

ELEC 341 – Graded Assignments

Assignment A1

White-Box Systems

10 Marks

Learning Objectives

Modeling White Box Systems

Circuit Analysis

Impulse / Natural Response

Practical Impulse Response

Envelope Approximation

Step Response

Settle Time

Matlab

inv()

tf()

minreal()

lsim()

impz()

step()

plot()

When you design a circuit from scratch, you know exactly what’s inside and can identify the system analytically. This is called a “White Box” system.

Q1 2 mark(s) CCT Analysis

Use circuit analysis to compute the transfer function **Vout/Vin** of the **Voltage Amplifier** circuit. After assigning Q1.G, use **minreal()** to cancel any common factors.

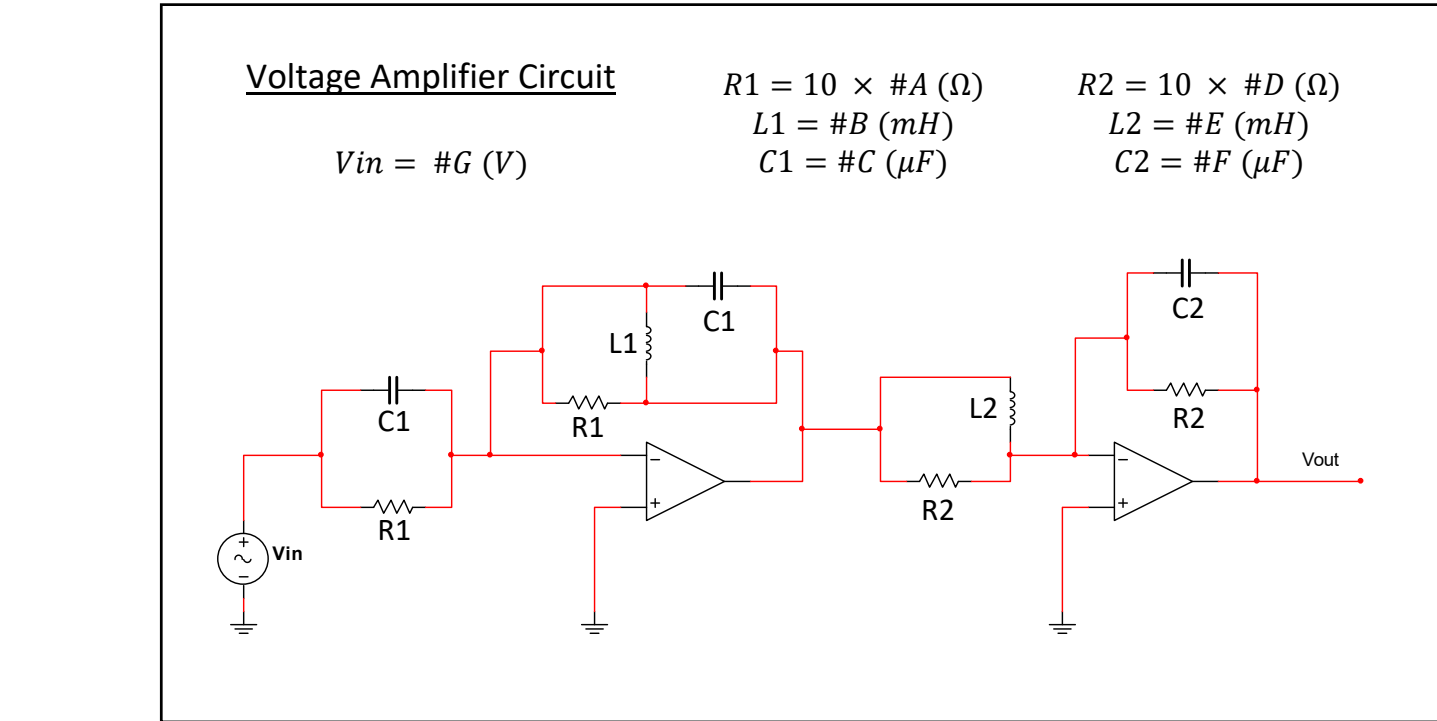
- Q1.G (V/V) LTI

*The circuit is nothing but a 2-stage amplifier. If you have difficulty analyzing it, review standard op-amp circuits. Most op-amp circuits are either an amplifier or weighted sum. If you round the coefficients, poles or zeros, of a transfer function, the error compounds. If you do not carry at least 3 significant digits, your error could compound quite a bit. But there is **no good reason** to round digits in the first place. Your MAT file isn’t going to be any cleaner, just less accurate.*

Q2 2 mark(s) Impulse & Envelope

Plot the **Step** response. Scale the input by Vin to simulate the voltage source. Find the **EXPONENTIAL** envelope from the Inverse Laplace Xform, or estimate it by trial & error. Your envelope should have the form $FV \pm K \exp(-A \cdot T)$, where FV is the final value.

