

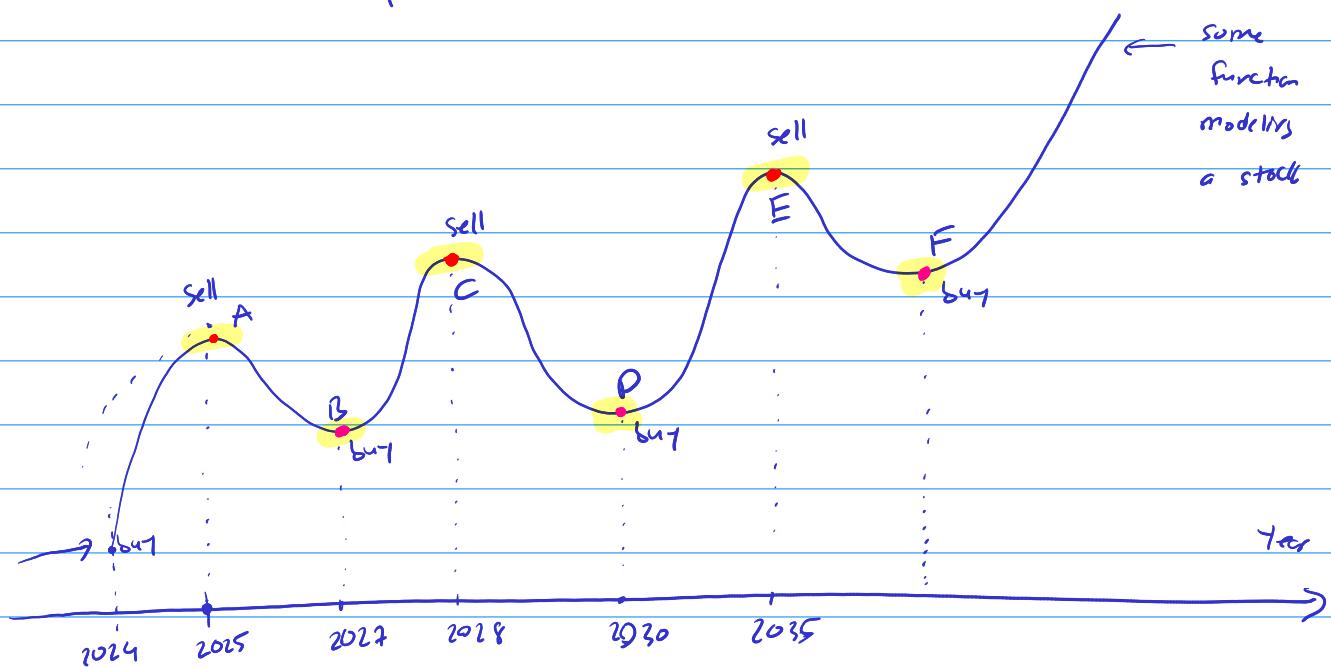
we can use function to model data / real-world issues

why we want to do that?

The benefit is: — Make future predictions / estimation

Use **Derivatives** to solve it

{ — Find some optimal value of the function. For example: Find the number of items that a company should produce to maximize their profit.



A, B, C, D, E, F are called local extrema of the function.

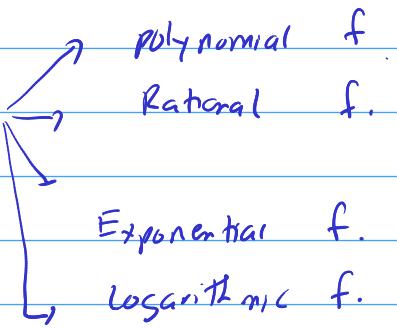
We can use "Derivatives" to find these points for a given function

Points A, C, E: local max where the 1st derivatives are zeros and 2nd derivatives are negative

Points B, D, F: local min 1st derivative are zeros and 2nd derivatives are positive.

Derivatives

we will cover the following functions:



Rule 1 (power rule)

The derivative of $f(x)$ is denoted by $f'(x)$

$$\begin{aligned}f(x) &= x^n \\ \Rightarrow f'(x) &= n \cdot x^{n-1}\end{aligned}$$

Example: Find $f'(x)$

$$\textcircled{1} \quad f(x) = x^4 \Rightarrow f'(x) = 4 \cdot x^{4-1} = 4x^3$$

$$\textcircled{2} \quad f(x) = x^{2024} \Rightarrow f'(x) = 2024 \cdot x^{2024-1}$$

$$= 2024 \cdot x^{2023}$$

$$\begin{aligned}\textcircled{3} \quad f(x) &= x^{\frac{1}{2}} = x^{\frac{1}{2}} \Rightarrow f'(x) = \frac{1}{2} \cdot x^{\frac{1}{2}-1} = x^{-\frac{1}{2}} \\ &\Rightarrow f'(x) = \frac{1}{2}\end{aligned}$$

$$\begin{aligned}\textcircled{4} \quad f(x) &= \sqrt{x} = x^{\frac{1}{2}} \\ \Rightarrow f'(x) &= \frac{1}{2} \cdot x^{\frac{1}{2}-1} = \frac{1}{2} \cdot x^{-\frac{1}{2}}\end{aligned}$$

$$\textcircled{5} \quad f(x) = \sqrt[3]{x} = x^{\frac{1}{3}}$$

$$f'(x) = \frac{1}{3} x^{\frac{1}{3}-1} = \frac{1}{3} x^{-\frac{2}{3}}$$

In general: $f(x) = \sqrt[n]{x} = x^{\frac{1}{n}}$

$$f'(x) = \frac{1}{n} \cdot x^{\frac{1}{n}-1}$$

Assignment 12

Find $f'(x)$

$$\textcircled{1} \quad f(x) = x^{1000}$$

$$\textcircled{5} \quad f(x) = \sqrt[4]{x}$$

$$\textcircled{2} \quad f(x) = x^3$$

$$\textcircled{6} \quad f(x) = \sqrt[5]{x}$$

$$\textcircled{3} \quad f(x) = x^7$$

$$\textcircled{7} \quad f(x) = x^{\frac{2}{3}}$$

$$\textcircled{4} \quad f(x) = x$$

$$\textcircled{8} \quad f(x) = x^{\frac{7}{3}}$$

Show all the work
as in the example.

$$\textcircled{9} \quad f(x) = x^{-6}$$

$$\textcircled{10} \quad f(x) = \frac{1}{x} \quad (\text{extra credit})$$

Do not just give the final
answer.