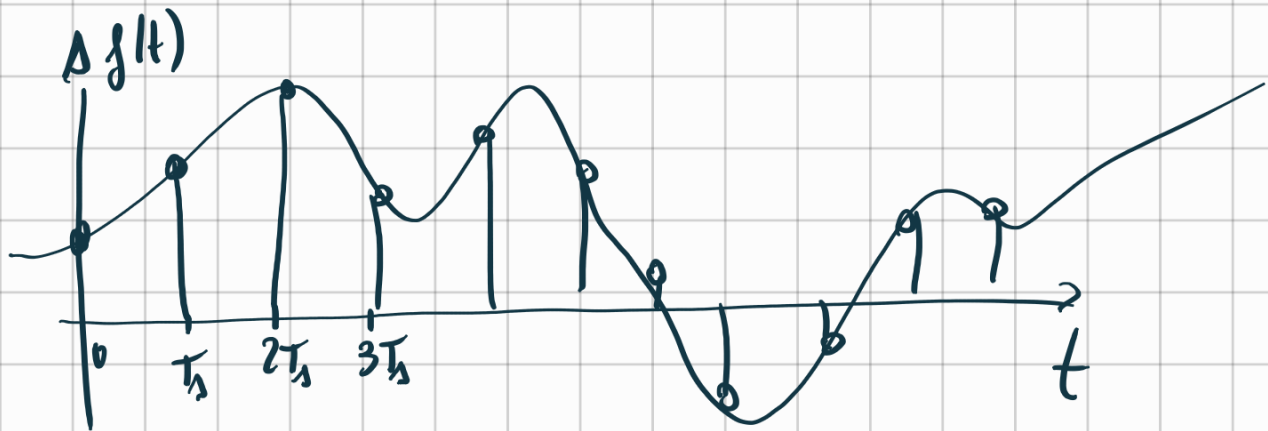


# Welcome to "Sistemas Multimedia"

2023-09-18



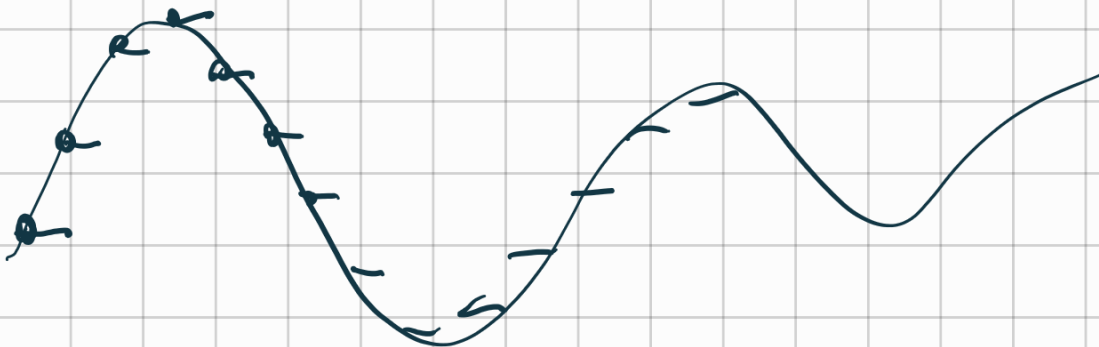
↓ sample

$$f(t) \rightarrow f(nT_s)$$

↑ sampling period

Quantize

$$f(nT_s) \approx \lfloor A f(nT_s) \rfloor$$



$$f(t) = \sin(\theta(t))$$

$$\theta(t) = 2\pi f_0 t$$

$$f_0 = \frac{1}{2\pi} \frac{d\theta(t)}{dt}$$

$$f(t) = \sin(2\pi f_0 t)$$

$$= \sin\left(2\pi \frac{f_0}{F_s} n\right)$$

$$t = nT_s = \frac{n}{F_s}$$