- Q2.K (V) Scalar
- Q2.A (s^-1) Scalar



In Matlab, you can use `impulse()` to find a natural response, but in practice its an impossible input function because it is infinitely large. But you can approximate it. Just remember a fundamental property of the impulse function is the area under the curve is 1.

*Pay attention to **PHYSICAL UNITS**. An answer that is 1000x too big or too small is **WRONG**.*

Q3 1 mark(s) Approximate Impulse

Plot the **Impulse** response of Q1.G.

Generate a signal that starts high V_h at $T_h=0$, goes low $V_l=0$ at T_l , and stays low for the length of the signal in Q2. This signal **APPROXIMATES** an impulse when V_h is large and T_l is small.

Use **lsim()** to apply the signal to the Voltage Amplifier and plot the response on the same figure.

T_l should be the **LARGEST** value that satisfies the following requirements:

The actual and approximate impulse responses are approximately equivalent when $T_l = Q3.T_l$

The actual and approximate impulse responses are noticeably different when $T_l = 5 \times Q3.T_l$

- $Q3.T_l$ (s) Scalar
- $Q3.V_h$ (KV) Scalar

The function you developed is POSSIBLE, but is it PRACTICAL ???

Why or why not ??? What's the difference ???

What was the point of maximizing T_l ???

What would you do if you really did need to do this in practice ???



What could be easier than a circuit with only current sources because you can turn to your old friend, Nodal Analysis ???

Now that you've got a new friend, Matlab, it's time to meet another new friend, Matrix-Method. To prove what a loyal friend it is, try to solve this problem **by inspection**.

Q4 2 mark(s) CCT Analysis

Compute the transfer function **I_{out}/I_{in}** of the **Shunt** circuit.

Use **minreal()** to cancel any common factors.

- Q4.G (pure) LTI

Q5 2 mark(s) Step & Envelope

Plot the **STEP** response.

Find the **EXPONENTIAL** envelope from the Inverse Laplace Xform, or estimate it by trial & error.

Your envelope should have the form $FV \pm K \exp(-A \cdot T)$, where FV is the final value.

- Q5.K (A) Scalar
- Q5.A (s^{-1}) Scalar

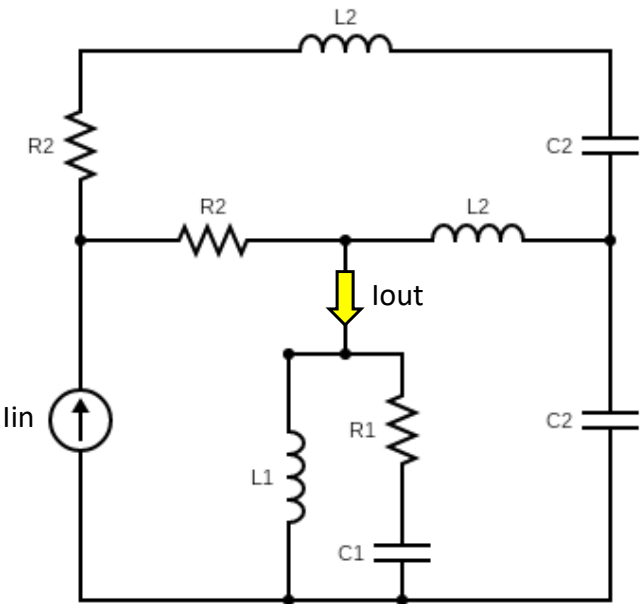
COW: Check your initial and final values **by inspection** of the circuit.

If they do not agree, your transfer function isn't right.

Shunt Circuit

$I_{in} = \#H (A)$

All other component values are the same as in the Voltage Amplifier Circuit



Settle time is the time it takes for a response to settle to within 2% of its final value.

COW: Pay attention to **PHYSICAL UNITS**.

*An answer that is 1000x too big or too small is **WRONG**.*

Q6 1 mark(s) Settle Time

For your Q5 Step Response, estimate settle time T_s .

- Q6. T_s (ms) Scalar

What is the settle time for your Impulse response ???

Is it even possible to find the settle time of your Impulse response ???

