

Analysis of cytolytic immunity models

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Overview

This document goes over the analysis of the model results from the main model described in the manuscript: CMV infection with cytolytic immune response (see `model_code_documentation/CMV_Models.pdf` for equations and code). The immune parameters for this model are fit across the entire episode for each infant. The `beta` and `start_time` parameters were fit to the expansion phase only in a prior analysis to estimate R_0 (see first results section of `target_cell_model_analysis.pdf` for that).

This document and code generated the results presented for publication: Figures 3 and 4 come from here. This is how the analysis was broken down:

1. Assesment of optimized parameter values and model fit
2. Model results interpretation through simulation using best fits and estimation of infected cell lifespan with immune response
3. Estimation of effective reproduction number, R , to evaluate critical time points during infection
4. Check on epithelial cell loss

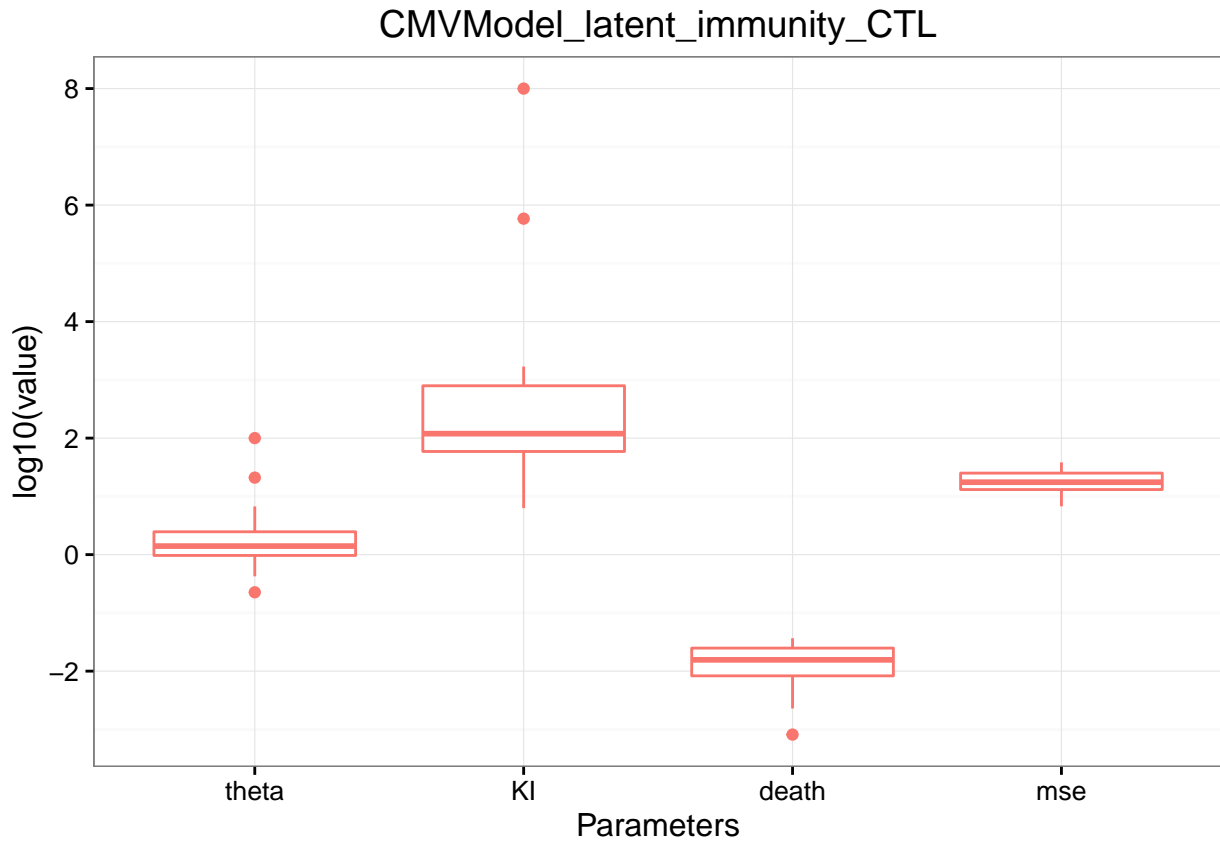
Model optimization and results

