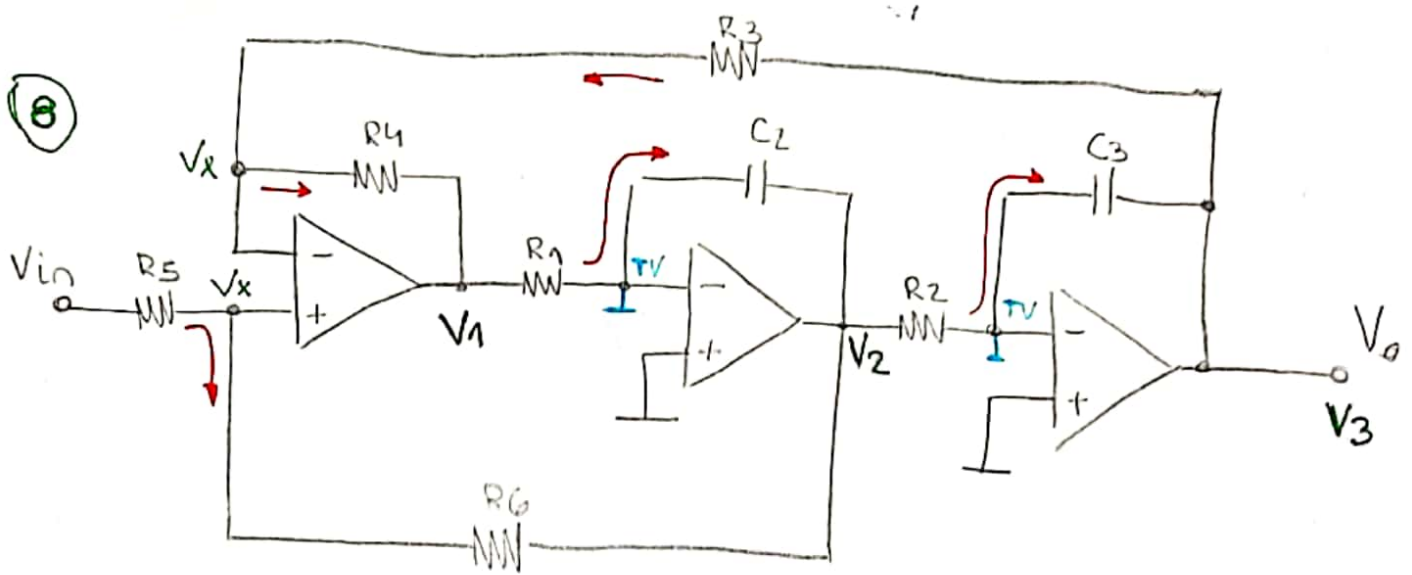
$$\frac{V_2}{V_1} = \frac{\frac{sCGG_1 + sCGG_2}{sC + G} - \left(\frac{sCGG_1 + s^2C^2G_1 + sCGG_1 + sCGG_1 + G^2G_1}{sC + G} \right)}{\left(\frac{sCG + s^2C^2 + sCG + sCG + G^2}{sC + G} \right) G_2}$$

$$\frac{V_2}{V_1} = \frac{-s^2C^2G_1 + s \cdot CG \cdot (G_2 - 2G_1) - G^2G_1}{s^2(s^2C^2 + s \cdot 3CG + G^2) G_2}$$

$$\frac{V_2}{V_1} = \frac{-s^2G_1 + s \frac{G}{C} \cdot (G_2 - 2G_1) - \frac{G^2G_1}{C^2}}{\left[s^2 + \frac{3G}{C} \cdot s + \left(\frac{G}{C} \right)^2 \right] G_2}$$

$$\boxed{\frac{V_2}{V_1} = -\frac{G_1}{G_2} \cdot \frac{s^2 + \frac{G}{CG_1} (2G_1 - G_2) \cdot s + \left(\frac{G}{C} \right)^2}{s^2 + \frac{3G}{C} \cdot s + \left(\frac{G}{C} \right)^2}}$$