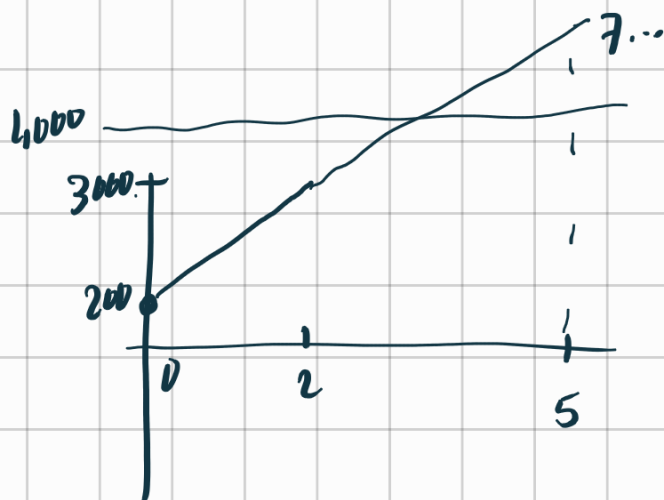
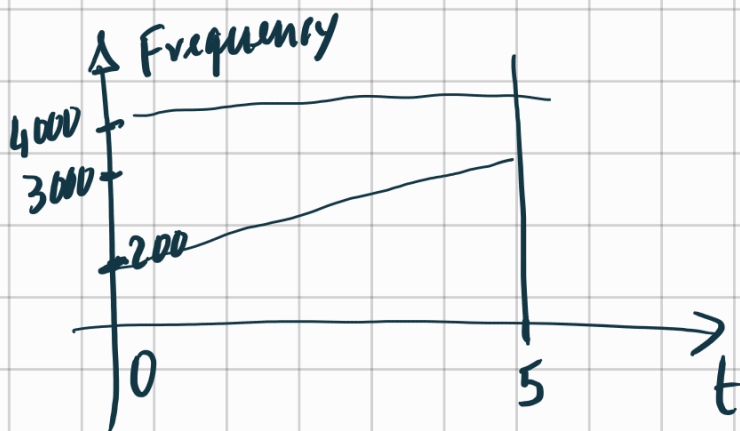
$\uparrow$  period       $\uparrow$  frequency

$$= \sin\left(2\pi \left(\frac{f_0}{F_s} + k\right) n\right)$$

$$\uparrow k \in \mathbb{Z}$$

Unique representation if  $\left|\frac{f_0}{F_s}\right| < \frac{1}{2}$

$$2|f_0| < F_s$$



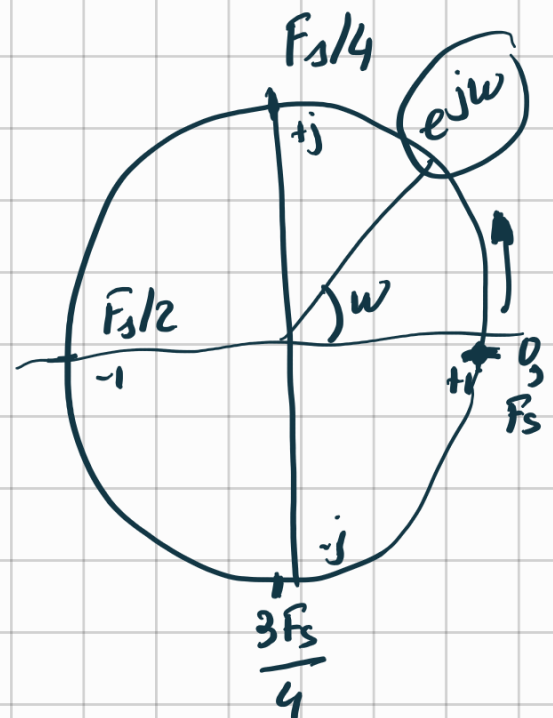
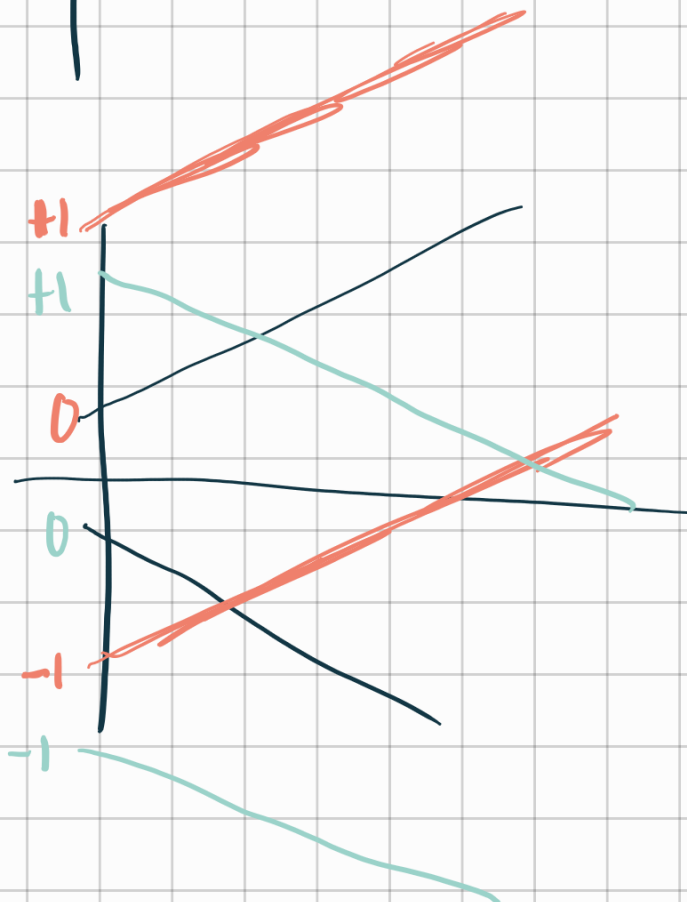
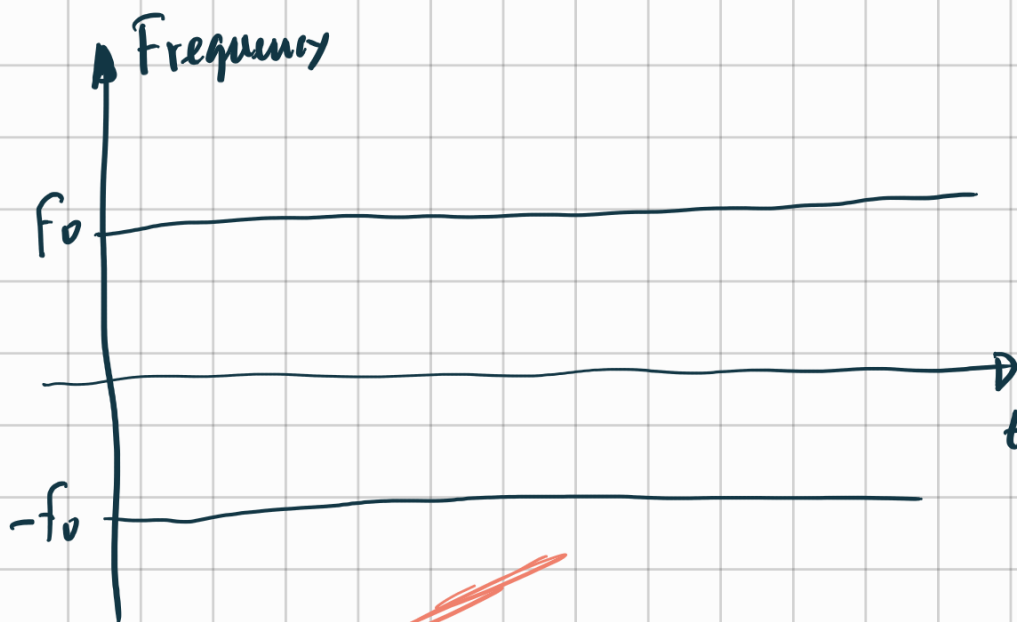
$$e^{ix} = \cos x + (i) \sin x$$