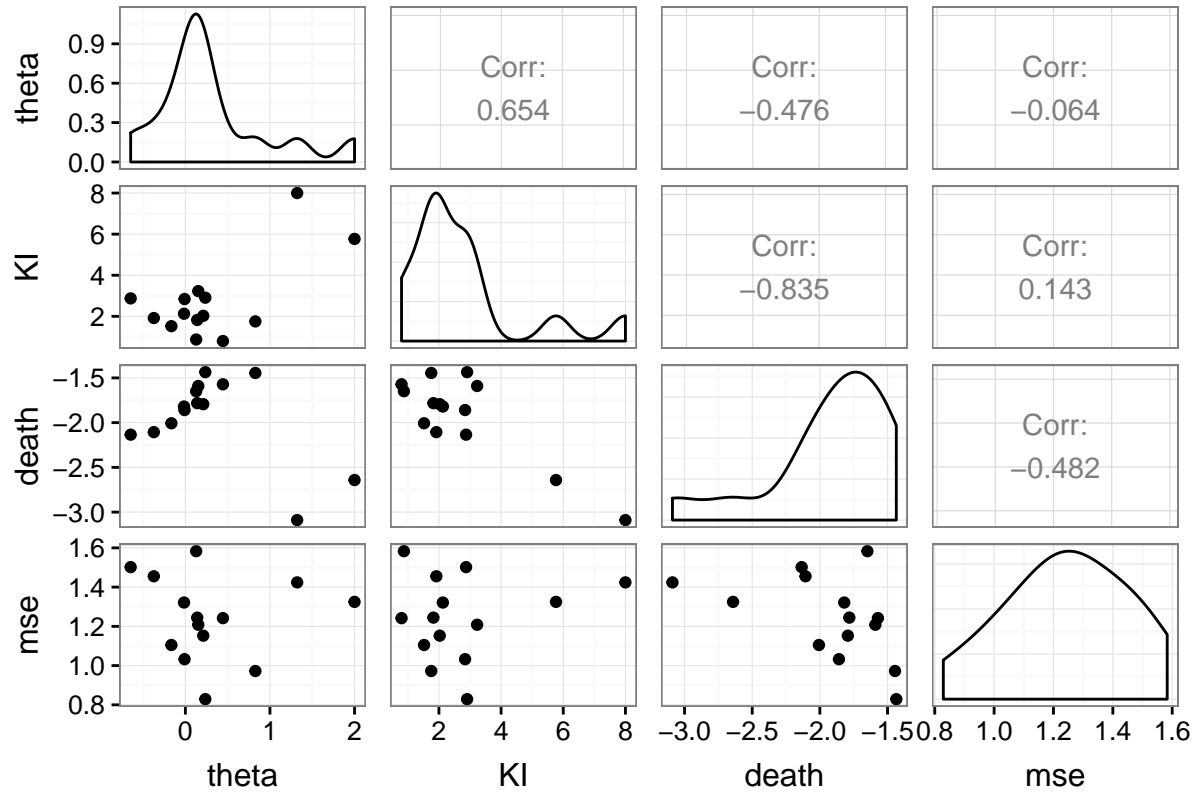
Model parameters were estimated for each infant episode after initializing. Subject by subject parameters and model fits appear in the results_figures/

Fitted model parameters

| | PatientID2 | theta | log10KI | gammaX100 | mse |
|----|------------|--------|---------|-----------|-------|
| 1 | A | 1.34 | 0.87 | 2.24 | 38.30 |
| 2 | B | 0.23 | 2.87 | 0.73 | 31.76 |
| 3 | C | 0.42 | 1.92 | 0.78 | 28.53 |
| 4 | D | 20.97 | 8.00 | 0.08 | 26.54 |
| 5 | E | 0.98 | 2.84 | 1.38 | 10.78 |
| 6 | F | 2.78 | 0.80 | 2.68 | 17.45 |
| 7 | G | 1.42 | 3.23 | 2.57 | 16.15 |
| 8 | H | 100.00 | 5.77 | 0.23 | 21.13 |
| 9 | I | 0.68 | 1.52 | 0.98 | 12.73 |
| 10 | J | 1.38 | 1.82 | 1.65 | 17.56 |
| 11 | K | 0.96 | 2.13 | 1.51 | 20.96 |
| 12 | L | 1.63 | 2.03 | 1.61 | 14.21 |
| 13 | M | 6.72 | 1.75 | 3.59 | 9.39 |
| 14 | N | 1.72 | 2.91 | 3.67 | 6.74 |

Table 1: Supplementary Table - Fits from cytolytic immune model





Simulated data fit compared to episode data (Figure 3)

(also saves figure results_figures/CTL_model_fits.pdf that displays parameter values, R0 along with time series plots. This chunk has eval = F in the code.)