8



$$(V_i - V_x)G_5 = (V_x - V_2)G_6 \quad (1)$$

$$V_1 \cdot G_1 = -V_2 \cdot SC_2 \quad (2)$$

$$V_2 G_2 = -V_3 \cdot SC_3 \quad (3)$$

$$(V_3 - V_x)G_3 = (V_x - V_1)G_4 \quad (4)$$

$$V_2 = -V_1 \cdot \frac{G_1}{SC_2}$$

$$V_3 = -V_2 \cdot \frac{G_2}{SC_3}$$

$$V_3 \cdot G_3 + V_1 G_4 = V_x \cdot (G_3 + G_4) \rightarrow -V_2 \cdot \frac{G_2 G_3}{SC_3} + V_1 \cdot G_4 = V_x \cdot (G_3 + G_4)$$

$$\rightarrow V_1 \cdot \left(\frac{G_1 G_2 G_3}{S^2 C_2 C_3} + G_4 \right) = V_x \cdot (G_3 + G_4) \quad (A)$$

$$-V_x (G_5 + G_6) = -V_i G_5 - V_2 \cdot G_6 \rightarrow V_x \cdot (G_5 + G_6) = V_i G_5 - V_1 \frac{G_1 G_6}{SC_2}$$

$$V_x = V_i \frac{G_5}{(G_5 + G_6)} - V_1 \frac{G_1 G_6}{SC_2 (G_5 + G_6)} \quad (B)$$

$$(3) + (A) \quad V_1 \left(\frac{S^2 C_2 C_3 G_4 + G_1 G_2 G_3}{S^2 C_2 C_3} \right) = V_i \cdot \frac{G_5 (G_3 + G_4)}{(G_5 + G_6)} - V_1 \cdot \frac{G_1 G_6 (G_3 + G_4)}{SC_2 (G_5 + G_6)}$$

$$\frac{G_6}{G_3}$$

$$V_1 \left(\frac{S^2 C_2 C_3 G_4 + G_1 G_2 G_3}{S^2 C_2 C_3} + \frac{G_1 G_6 (G_3 + G_4)}{SC_2 (G_5 + G_6)} \right) = V_i \cdot \frac{G_5 (G_3 + G_4)}{(G_5 + G_6)}$$

$$V_1 \left(\frac{S^2 C_2 C_3 G_4 (G_5 + G_6) + G_1 G_2 G_3 (G_5 + G_6) + SC_2 G_1 G_6 (G_3 + G_4)}{S^2 C_2 C_3 (G_5 + G_6)} \right) = V_i \frac{G_5 (G_3 + G_4)}{(G_5 + G_6)}$$

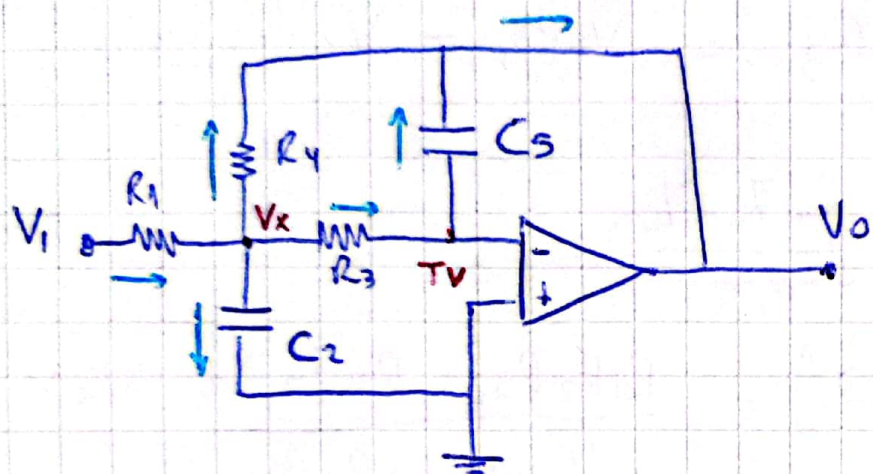
$$\frac{V_1}{V_i} = \frac{S^2 C_2 C_3 G_5 (G_3 + G_4)}{S^2 C_2 C_3 G_4 (G_5 + G_6) + SC_2 G_1 G_6 (G_3 + G_4) + G_1 G_2 G_3 (G_5 + G_6)}$$

$$a) \frac{V_1}{V_i} = \frac{G_5 (G_3 + G_4)}{G_4 (G_5 + G_6)} \cdot \frac{S^2}{S^2 + \frac{G_1 G_6 (G_3 + G_4)}{C_2 G_4 (G_5 + G_6)} S + \frac{G_1 G_2 G_3}{C_2 C_3 G_4}} = \frac{R_6 (R_3 + R_4)}{R_3 (R_5 + R_6)} \cdot \frac{S^2}{S^2 + \frac{R_5 (R_3 + R_4)}{R_1 R_3 C_2 (R_5 + R_6)} S + \frac{R_4}{R_1 R_2 R_3 C_2 C_3}}$$

