



Chapter 1: Exercises

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1. Prove that the following identities are valid using algebraic manipulation.

$$(a) AB' + BC' + CA' = A'B + B'C + C'A$$

$$(b) AB + A'C + BCD = AB + A'C$$

2. Find the complements of the following functions.

$$(a) F = A + BC$$

$$(b) F = AB + B'C + CA'D$$

4. Simplify the following expressions by means of a four-variable map.

(a) $A'D + BD + B'C + AB'D$

(b) $X'Z + W'XY' + W(X'Y + XY')$

(c) $AB'C + B'C'D' + BCD + ACD' + A'B'C + A'BC'D$

(d) $ABC + CD + BC'D + B'C$

5. Design a **combinational circuit** whose input ($A_3A_2A_1A_0$) is a four-bit number and whose output ($F_3F_2F_1F_0$) is the 2's complement of the input number.

6. Design a **mealy sequential circuit** which converts the X sequence input to the Z sequence output. Try to use as less states as possible.

X input			Z output		
t2	t1	t0	t2	t1	t0
0	0	0	0	1	1
0	0	1	1	0	0
0	1	0	1	0	1
0	1	1	1	1	0
1	0	0	1	1	1