1.

Since this is a classification problem, the prediction will be the majority vote.

Thus, the final prediction is that the customer would make a claim on the policy.

2.

Tree 1 prediction: Claim amount of 100k

Tree 2 prediction: Claim amount of 70k

Tree 3 prediction: Claim amount of 30k

The final prediction is the average, which is $\frac{100+70+30}{3}=66.67$

Thus the final prediction is 66.67k

3.

a. The prediction of the first round is the average of y

| Х | У | Pred1 |
|----|---|----------|
| -1 | 1 | 2.666667 |
| 2 | 2 | 2.666667 |
| 4 | 5 | 2.666667 |

b. The target of the second round is the errors of the first round

| Х | У | Pred1 | e1 |
|----|---|----------|----------|
| -1 | 1 | 2.666667 | -1.66667 |
| 2 | 2 | 2.666667 | -0.66667 |
| 4 | 5 | 2.666667 | 2.333333 |

c. The second round predicts the errors of the first round

| Х | У | Pred1 | e1 | Pred 2 |
|----|---|----------|----------|----------|
| -1 | 1 | 2.666667 | -1.66667 | -1.16667 |
| 2 | 2 | 2.666667 | -0.66667 | -1.16667 |
| 4 | 5 | 2.666667 | 2.333333 | 2.333333 |

d. The predictions of y after the second round is the sum of the first round predictions and the second round predictions

| х | У | Pred1 | e1 | Pred2 | Final |
|----|---|----------|----------|----------|-------|
| -1 | 1 | 2.666667 | -1.66667 | -1.16667 | 1.5 |
| 2 | 2 | 2.666667 | -0.66667 | -1.16667 | 1.5 |
| 4 | 5 | 2.666667 | 2.333333 | 2.333333 | 5 |

e. The target of the third round is the errors of the second rounds

| Х | у | Pred1 | e1 | Pred2 | Final | e2 |
|----|---|----------|----------|----------|-------|------|
| -1 | 1 | 2.666667 | -1.66667 | -1.16667 | 1.5 | -0.5 |
| 2 | 2 | 2.666667 | -0.66667 | -1.16667 | 1.5 | 0.5 |
| 4 | 5 | 2.666667 | 2.333333 | 2.333333 | 5 | 0 |

f. The third round predicts the errors of the second round

| Х | У | Pred1 | e1 | Pred2 | Final | e2 | Pred3 |
|----|---|----------|----------|----------|-------|------|-------|
| -1 | 1 | 2.666667 | -1.66667 | -1.16667 | 1.5 | -0.5 | -0.5 |
| 2 | 2 | 2.666667 | -0.66667 | -1.16667 | 1.5 | 0.5 | 0.25 |
| 4 | 5 | 2.666667 | 2.333333 | 2.333333 | 5 | 0 | 0.25 |

g. The predictions of y after the third round is the sum of the first round predictions, the second round predictions and the third round predictions

| Х | У | Pred1 | e1 | Pred2 | Final | e2 | Pred3 | Pred_final |
|----|---|----------|----------|----------|-------|------|-------|------------|
| -1 | 1 | 2.666667 | -1.66667 | -1.16667 | 1.5 | -0.5 | -0.5 | 1 |
| 2 | 2 | 2.666667 | -0.66667 | -1.16667 | 1.5 | 0.5 | 0.25 | 1.75 |
| 4 | 5 | 2.666667 | 2.333333 | 2.333333 | 5 | 0 | 0.25 | 5.25 |

4.

a. Since there are 5 observations, each has a weight of 1/2

| | x1 | x2 | У | Weight |
|---|----|----|----|--------|
| | | | | 1 |
| 0 | 1 | 2 | 1 | 0.2 |
| 1 | 2 | 5 | 1 | 0.2 |
| 2 | 3 | 4 | -1 | 0.2 |
| 3 | 4 | 0 | -1 | 0.2 |
| 4 | 0 | 1 | -1 | 0.2 |

b. Predictions of stump 1 are:

| | x1 | x2 | У | Weight | Stump 1 |
|---|----|----|----|--------|---------|
| | | | | 1 | pred |
| 0 | 1 | 2 | 1 | 0.2 | 1 |
| 1 | 2 | 5 | 1 | 0.2 | 1 |
| 2 | 3 | 4 | -1 | 0.2 | -1 |
| 3 | 4 | 0 | -1 | 0.2 | -1 |
| 4 | 0 | 1 | -1 | 0.2 | 1 |

Since observation 4 is incorrectly classified, its weight should be increased. All other observations should have their weights decreased, as they were classified correctly.

c.

$$\epsilon_1 = 0.2$$

$$\alpha_1 = L * 0.5 * \ln\left(\frac{1 - 0.2}{0.2}\right) = 0.$$

For the misclassified observations:

$$w_{new} = 0.2 * e^{0.693} = 0.4$$

For the remaining:

$$w_{new} = 0.2 * e^{-0.693} = 0.1$$

| | x1 | x2 | У | Weight | Stump 1 | Weight | Stump 2 |
|---|----|----|----|--------|---------|--------|---------|
| | | | | 1 | pred | 2 | pred |
| 0 | 1 | 2 | 1 | 0.2 | 1 | 0.125 | 1 |
| 1 | 2 | 5 | 1 | 0.2 | 1 | 0.125 | 1 |
| 2 | 3 | 4 | -1 | 0.2 | -1 | 0.125 | 1 |
| 3 | 4 | 0 | -1 | 0.2 | -1 | 0.125 | -1 |
| 4 | 0 | 1 | -1 | 0.2 | 1 | 0.5 | -1 |

Repeating for rounds 2 and 3:

| | 1 | 2 | l | \\\a:ab+ | C4 | \\\a:ab+ | Cturana | \\\a:ab+ | Cturana |
|---|----|----|----|----------|--------|----------|---------|----------|---------|
| | x1 | x2 | У | Weight | Stump | Weight | Stump | Weight | Stump |
| | | | | 1 | 1 pred | 2 | 2 pred | 3 | 3 Pred |
| 0 | 1 | 2 | 1 | 0.2 | 1 | 0.125 | 1 | 0.07142 | -1 |
| | | | | | | | | 9 | |
| 1 | 2 | 5 | 1 | 0.2 | 1 | 0.125 | 1 | 0.07142 | 1 |
| | | | | | | | | 9 | |
| 2 | 3 | 4 | -1 | 0.2 | -1 | 0.125 | 1 | 0.5 | -1 |
| 3 | 4 | 0 | -1 | 0.2 | -1 | 0.125 | -1 | 0.07142 | -1 |
| | | | | | | | | 9 | |
| 4 | 0 | 1 | -1 | 0.2 | 1 | 0.5 | -1 | 0.28571 | -1 |
| | | | | | | | | 4 | |

d.

$$\epsilon_2 = 0.125$$

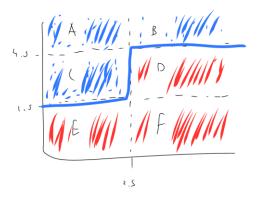
$$\epsilon_3 = 0.071429$$

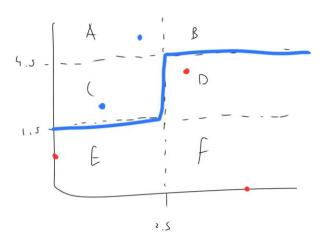
$$\alpha_2=0.972955$$

$$\alpha_3 = 1.28475$$

Stump 3 has the highest voting power, as it has the largest lpha

e.





f.

We can see that the adaboost perfectly classifies the positives and the negatives.

Therefore, the error is 0.