Overfitting and Model Tuning

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Reading Materials

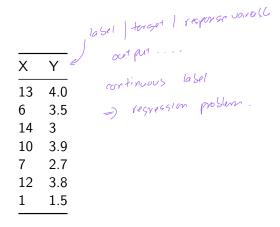
► Max Kuhn. Chapter 4.

Prediction Problem

Given data of $X = [X_1, X_2, ..., X_d]$ and Y. Find the relation between X and Y.

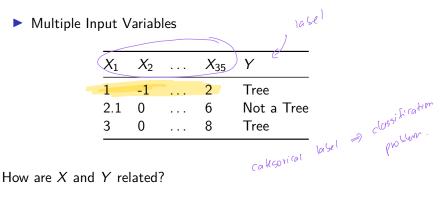
Prediction Problem - Examples

► One Input Variable X



How are X and Y related? Given new X, we want to predict Y

Prediction Problem - Examples



How are X and Y related?

Prediction Problem

- ▶ If Y is continous, we have a **regression** problem.
- ▶ If *Y* is categorical, we have a **classification** problem.
- ▶ If Y is binary, we have a **binary classification** problem.

Prediction Problem - Examples

► This is a regression problem since *Y* is continuous.

Υ
4.0
3.5
3
3.9
2.7
3.8
1.5

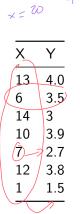
Prediction Problem - Examples

▶ This is a binary classification Problem since Y is binary.

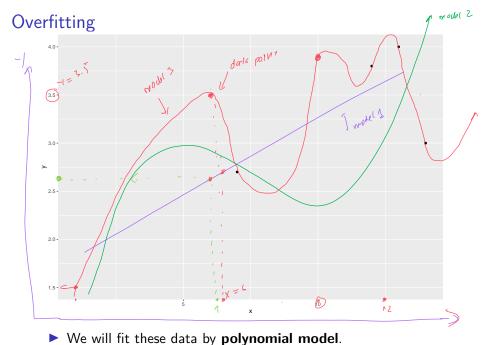
X_1	X_2	 X ₃₅	Y	
1	-1	 2	Tree	
2.1	0	 6	Not a	Tree
3	0	 8	Tree	

Overfitting

Consider the data:

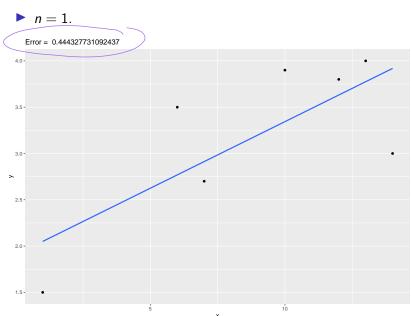


- ▶ We will fit these data by polynomial model.
- ▶ In polynomial model, Y is a polynomial function of X.

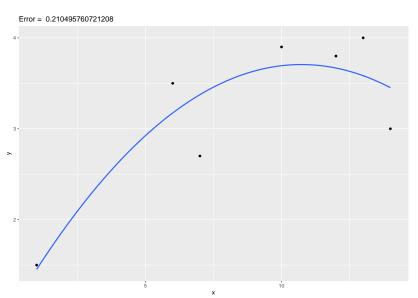


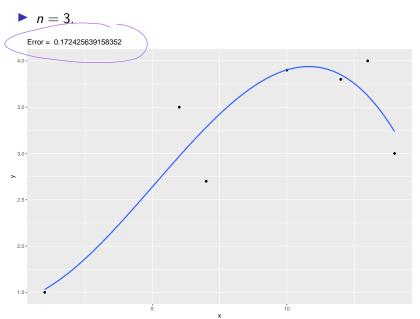
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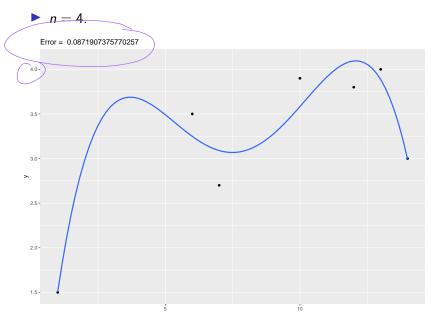
- ▶ In polynomial model, we need to specify the degree of the polynomial, *n*. Let try a few.
- ▶ If n = 1, we have a familiar **linear model**.
- Question: Does increasing n resuls in a better model?