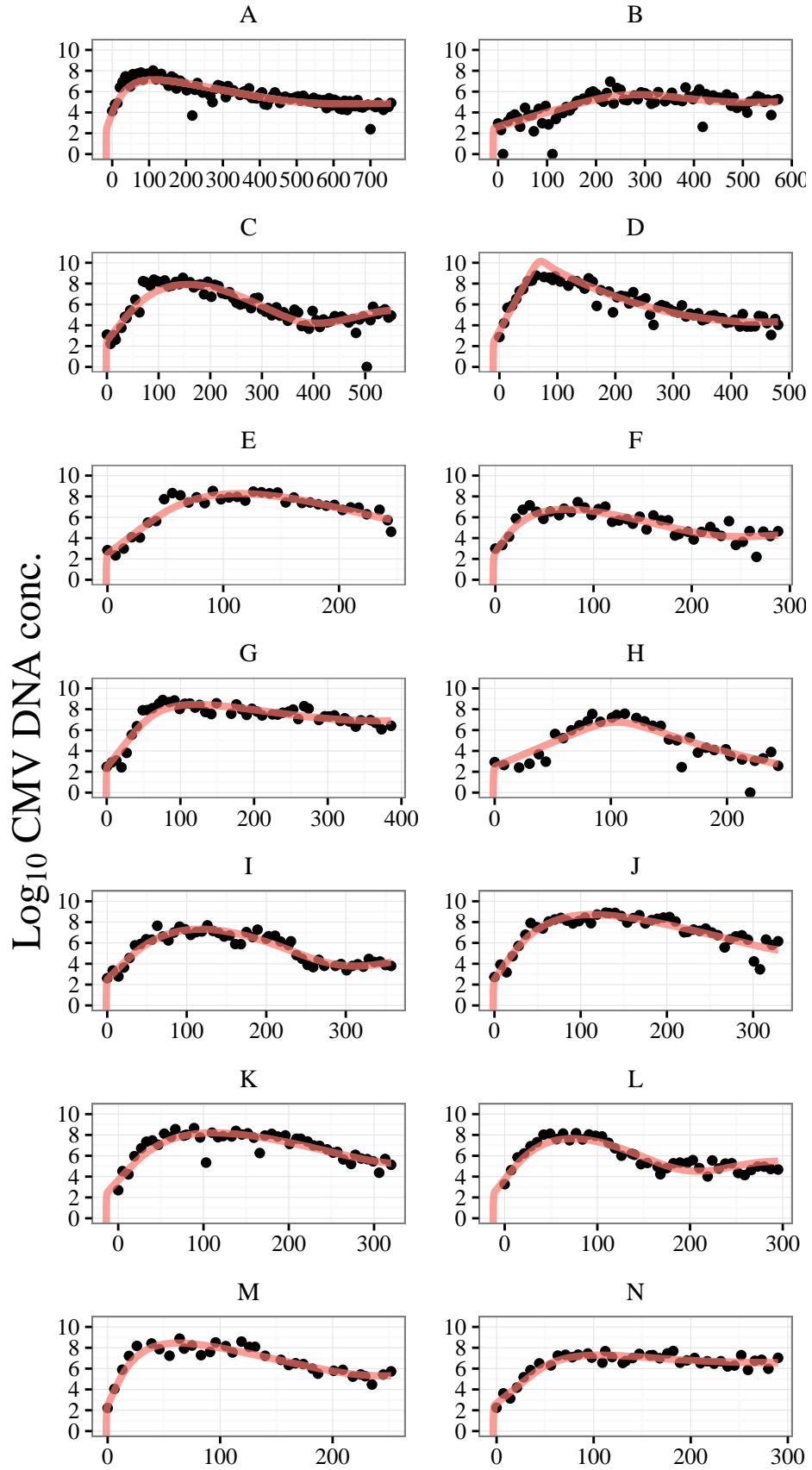


Figure 1: Best immune model fits

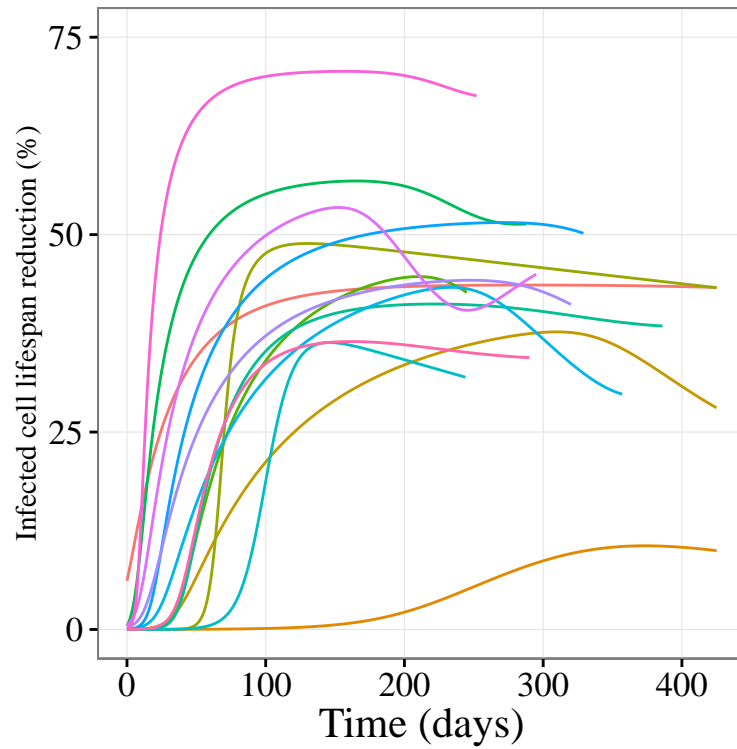
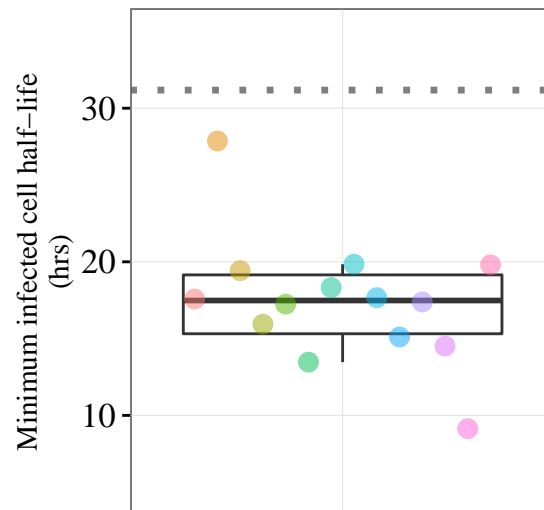


Figure 2: Immune pressure over time on infected cell lifespan

Infected cell lifespan with immune pressure

Time series plots of immune pressure

Magnitude of peak response (shortest infected cell lifespan)



| PatientID2 | minimum_lifespan_hrs | maximum_reduction_pct |
|------------|----------------------|-----------------------|
| A | 17.57 | 43.61 |
| B | 27.87 | 10.59 |
| C | 19.42 | 37.68 |
| D | 15.93 | 48.88 |
| E | 17.24 | 44.68 |
| F | 13.47 | 56.79 |
| G | 18.32 | 41.21 |
| H | 19.84 | 36.34 |
| I | 17.66 | 43.33 |
| J | 15.11 | 51.53 |
| K | 17.39 | 44.22 |
| L | 14.51 | 53.44 |
| M | 9.14 | 70.68 |
| N | 19.80 | 36.46 |

Table 2: Maximum immune pressure effect on infected cell lifespan (compared to 31 hours without immunity)

| variable | median | IQR | range |
|-----------------------|--------|----------------|---------------|
| minimum_lifespan_hrs | 17.48 | 15.314, 19.149 | 9.139, 27.867 |
| maximum_reduction_pct | 43.92 | 38.564, 50.866 | 10.593, 70.68 |

Table 3: Summary of maximum immune pressure effect on infected cell lifespan (compared to 31 hours without immunity)

Time of peak response (when shortest infected cell lifespan)

Effective reproduction number

Clearance phase initiation and effective $R == 1$

When effective R crosses 1 for the first time, that initiates clearance. This matches with the peak viral load day predicted in the model as expected (with some round error)

Comparing clearance phase initiation and peak immune response day

Clearance phase initiation equivalent to first day that $R = 1$. It happens much earlier than the peak immune pressure day.

