



In general, if the sample size (the number of data points in the sample) goes to infinity,

then: sample mean approaches pop. mean

and sample variance approaches pop. variance

⑩ Binomial Distribution.

Consider an experiment of tossing a coin.

100 times.

Let X be the number of times you get tail.

X is a binomial distribution.

consider of a sequence of independent and identical experiments where each experiment has only 2 outcomes: Success and Failure.
(S) and (F)

let X be the number of success.

let p be the prob of success.

X is called a binomial distribution.

$$X \sim \text{Binomial}(p, n)$$

p : chance of success

n : number of trials.

Example:

X is the number of tail when tossing a fair coin 20 times.

$$X \sim \text{Binomial}(\underline{p=0.5}, \underline{n=20})$$

Some Questions:

$$\left. \begin{array}{l} \textcircled{1} \quad \textcircled{EX} = ? \quad \textcircled{V(X)} = ? \\ \textcircled{2} \quad P(X=7) = ? \end{array} \right\}$$

$$X \sim \text{Binomial}(n, p)$$

$$\textcircled{1} \quad E(X) = n \cdot p$$

$$\textcircled{2} \quad V(X) = n \cdot p(1-p)$$

$$\textcircled{3} \quad P(X = k) = \underbrace{\binom{n}{k}}_{\text{red arrow}} p^k (1-p)^{n-k} \quad \leftarrow$$

$$\binom{n}{k} = \frac{n!}{k! (n-k)!}$$

n choose k

$$n! = 1 \cdot 2 \cdot 3 \cdot 4 \cdots n$$

\downarrow
(n factorial)