Machine Learning In Action — Chapter 2

Example 2.1

In this example, the parameters are

$$k = 3,$$
 $in_X = \begin{pmatrix} 0.6 & 0.6 \end{pmatrix},$ $data_set = \begin{pmatrix} 1.0 & 1.1 \\ 1.0 & 1.0 \\ 0.0 & 0.0 \\ 0.0 & 0.1 \end{pmatrix},$ $labels = \begin{pmatrix} A \\ A \\ B \\ B \end{pmatrix}$

Using the above arguments,

$$diff_matrix = \mathbf{tile} \left(in_X, (\mathbf{4}, \mathbf{1}) \right) - data_set$$

$$= \begin{pmatrix} 0.6 & 0.6 \\ 0.6 & 0.6 \\ 0.6 & 0.6 \end{pmatrix} - \begin{pmatrix} 1.0 & 1.1 \\ 1.0 & 1.0 \\ 0.0 & 0.0 \\ 0.0 & 0.1 \end{pmatrix}$$

$$= \begin{pmatrix} -0.4 & -0.5 \\ -0.4 & -0.4 \\ 0.6 & 0.6 \\ 0.6 & 0.5 \end{pmatrix}$$

and $diff_matrix$ represent the straight line distance the vector is from the other data points in the set. To calculate the Euclidean Distance, take the square of every element in $diff_matrix$, sum them across the rows, then take the square root.

$$sq_diff_matrix = \begin{pmatrix} 0.16 & 0.25 \\ 0.16 & 0.16 \\ 0.36 & 0.36 \\ 0.36 & 0.25 \end{pmatrix}, sq_distances = \begin{pmatrix} 0.41 \\ 0.32 \\ 0.72 \\ 0.61 \end{pmatrix}$$

Finally,

$$distances = \begin{pmatrix} 0.64031 \\ 0.56568 \\ 0.84852 \\ 0.78102 \end{pmatrix}, sorted_dist_indices = \begin{pmatrix} 1 \\ 0 \\ 3 \\ 2 \end{pmatrix}$$

Taking the first 3 labels, we can see that there are 2 data points labelled A and 1 data point labelled B. Hence, by majority, the data point $in_{-}X$ is classified in group A.