Minimum effective R vs R_0

Effective R over time

Immune effect on epithelial cell population

Only one of the model predicts substantial population depletion

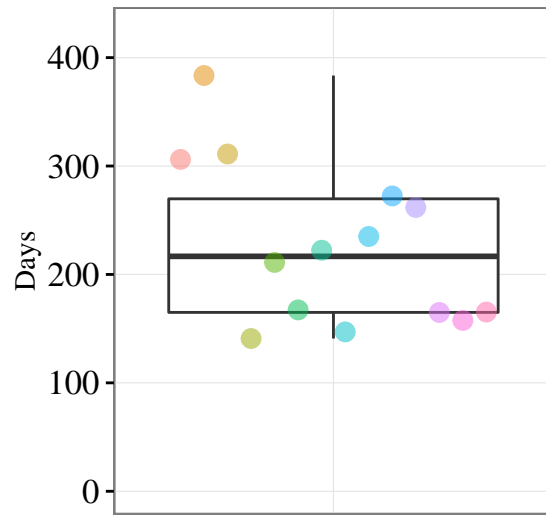


Figure 3: distribution of peak immune pressure

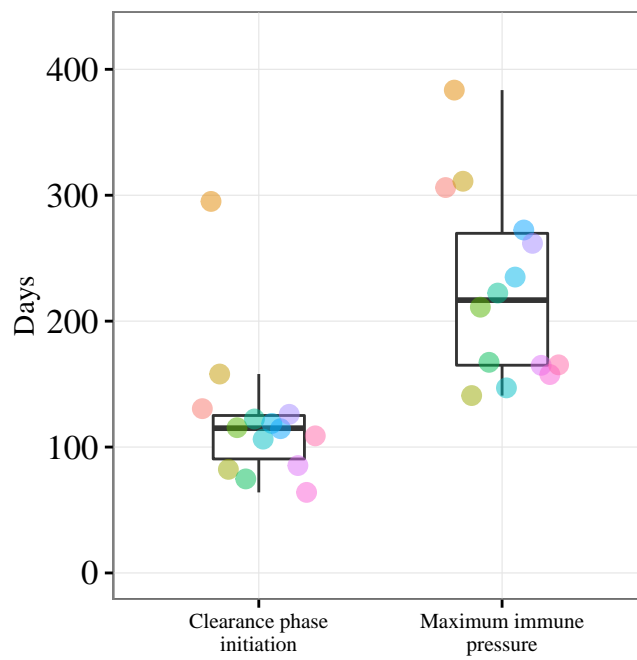


