

CZ2007 Introduction to Database Systems (Week 4)

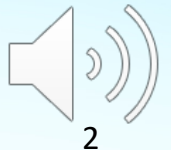
Topic 4: Third Normal Form (1)



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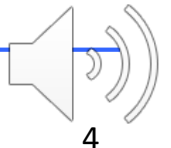
This Lecture

- 3NF ←
- 3NF Decomposition



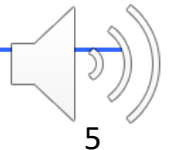
Third Normal Form (3NF)

- A relaxation of BCNF that
 - Is less strict
 - Allows decompositions that **always** preserve functional dependencies



First Normal Form (1NF)

- Key-attribute: An attribute in a multi-attribute key
 - ABC is key, then A, B, or C is key attribute
 - Key-attribute(s) = Partial key or part of a key; AB is partial key
- 1NF: All attributes have atomic values
- 2NF: Every non-key attribute is dependent on the whole of every candidate key
 - But, may still have (non-key-attribute X) \rightarrow (non-key-attribute Y) in the relation

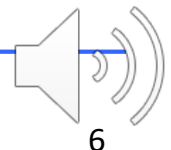


Second Normal Form (2NF)

- 2NF: Every non-key attribute is dependent on the whole of **EVERY** candidate key
 - But, **may still have (non-key-attribute X) \rightarrow (non-key-attribute Y) in the relation**
- Example:
 - Given FDs: $A \rightarrow B$, $A \rightarrow C$, $B \rightarrow C$
 - Key: {A}
 - Non-key attributes: B, C
 - $A \rightarrow B$ means B depends on key
 - $A \rightarrow C$ means C depends on key
 - But $B \rightarrow C$ means **non-key C depends on non-key B**
 - So R is in 2NF

R

A	B	C

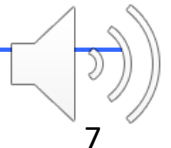


Third Normal Form (3NF)

- Definition: A table satisfies 3NF, if and only if for every non-trivial $X \rightarrow Y$
 - Either X contains a key (Y depends on key)
 - Or each attribute in Y is contained in a key (Y depends on key)
- Example:
 - Given FDs: $C \rightarrow B$, $AB \rightarrow C$, $BC \rightarrow C$
 - Keys: $\{AB\}$, $\{AC\}$
 - $AB \rightarrow C$ is OK, since AB is a key of R
 - $C \rightarrow B$ is OK, since B is part of AB
 - We ignore $BC \rightarrow C$ since it is trivial
 - So R is in 3NF

R

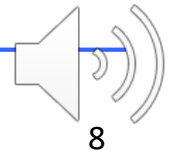
A	B	C



Third Normal Form (3NF)

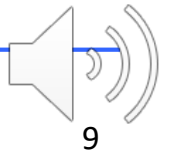
- Definition: A table satisfies 3NF, if and only if for every non-trivial $X \rightarrow Y$
 - Either X contains a key (X depends on key)
 - Or each attribute in Y is contained in a key (Y depends on key)
- Another Example:
 - Given FDs: $A \rightarrow B$, $B \rightarrow C$
 - Keys: {A}
 - $A \rightarrow B$ is OK, since A is a key of R
 - $B \rightarrow C$ is not OK, since B doesn't contain a key, and C is NOT in a key of R
 - So R is NOT in 3NF

R	A	B	C



3NF, BCNF

- 3NF: All attributes (key-attributes or non-key-attributes) depends (directly or transitively) on candidate keys
 - But candidate keys may have **overlapping** attributes
 - May result in key-attribute(s) of one key depends on key-attribute(s) of another key
- BCNF: In all dependencies (FDs), LHS must contain key (cannot depend on partial key)



