1.

$$\bar{c} = 3$$

$$s_c^2 = \frac{1}{9} \sum_{i=1}^{10} (c_i - 3)^2 = \frac{16}{9}$$

standard error =
$$s_c \sqrt{l} = \frac{16}{9} * \sqrt{9} = \frac{16}{9} * 3 = \frac{16}{3} = 5.333$$

In the video, $\frac{16}{9}$ is stated to equal $\frac{4}{3}$, but this is not true.

2.

$$\hat{\mu}_c = 2.25$$

$$\hat{y}_5 = 12 + 2.25 = 14.25$$

$$\hat{y}_6 = 15 + 2.25 = 17.25$$

$$\hat{y}_7 = 21 + 2.25 = 23.25$$

$$ME = \frac{(15 - 14.25) + (21 - 17.25) + (22 - 23.25)}{3} = 1.083$$

$$MSE = \frac{(15 - 14.25)^2 + (21 - 17.25)^2 + (22 - 23.25)^2}{3} = 5.3958$$

$$5.3958 - 1.083 = 4.31$$

The answer is B.

3.

For an AR(1) model, it is possible for β_0 to equal 1.

The answer is A, as it is the only false answer.

4.

Since it is a stationary AR(1) model, $|\beta_1| < 1$ is always true.

The answer is E.

$$\bar{y} = 4.25$$

$$\beta_1 = \frac{\sum_{t=2}^T (y_{t-1} - \bar{y})(y_t - \bar{y})}{\sum_{t=2}^T (y_t - \bar{y})^2}$$

$$\beta_1 = 0.366796$$

$$\beta_0 = 4.25(1 - 0.366795) = 2.69112$$

6.

$$\bar{y} = 40$$

$$\beta_1 = \frac{\sum_{t=2}^{T} (y_{t-1} - \bar{y})(y_t - \bar{y})}{\sum_{t=2}^{T} (y_t - \bar{y})^2} = \frac{117}{262} = 0.4466$$

$$\beta_0 = 40(1 - 0.4466) = 22.1374$$

$$e_2 = -0.9806$$

$$e_3 = -0.767$$

$$e_4 = 2.3398$$

$$e_5 = 4.5534$$

$$e_6 = 8.767$$

$$\bar{e} = 2.7825$$

$$s^2 = \frac{\sum_{t=2}^{6} (e_t - \bar{e})^2}{6 - 3} = 21.97 = 22$$

The answer is C.

7.

Calculating up to the five step ahead forecast.

$$y_t = 0.6t_{t-1} - 5 + \epsilon$$

$$y_T = 7$$

$$y_{T+1} = -5 + (0.6 * 7) = -0.8$$

$$y_{T+2} = -5 + 0.6(-0.8) = -5.48$$

$$y_{T+3} = -8.288$$

$$y_{T+4} = -9.9728$$

$$y_{T+5} = -10.9837$$

8.

$$\hat{s}_5 = \frac{13 + 8}{2} = 10.5$$

$$\hat{y}_{5+1} = \hat{s}_5 = 10.5$$

9.

$$\hat{s}_2 = 0.2(3) + 0.8(1) = 1.4$$

$$\hat{s}_3 = 0.2(5) + 0.8(1.4) = 2.12$$

$$\hat{s}_4 = 0.2(8) + 0.8(2.12) = 3.296$$

$$\hat{s}_5 = 0.2(13) + 0.8(3.296) = 5.2368$$

$$\hat{y}_{5+1} = \hat{s}_5 = 5.2368$$

10.

$$\hat{s}_{100} = \hat{y}_{102} = 0.2(100.2) + 0.8(95.1) = 96.12$$

$$\hat{s}_{99}^{(2)} = 0.2(95.1) + 0.8(89.9) = 90.94$$

$$\hat{\mathbf{s}}_{100}^{(2)} = 0.2(96.12) + 0.8(90.94) = 91.976$$

$$\beta_0 = 2(96.12) - 91.976 = 100.264$$

$$\beta_1 = \frac{0.2}{0.8}(96.12 - 91.976) = 1.036$$

$$\hat{y}_{102} = 100.264 + 1.036(2) = 102.336$$

$$103.336 - 91.976 = 6.216$$

The answer is D.