Figure 4: distribution of days for critical immune times

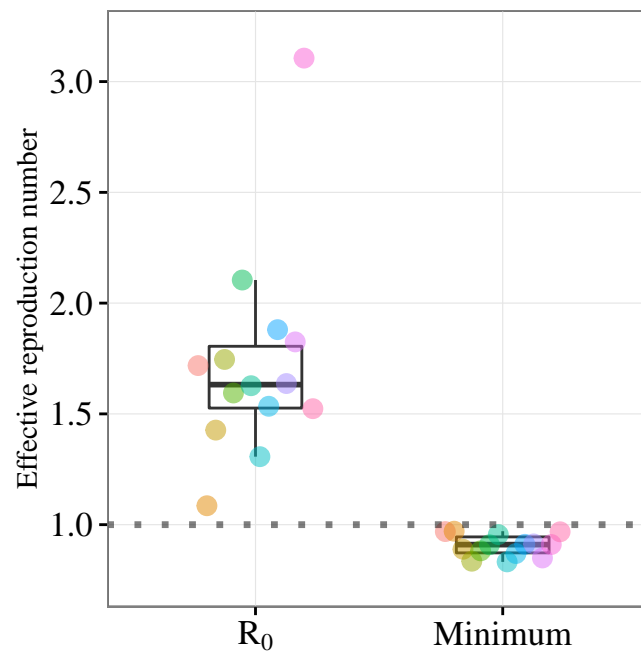


Figure 5: R_0 vs minimum R

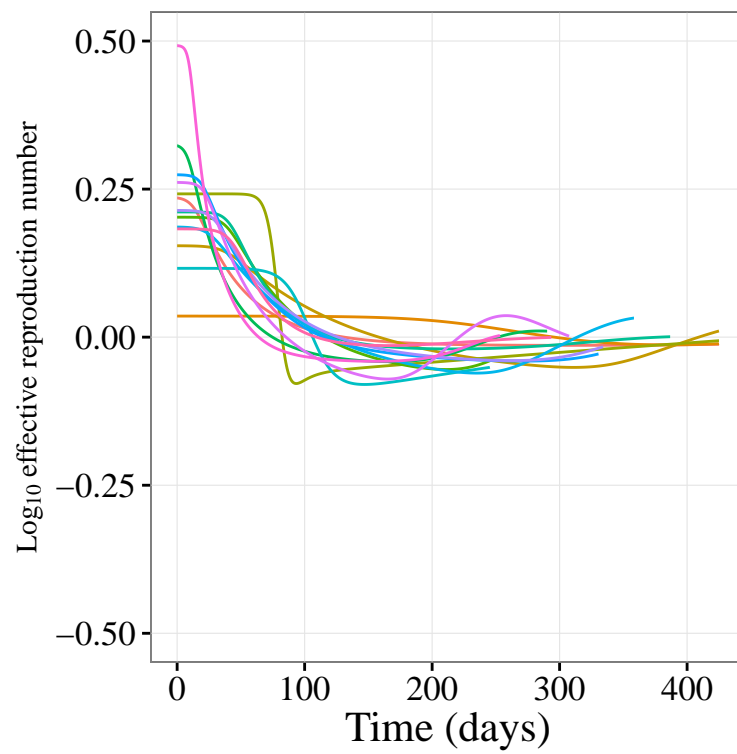


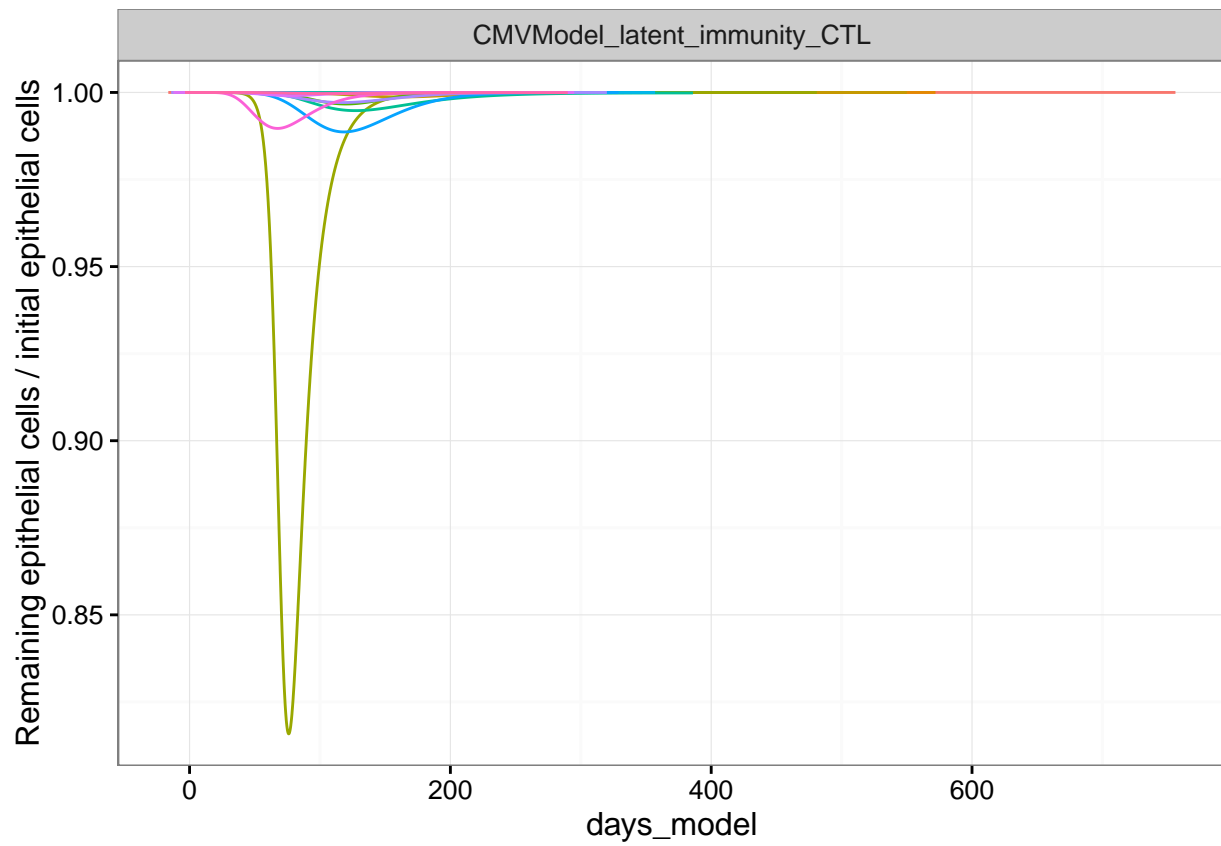
Figure 6: Immune pressure over time on infected cell lifespan

