# Time Series Decomposition

#### Time Series Patterns

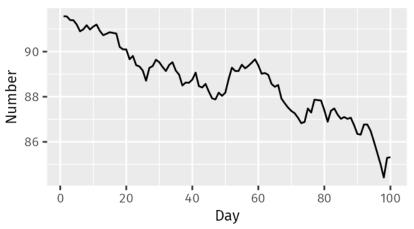
A time series may consist of

- trend,
- seasonality and
- cycles

#### Trend

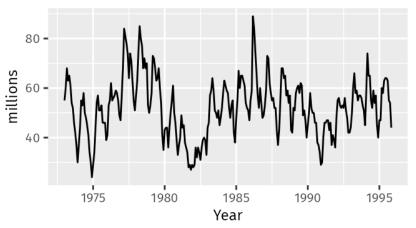
- ▶ A trend is a long-term increase or decrease in the data.
- Trend does not have to be linear.
- Sometimes we will refer to a trend as "changing direction", when it might go from an increasing trend to a decreasing trend.

# US treasury bill contracts



➤ The US treasury bill contracts show results from the Chicago market for 100 consecutive trading days in 1981. There is a downward trend

Sales of new one-family houses, USA

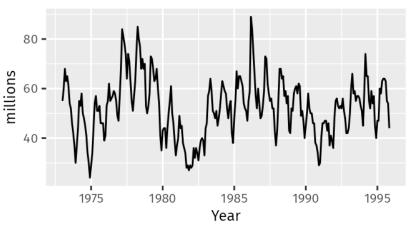


▶ There is no apparent trend in the data over this period

# Cycle and Seasonal

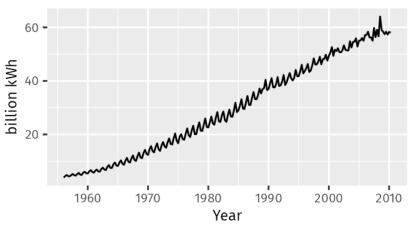
- cycle: repeated events over time that are not equally spaced
- seasonal: repeated events over time that are equally spaced

## Sales of new one-family houses, USA



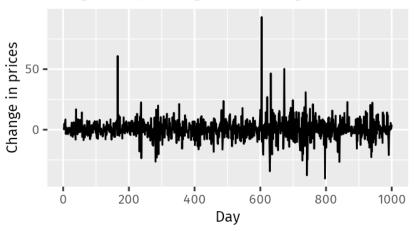
➤ The monthly housing sales show strong seasonality within each year, as well as some strong cyclic behaviour with a period of about 6–10 years

# Australian quarterly electricity production



The Australian quarterly electricity production shows a strong increasing trend, with strong seasonality. There is no evidence of any cyclic behavior here

# Google daily changes in closing stock price



No trend, seasonality or cyclic behaviour. There are random fluctuations which do not appear to be very predictable, and no strong patterns that would help with developing a forecasting model.

## Time series decomposition

- When we decompose a time series into components, we usually combine the trend and cycle into a single trend-cycle component (sometimes called the trend for simplicity).
- ▶ Three components: a trend-cycle component, a seasonal component, and a remainder component (containing anything else in the time series).

# Two decompositions

▶ Additive Decomposition

$$y_t = S_t + T_t + R_t$$

Multiplicative decomposition

$$y_t = S_t \times T_t \times R_t$$

# Relationship

The log transformation will turn a multiplicative model to additive model.

# Central MA vs. MA

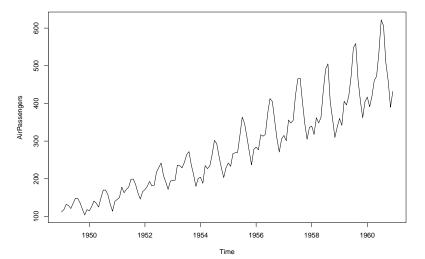
Link.

# Classical Decomposition

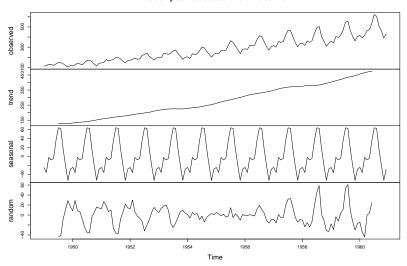
In classical decomposition, we assume that the seasonal component is constant from year to year

## Classical Decomposition

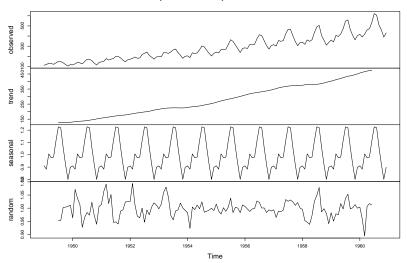
- ▶ Trend Estimate: Smooth the data using centred moving average (CMA) of the order equal to the periodicity of the data
- Detrend the data: calculate the detrended series by subtracting/dividing the trend estimate
- Seasonal Estimate: Average value for each period is calculated based on the de-trended series.
- Random/Remainder: subtract from the series the trend and seasonal component estimations



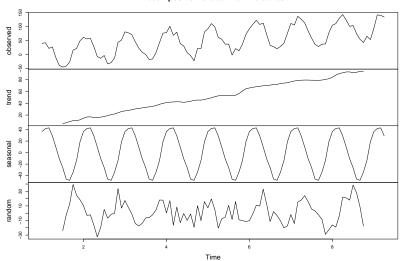
#### Decomposition of additive time series



#### Decomposition of multiplicative time series



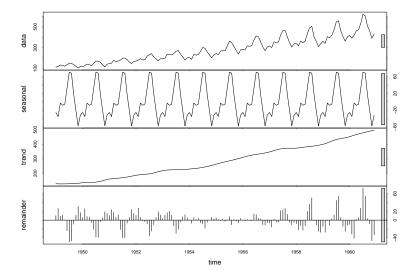
#### Decomposition of additive time series



## STL Decomposition

- Classical Decomposition uses Central Moving Average to estimate the trend
- ► STL uses LOESS (locally estimated scatterplot smoothing) to estimate the trend
- Link
- ➤ The seasonal component is estimated using moving averages of the de-trend series

- STL will handle any type of seasonality
- ▶ STL is a versatile and robust method for decomposing time series
- ▶ STL can be implemented using stl function



## Other Decomposition Methods

- X-11 decomposition: originated in the US Census Bureau and Statistics Canada
- ► SEATS decomposition: developed at the Bank of Spain, and is now widely used by government agencies around the world