3NF, BCNF

- 3NF: All attributes (key-attributes or non-key-attributes) depends (directly or transitively) on candidate keys
 - But candidate keys may have **overlapping** attributes
 - May result in key-attribute(s) of one key depends on key-attribute(s) of another key
- Example:
 - Given FDs: $C \rightarrow B$, $AB \rightarrow C$, $BC \rightarrow C$
 - Keys: $\{AB\}$, $\{AC\}$
 - Key-attributes: A , B , C
 - R is in 3NF but $C \rightarrow B$ means partial key B depends on partial key C
- BCNF: In all dependencies (FDs), LHS must contain key (cannot depend on partial key)

R

A	B	C

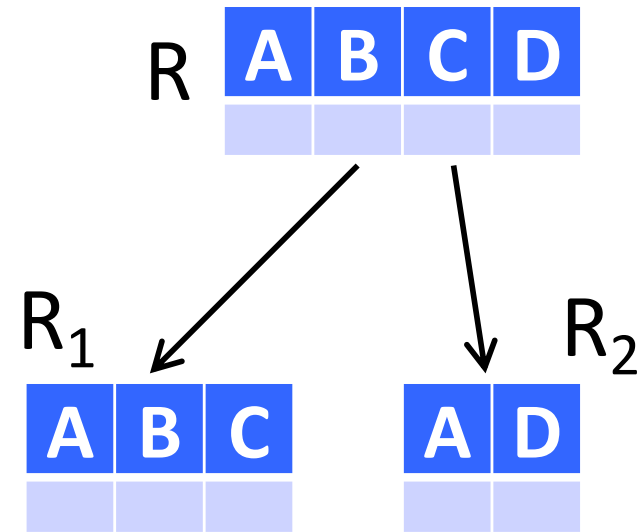
This Lecture

- 3NF
- 3NF Decomposition



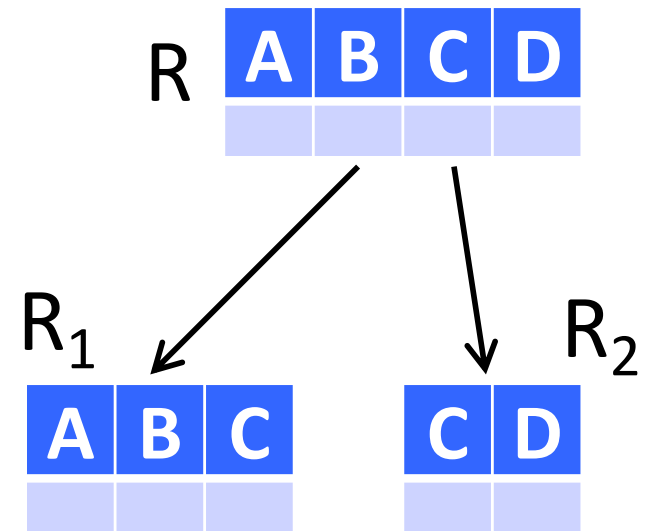
3NF Decomposition

- Given: A table NOT in 3NF
- Objective: Decompose it into smaller tables that are in 3NF
- Example
 - Given: $R(A, B, C, D)$
 - FDs: $AB \rightarrow C$, $C \rightarrow B$, $A \rightarrow D$
 - Keys: $\{AB\}$, $\{AC\}$
 - **R is not in 3NF, due to $A \rightarrow D$**
 - 3NF decomposition of R :
 $R_1(A, B, C)$, $R_2(A, D)$



3NF Decomposition Algorithm

- Given: A table R, and a set S of FDs
 - e.g., $R(A, B, C, D)$
 $S = \{A \rightarrow BD, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Step 1: Derive a **minimal basis** of S
 - e.g., a minimal basis of S is $\{A \rightarrow B, A \rightarrow C, C \rightarrow D\}$
- Step 2: In the minimal basis, combine the FDs whose left hand sides are the same
 - e.g., after combining $A \rightarrow B$ and $A \rightarrow C$, we have $\{A \rightarrow BC, C \rightarrow D\}$
- Step 3: Create a table for each FD remained
 - $R_1(A, B, C), R_2(C, D)$
- Step 4: If none of the tables contain a key of the original table R, create a table that contains a key of R
- Step 5: Remove redundant tables