| PatientID2 | peak_immune_day |
|------------|-----------------|
| A | 306.10 |
| B | 383.50 |
| C | 311.10 |
| D | 140.90 |
| E | 211.10 |
| F | 167.30 |
| G | 222.30 |
| H | 147.00 |
| I | 235.00 |
| J | 272.40 |
| K | 261.80 |
| L | 164.90 |
| M | 157.60 |
| N | 165.30 |

Table 4: Day of peak immune pressure

| median | IQR | range |
|--------|-------------|--------------|
| 216.70 | 165, 269.75 | 140.9, 383.5 |

Table 5: Summary stats for day of immune pressure



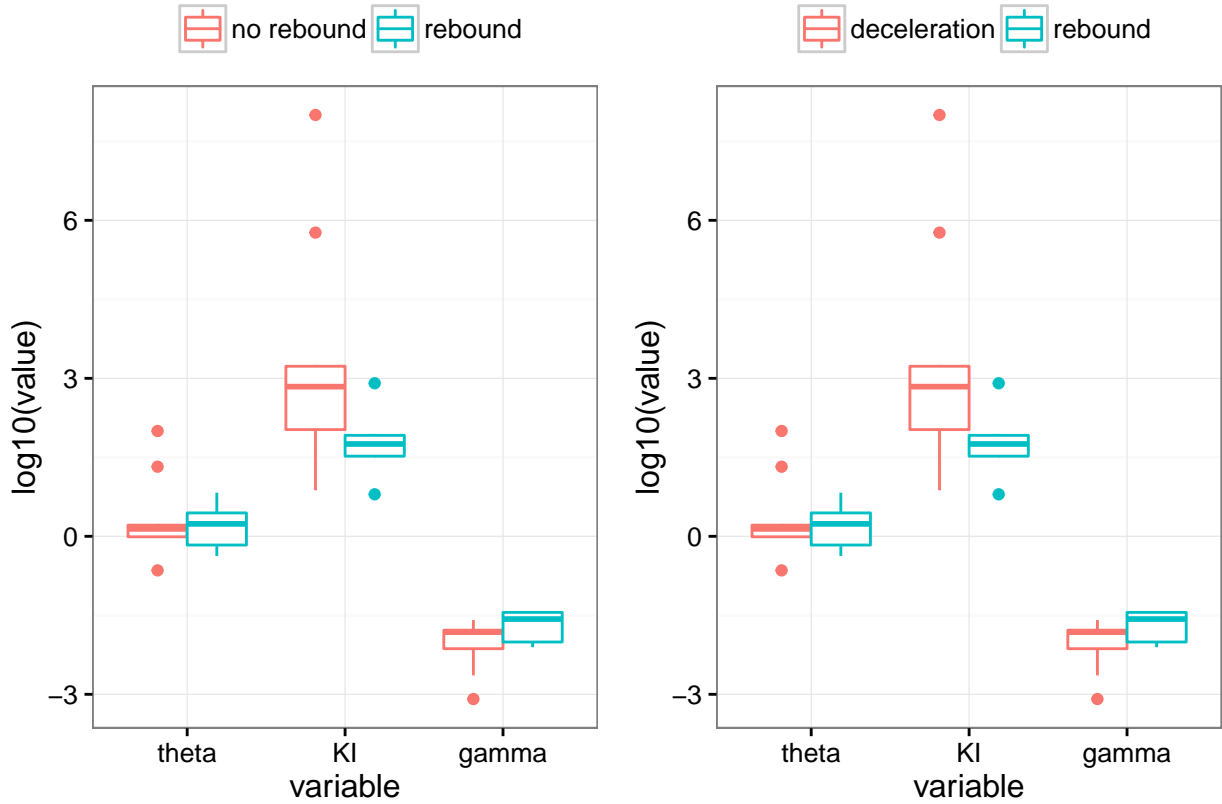
| PatientID2 | peak_viral_day | effectiveR_eq1_day |
|------------|----------------|--------------------|
| A | 130.90 | 130.50 |
| B | 295.80 | 295.10 |
| C | 158.20 | 158.00 |
| D | 82.50 | 82.30 |
| E | 115.40 | 115.40 |
| F | 74.60 | 74.70 |
| G | 122.40 | 122.30 |
| H | 106.30 | 106.30 |
| I | 118.80 | 118.80 |
| J | 114.70 | 114.60 |
| K | 126.10 | 126.00 |
| L | 85.20 | 85.30 |
| M | 63.80 | 64.00 |
| N | 109.10 | 108.90 |