$$b) \frac{V_2}{V_i} = -\frac{G_1 G_5 (G_3 + G_4)}{C_2 G_4 (G_5 + G_6)} \cdot \frac{S}{S^2 + \frac{G_1 G_6 (G_3 + G_4)}{C_2 G_4 (G_5 + G_6)} S + \frac{G_1 G_2 G_3}{C_2 C_3 G_4}} = -\frac{R_6 (R_3 + R_4)}{R_1 R_3 C_2 (R_5 + R_6)} \cdot \frac{S}{S^2 + \frac{R_5 (R_3 + R_4)}{R_1 R_3 C_2 (R_5 + R_6)} S + \frac{R_4}{R_1 R_2 R_3 C_2 C_3}}$$

$$c) \frac{V_3}{V_i} = \frac{G_1 G_2 G_5 (G_3 + G_4)}{C_2 C_3 G_4 (G_5 + G_6)} \cdot \frac{1}{S^2 + \frac{G_1 G_6 (G_3 + G_4)}{C_2 G_4 (G_5 + G_6)} S + \frac{G_1 G_2 G_3}{C_2 C_3 G_4}} = \frac{R_6 (R_3 + R_4)}{R_1 R_2 R_3 C_2 C_3 (R_5 + R_6)} \cdot \frac{1}{S^2 + \frac{R_5 (R_3 + R_4)}{R_1 R_3 C_2 (R_5 + R_6)} S + \frac{R_4}{R_1 R_2 R_3 C_2 C_3}}$$

4)



$$\frac{V_1 - V_x}{R_1} = \frac{V_x - V_o}{R_4} + \frac{V_x}{R_3} + \frac{V_x}{Z_2}$$

$$\textcircled{1} \quad \frac{V_1 - V_x}{R_1} = -\frac{V_o}{R_4} + V_x \left(\frac{1}{R_4} + \frac{1}{R_3} + \frac{1}{Z_2} \right)$$

$$\frac{V_x}{R_3} = -\frac{V_o}{Z_2} \rightarrow V_x = -V_o \frac{R_3}{Z_2} \quad \textcircled{2}$$

~~$$\frac{V_o}{V_1} = -\frac{1}{C_2 C_5 R_1 R_3 s^2 + s(R_1 R_3 + R_1 R_4 + R_3 R_4)} + \frac{1}{C_2 C_5 R_3 R_4}$$~~

$$\frac{V_o}{V_1} = -\frac{1}{C_2 C_5 R_1 R_3} \frac{1}{s^2 + s \frac{(R_1 R_3 + R_1 R_4 + R_3 R_4)}{C_2 R_1 R_3 R_4}} + \frac{1}{C_2 C_5 R_3 R_4}$$

NOTA

Para $R_1 = R_3 = R_4 = 1 \Omega$ y $C_2 = 1 F$ y $C_5 = 0,01 F$.

$$H(s) = - \frac{100}{s^2 + 3s + 100}$$

$$\omega_0 = 10 \rightarrow \phi = \frac{10}{3} = 3,33$$

b) Para que $\omega_0 = 1000 \text{ rad/s} \rightarrow \omega_0^2 = 10^6 = \frac{1}{C_2 C_5 R_3 R_4}$ ①

$C_2 = 4700 \text{ pF}$ y $C_5 = 47 \text{ pF}$

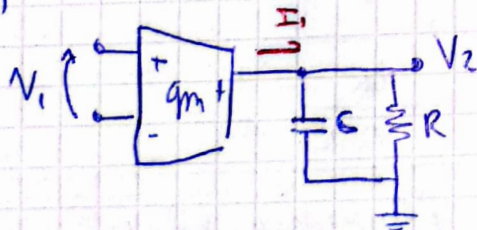
Si queremos mantener ϕ

$$\frac{\omega_0}{\phi} = 300 = \frac{(R_1 R_3 + R_1 R_4 + R_3 R_4)}{C_2 R_1 R_3 R_4}$$
 ②

de ① $\rightarrow 2,209 \cdot 10^{-3} = \frac{1}{R_3 R_4} \rightarrow R_3 R_4 = 4,526 \cdot 10^{12}$

Si $R_3 = R_4 \rightarrow R = 2,12 \text{ M}\Omega$

10)



$$I_1 = V_1 \cdot g_m$$

$$V_2 = V_1 \left(\frac{1}{sC} + R \right) g_m = V_1 \left(\frac{sCR + 1}{sC} \right) g_m$$

$$\frac{V_2}{V_1} = \frac{(sCR + 1) g_m}{sC}$$

$$\frac{V_2}{V_1} = R g_m \frac{s + \frac{1}{CR}}{s}$$