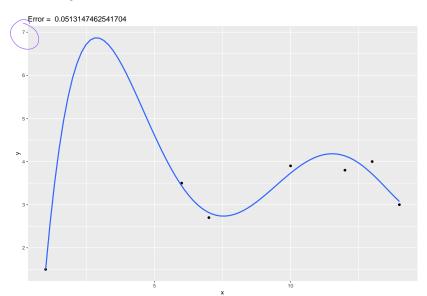
ightharpoonup n=2.



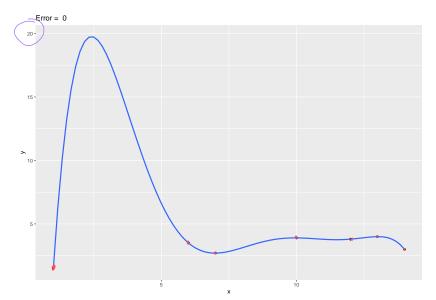




n = 5.



n = 6.



Question: What are the errors when n > 6?

- **Question**: What are the errors when n > 6?
- ► Answer: The errors are all zeros. (There are actually many solutions for each degree greater than 6.)

▶ Question: What is the best model?

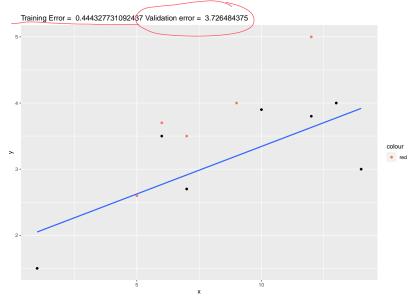
- ▶ **Question**: What is the best model?
- ► Answer: We do not know. We need a validation dataset to validate the models.

► The errors we have seen are called **training errors**

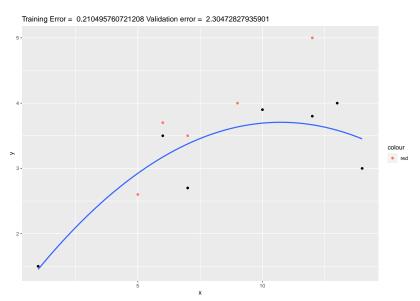
- Let's validate these models with a validation dataset
- Validation Data

Υ
2.6
3.5
4.0
3.7
5.0

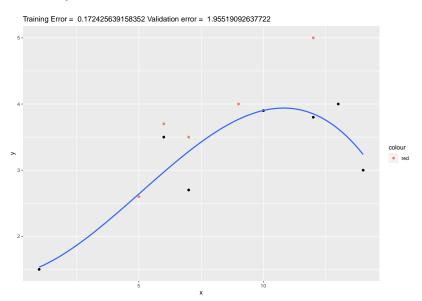
ightharpoonup n = 1.

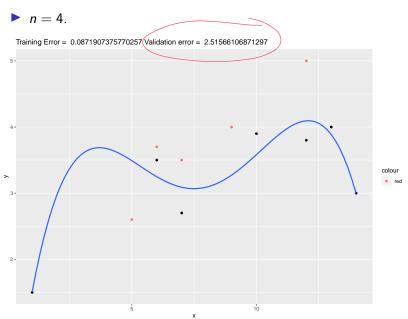


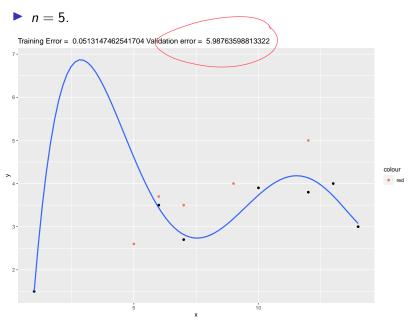
n = 2.

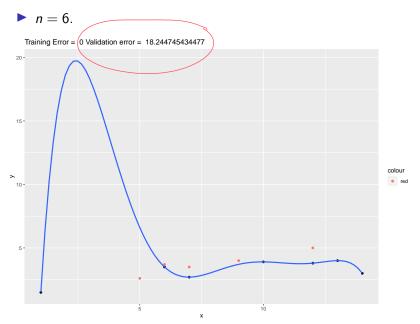


n = 3.









