

Continuous but not Smooth

Find values of the constants a and b for which the following function is continuous but *not* differentiable.

$$f(x) = \begin{cases} ax + b, & x > 0; \\ \sin 2x, & x \leq 0. \end{cases}$$

In other words, the graph of the function should have a sharp corner at the point $(0, f(0))$.

for a function to be continuous,
 $\lim_{x \rightarrow 0} ax+b = \lim_{x \rightarrow 0} \sin 2x$
 it should be unbroken, which
 means that if we have a
 piecewise function, the next
 function should start where
 the other ends.

for a function to be not differentiable, the left and right $f'(x)$ should not be equal

$$\lim_{x \rightarrow 0^-} \sin x \neq \lim_{x \rightarrow 0^+} a$$

~~$\times \sin 2$~~ $\neq a$ and

$$b = 0$$

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$$\begin{aligned}\lim_{\Delta x \rightarrow 0} \frac{\Delta f}{\Delta x} &= \frac{\sin 2(x + \Delta x) - \sin 2(x)}{\Delta x} \\ &= \frac{\cancel{\sin 2x} + \cancel{\sin 2\cancel{x}} - \cancel{\sin 2x}}{\cancel{\Delta x}} \\ &\approx \sin 2\end{aligned}$$