Minimal Basis

- Given a set S of FDs, the **minimal basis** of S is a **simplified** version of S
- Previous example:
 - $S = \{A \rightarrow BD, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
 - A minimal basis: $\{A \rightarrow B, A \rightarrow C, C \rightarrow D\}$
- How simplified?
- Three conditions.
- **Condition 1: For any FD in the minimal basis, its right hand side has only one attribute.**
- Example in S : $A \rightarrow BD$ does not satisfy this condition
- That is why $A \rightarrow BD$ is not in the minimal basis

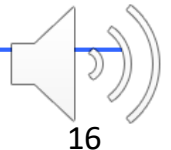


Minimal Basis

- Previous example:
 - $S = \{A \rightarrow BD, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
 - A minimal basis: $\{A \rightarrow B, A \rightarrow C, C \rightarrow D\}$
- Condition 2: No FD in the minimal basis is redundant.
- That is, no FD in the minimal basis can be derived from the other FDs.
- Example in S: $BC \rightarrow D$ can be derived from $C \rightarrow D$
- That is why $BC \rightarrow D$ is not in the minimal basis

Minimal Basis

- Previous example:
 - $S = \{A \rightarrow BD, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
 - A minimal basis: $\{A \rightarrow B, A \rightarrow C, C \rightarrow D\}$
- **Condition 3:** For each FD in the minimal basis, none of the attributes on the left hand side is redundant
- That is, for any FD in the minimal basis, if we remove an attribute from the left hand side, then the resulting FD is a new FD that cannot be derived from the original set of FDs
- Example:
 - S contains $AB \rightarrow C$
 - If we remove B from the left hand side, we have $A \rightarrow C$
 - $A \rightarrow C$ can be derived from S, as $\{A\}^+ = \{ABDC\}$
 - This indicates that $A \rightarrow C$ is “hidden” in S
 - Hence, we can replace $AB \rightarrow C$ with $A \rightarrow C$, as $A \rightarrow C$ is “simpler”
 - This is why $AB \rightarrow C$ is not in the minimal basis



Algorithm for Minimal Basis

- Given: a set S of FDs
- Example: $S = \{A \rightarrow BD, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Step 1: Transform the FDs, so that each right hand side contains only one attribute
- Result: $S = \{A \rightarrow B, A \rightarrow D, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Reason:
 - Condition 1 for minimal basis:
The right hand side of each FD contains only one attribute



Algorithm for Minimal Basis

- Result of Step 1:
 - $S = \{A \rightarrow B, A \rightarrow D, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Step 2: Remove redundant FDs
- Is $A \rightarrow B$ redundant?
- i.e., is $A \rightarrow B$ implied by other FDs in S ?
- Let's check
- Without $A \rightarrow B$, we have $\{A \rightarrow D, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Given those FDs, we have $\{A\}^+ = \{AD\}$, which does not contain B
- Therefore, $A \rightarrow B$ is not implied by the other FDs

Algorithm for Minimal Basis

- Result of Step 1:
 - $S = \{A \rightarrow B, A \rightarrow D, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Continue Step 2: Remove redundant FDs
- Is $A \rightarrow D$ redundant?
- i.e., is $A \rightarrow D$ implied by other FDs in S ?
- Let's check
- Without $A \rightarrow D$, we have $\{A \rightarrow B, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Given those FDs, we have $\{A\}^+ = \{ABCD\}$, which contains D
- Therefore, $A \rightarrow D$ is implied by the other FDs
- Hence, $A \rightarrow D$ is redundant and should be removed
- Result: $S = \{A \rightarrow B, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$