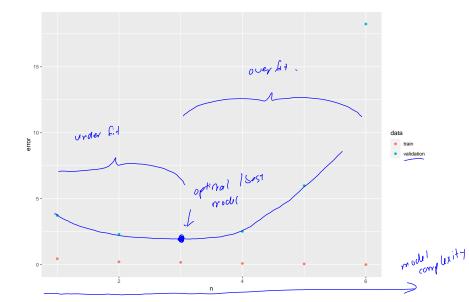
► Training Error vs. Validation Error

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	Training Error	Validation Error
$\overline{n=1}$	0.4443277	3.726484
n = 2	0.2104958	2.304728
n=3	0.1724256	1.955191 (Best!)
n = 4	0.08719074	2.515661
n = 5	0.05131475	5.987636
n=6	0	18.24475



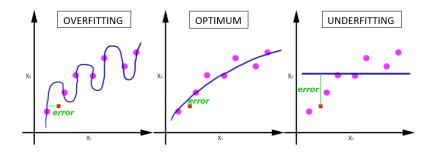
► Training Error vs. Validation Error



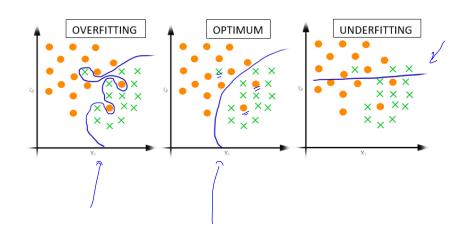
- As the degree n increases, the training errors decrease
- ▶ Model 6 (n = 6) is the best (perfect) in training but the worst in validation.
- ► The best model is the model with the best (lowest) error in validation data.

Overfitting - Polynomial Model ## - Model 4, 5 and 6 are **overfitted** - Model 1 and 2 are **underfitted** - Model 3 is the best model.

Overfitting in Regression



Overfitting in Classification



Model Complexity/Capacity

- ▶ In polynomial models, the larger *n*, the more complex/capable the model. ____
- Model complexity can be measured by the number of parameters/unknown of the model.

Linear model:

$$= ax + b$$

▶ Question: How many unknowns/parameters in linear model?

▶ Linear model (n = 1):

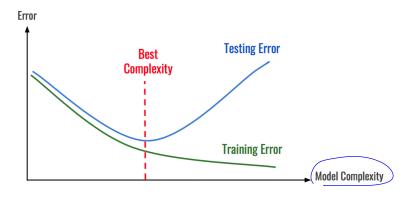
$$y = ax + b$$

- Question: How many unknowns/parameters in linear model?
- **Answer**: Two unknowns/paramters: a and b

Quadratic model (n = 2): $v = ax^{2} + bx + c$

- Three unknowns: a, b, and c.
- Quadratic model has more unknowns/parameters then linear model. Thus, quadratic model is more complex than linear model

► The mode complex the model, the easier it becomes overfitted!



Model Tuning

- \blacktriangleright We just "tuned" the the parameter n.
- ► The parameter *n* is called **tuning parameter**, or **hyperparameter**

Model Tuning

- Model tuning is the process of finding the **best** values for the tuning parameters of the model
- ► This is done through **trying out** many values for the tuning parameters then select the best values.

Model Training

- Model training is the process of finding the unknown/parameters of the model
- **Example**: Training linear model y = ax + b is to find a and b that best fit the data

Model Training vs. Model Tuning

- Model training finds the parameters
 - ► Model tuning finds **hyperparameters**

Model vs. Family of Models

- ► The polynomial model is a **family** of models.
- Linear model is just **one** model
- A family of models has "tuning parameters".
- A single model, say, linear model, does not have tuning parameter
- Some model has multiple tuning parameters.

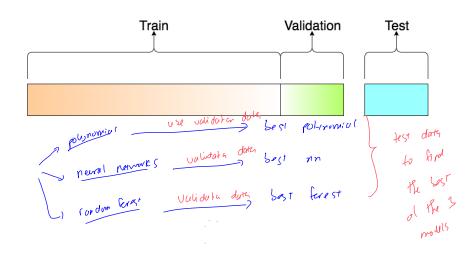
Data Splitting

- ▶ We need validation data for model tuning.
- ▶ **Question**: How can one of obtain validation data?

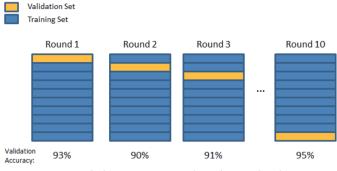
Data Splitting

- We need validation data for model tuning.
- Question: How can one of obtain validation data?
- ► Answer: We do not use the entire data to train models. We use a portion of it for training and save data for validation and testing.

Data Splitting: Train-Validation-Test

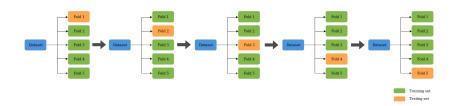


k-folds Cross Validation



Final Accuracy = Average(Round 1, Round 2, ...)

k-folds Cross Validation



k-folds Cross Validation and test