Table 6: Day of peak viral load (clearance start) and when $R = 1$

| variable | median | IQR | range |
|--------------------|--------|-----------------|-------------|
| peak_viral_day | 115.05 | 90.475, 125.175 | 63.8, 295.8 |
| effectiveR_eq1_day | 115.00 | 90.55, 125.075 | 64, 295.1 |

Table 7: Summary stats for day of peak viral load (clearance start) and when $R = 1$

Rebound parameters



| PatientID2 | R0 | minR |
|------------|------|------|
| A | 1.72 | 0.97 |
| B | 1.09 | 0.97 |
| C | 1.43 | 0.89 |
| D | 1.75 | 0.84 |
| E | 1.59 | 0.88 |
| F | 2.10 | 0.91 |
| G | 1.63 | 0.96 |
| H | 1.31 | 0.83 |
| I | 1.53 | 0.87 |
| J | 1.88 | 0.91 |
| K | 1.64 | 0.91 |
| L | 1.82 | 0.85 |
| M | 3.11 | 0.91 |
| N | 1.52 | 0.97 |

Table 8: R0 and minimum effective R

| variable | median | IQR | range |
|----------|--------|--------------|--------------|
| R0 | 1.632 | 1.526, 1.805 | 1.085, 3.106 |
| minR | 0.910 | 0.873, 0.945 | 0.832, 0.97 |

Table 9: Summary stats for R0 and minimum effective R

Save output data and figures.

See code for this.

| PatientID2 | max_loss |
|------------|----------|
| A | 0.000 |
| B | 0.000 |
| C | 0.001 |
| D | 0.146 |
| E | 0.003 |
| F | 0.000 |
| G | 0.004 |
| H | 0.000 |
| I | 0.000 |
| J | 0.009 |
| K | 0.002 |
| L | 0.001 |
| M | 0.008 |
| N | 0.000 |

Table 10: Maximum cell loss (percent)

| median_pct_loss | range_pct_loss |
|-----------------|----------------|
| 0.001 | 0, 0.146 |

Table 11: Summary of maximum cell loss (percent)

| rebound_cat | median theta | median log10 KI) | median effector lifespan (1/gamma) |
|-------------|--------------|------------------|------------------------------------|
| no rebound | 1.38 | 2.84 | 66.05 |
| rebound | 1.72 | 1.75 | 37.27 |

Table 12: Immune parameter differences by rebound status (two category)

| rebound_cat2 | median theta | median log10 KI) | median effector lifespan (1/gamma) |
|--------------|--------------|------------------|------------------------------------|
| deceleration | 1.38 | 2.84 | 66.05 |
| rebound | 1.72 | 1.75 | 37.27 |

Table 13: Immune parameter differences by rebound status