Algorithm for Minimal Basis

- Result of the last step:
 - $S = \{A \rightarrow B, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Continue Step 2: Remove redundant FDs
- Is $AB \rightarrow C$ redundant?
- i.e., is $AB \rightarrow C$ implied by other FDs in S ?
- Let's check
- Without $AB \rightarrow C$, we have $\{A \rightarrow B, C \rightarrow D, BC \rightarrow D\}$
- Given those FDs, we have $\{AB\}^+ = \{AB\}$, which does not contain C
- Therefore, $AB \rightarrow C$ is NOT implied by the other FDs
- Hence, $AB \rightarrow C$ is not redundant and should not be removed

Algorithm for Minimal Basis

- Result of the last step:
 - $S = \{A \rightarrow B, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Continue Step 2: Remove redundant FDs
- Is $C \rightarrow D$ redundant?
- i.e., is $C \rightarrow D$ implied by other FDs in S ?
- Let's check
- Without $C \rightarrow D$, we have $\{A \rightarrow B, AB \rightarrow C, BC \rightarrow D\}$
- Given those FDs, we have $\{C\}^+ = \{C\}$, which does not contain D
- Therefore, $C \rightarrow D$ is NOT implied by the other FDs and should not be removed

Algorithm for Minimal Basis

- Result of the last step:
 - $S = \{A \rightarrow B, AB \rightarrow C, C \rightarrow D, BC \rightarrow D\}$
- Continue Step 2: Remove redundant FDs
- Is $BC \rightarrow D$ redundant?
- i.e., is $BC \rightarrow D$ implied by other FDs in S ?
- Let's check
- Without $BC \rightarrow D$, we have $\{A \rightarrow B, AB \rightarrow C, C \rightarrow D\}$
- Given those FDs, we have $\{BC\}^+ = \{BCD\}$, which contains D
- Therefore, $BC \rightarrow D$ is implied by the other FDs
- Hence, $BC \rightarrow D$ is redundant and should be removed
- Result: $S = \{A \rightarrow B, AB \rightarrow C, C \rightarrow D\}$

Algorithm for Minimal Basis

- Result of Step 2:
 - $S = \{A \rightarrow B, AB \rightarrow C, C \rightarrow D\}$
- Step 3: Remove redundant attributes on the left hand side (lhs) of each FD
- Only $AB \rightarrow C$ has more than one attribute on the lhs
- Let's check
- Is A redundant?
- If we remove A, then $AB \rightarrow C$ becomes $B \rightarrow C$
- Whether this removal is OK depends on whether $B \rightarrow C$ is “hidden” in S already
- If $B \rightarrow C$ is “hidden” in S, then the removal of A is OK, (since the removal does not add extraneous information into S)
- Is $B \rightarrow C$ “hidden” in S?
- Check: Given S, we have $\{B\}^+ = \{B\}$, which does NOT contain C
- Therefore, $B \rightarrow C$ is not “hidden” in S, and hence, A is NOT redundant



Algorithm for Minimal Basis

- **Result** of Step 2:
 - $S = \{A \rightarrow B, AB \rightarrow C, C \rightarrow D\}$
- **Step 3: Remove redundant attributes on the left hand side (lhs) of each FD**
- Only $AB \rightarrow C$ has more than one attribute on the lhs
- Let's check
- Is B redundant?
- If we remove B, then $AB \rightarrow C$ becomes $A \rightarrow C$
- Whether this is OK depends on whether $A \rightarrow C$ is “hidden” in S
- Is $A \rightarrow C$ “hidden” in S?
- Check: Given S, we have $\{A\}^+ = \{ABCD\}$, which contains C
- Therefore, $A \rightarrow C$ is “hidden” in S
- Hence, we can simplify $AB \rightarrow C$ to $A \rightarrow C$
- Final minimal basis: $S = \{A \rightarrow B, A \rightarrow C, C \rightarrow D\}$



To continue in

Topic 4: Third Normal Form (2)

