CIS 256 Lab #5

1)
$$T(n) = 2^{n} + 1$$
 and $f(n) = 4^{n} - 16$
 $c = 1$, $n = 3$
 $2^{3} + 1 \le 4^{3} - 16 = 3$ $T(n) \le cf(n)$
 $9 \le 48$

2)
$$f(n) = O(g(n))$$

 $f(n) \le c' \cdot g(n)$ for all $n \ge N'$
 $g(n) \le O(h(n))$
 $g(n) \le c'' \cdot h(n)$ for all $n \ge N''$
 $f(n) \le c' \cdot c'' h(n)$ and $c' \cdot c'' = c'''$
 $f(n) \le c''' h(n)$
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3)
$$T(n) = 0.01n^2 - 1$$

$$f(n) = 0(n)$$

$$\lim_{n \to \infty} \frac{cf(n)}{T(n)} = \lim_{n \to \infty} \frac{cn}{0.01n^2 - 1}$$

$$= \lim_{n \to \infty} \frac{c}{n \to \infty} = \lim_{n \to \infty} \frac{c}{0.01n^2 - 1}$$

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