$$1i \quad 1j$$

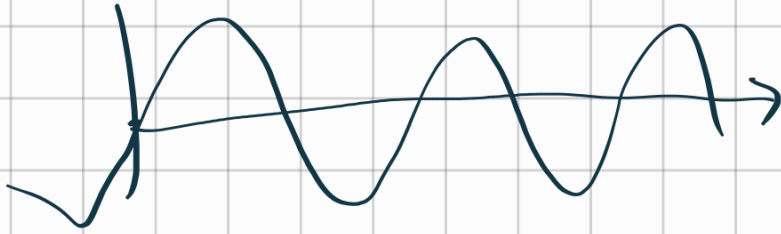
$$\cos x = \frac{e^{ix} + e^{-ix}}{2}$$

$$\sin x = \frac{e^{ix} - e^{-ix}}{2i}$$

$$\sin(2\pi f_0 t) = \frac{e^{j2\pi f_0 t} - e^{-j2\pi f_0 t}}{2j}$$



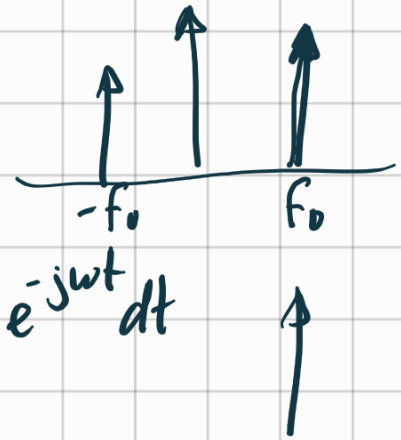
$$\sin(2\pi f_0 t)$$



Fourier

→  
transform

$$\frac{1}{2\pi} \int_{-\infty}^{+\infty} f(t) e^{-j\omega t} dt$$



limit

$$\frac{1}{h} \Lambda \xrightarrow{h \rightarrow 2h}$$