

Exam 1 - Practice 1

This practice exam will be updated. There may be more problems added to the practice exam. The solution will be posted.

Problem 1.

Find the following limits.

a.

$$\lim_{x \rightarrow 1} \frac{x^2 + 4x + 3}{x^2 + 5x + 6}$$

b.

$$\lim_{x \rightarrow -1} \frac{x^2 + 4x + 3}{x^2 + 5x + 6}$$

c.

$$\lim_{x \rightarrow \infty} \frac{2x^2 + 4x + 3}{3x^2 + 5x + 6}$$

d.

$$\lim_{x \rightarrow \infty} \frac{2x^2 + 4x + 3}{3x^3 + 5x + 6}$$

e.

$$\lim_{x \rightarrow \infty} \frac{2x^5 + 4x + 3}{3x^3 + 5x + 6}$$

f.

$$\lim_{x \rightarrow 1} \frac{\sin 3x}{\sin 5x}$$

g.

$$\lim_{x \rightarrow 0} \frac{\sin 3x}{\sin 5x}$$

h.

$$\lim_{x \rightarrow 0} \frac{x^2 + \sin 3x}{x + \sin 5x}$$

Problem 2

Find values of x , if any, at which the function is not continuous.

a. $f(x) = x^2 + \frac{x}{3} + 2024$

b. $f(x) = x^2 + \frac{3}{x-1} + 2024$

c. $f(x) = \frac{3}{2x+5} + \frac{x-1}{x^2-5x+6}$

Problem 3.

Find a value of the constant k , if possible, that will make the function continuous everywhere.

a.

$$f(x) = \begin{cases} x - 2, & x \leq 2 \\ kx^2 + k, & x > 2 \end{cases}$$

b.

$$f(x) = \begin{cases} x^2 + x + 4, & x \leq 0 \\ -9x + k^2, & x > 0 \end{cases}$$

Problem 4.

- a. Use the definition of derivatives to find $f'(x)$, and then find the tangent line to the graph of $y = f(x)$ at $x = 1$

$$f(x) = 2x^2 - 3x + 4$$

- b. Use the definition of derivatives to find $f'(x)$, and then find the tangent line to the graph of $y = f(x)$ at $x = 0$

$$f(x) = \frac{1}{x+1}$$