

from Sebesta book ch3.

a grammar for a small language

G

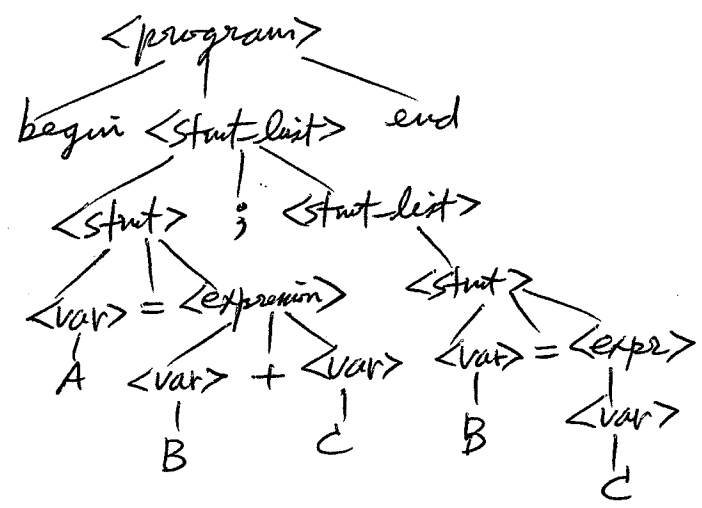
$$\begin{aligned}
 \langle \text{program} \rangle &\rightarrow \text{begin } \langle \text{stmt-list} \rangle \text{ end} \\
 \langle \text{stmt-list} \rangle &\rightarrow \langle \text{stmt} \rangle \\
 &\quad | \langle \text{stmt} \rangle ; \langle \text{stmt-list} \rangle \\
 \langle \text{stmt} \rangle &\rightarrow \langle \text{var} \rangle = \langle \text{expression} \rangle \\
 \langle \text{var} \rangle &\rightarrow A | B | C \\
 \langle \text{expression} \rangle &\rightarrow \langle \text{var} \rangle + \langle \text{var} \rangle \\
 &\quad | \langle \text{var} \rangle - \langle \text{var} \rangle \\
 &\quad | \langle \text{var} \rangle
 \end{aligned}$$

a sample program (stmt)

```

begin
  A = B + C ;
  B = C ;
end
  
```

show ^a parse tree

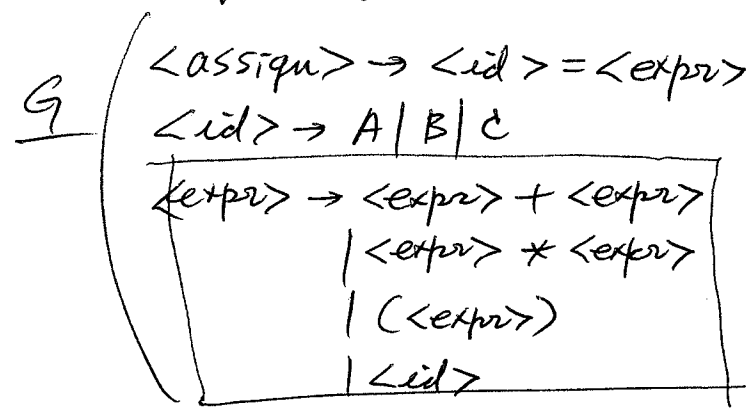


show the left-most derivation

$$\begin{aligned}
 \langle \text{program} \rangle &\Rightarrow \text{begin } \langle \text{stmt-list} \rangle \text{ end} \\
 &\Rightarrow \text{begin } \langle \text{stmt} \rangle ; \langle \text{stmt-list} \rangle \text{ end} \\
 &\Rightarrow \text{begin } \langle \text{var} \rangle = \langle \text{expr} \rangle ; \langle \text{stmt-list} \rangle \text{ end} \\
 &\Rightarrow \text{begin } A = \langle \text{expr} \rangle ; \langle \text{stmt-list} \rangle \text{ end} \\
 &\Rightarrow \text{begin } A = \langle \text{var} \rangle + \langle \text{var} \rangle ; \langle \text{stmt-list} \rangle \text{ end} \\
 &\quad \vdots \\
 &\Rightarrow \text{begin } A = B + C ; B = C \text{ end}
 \end{aligned}$$

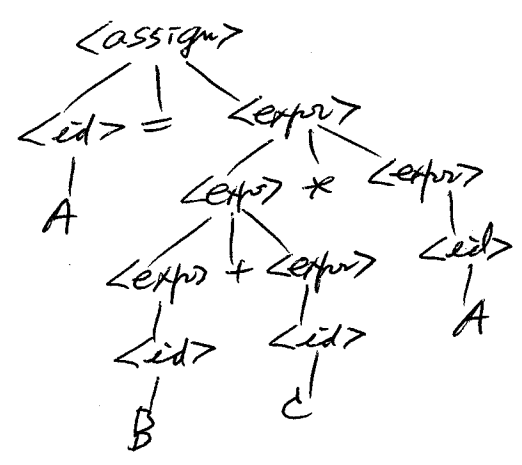
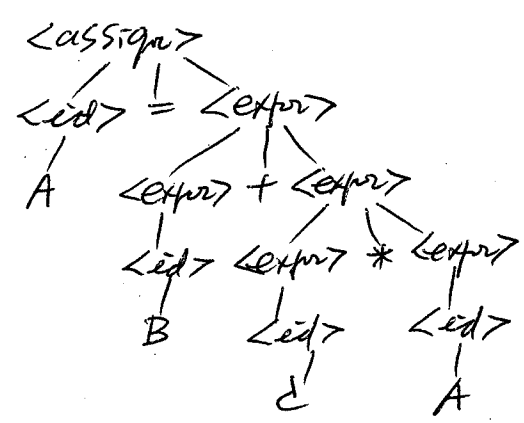
The given string (program) is in the lang.
 defined by the Grammar, $\therefore \exists$ a parse tree
 or, \exists a derivation.

— a simple assignment statement



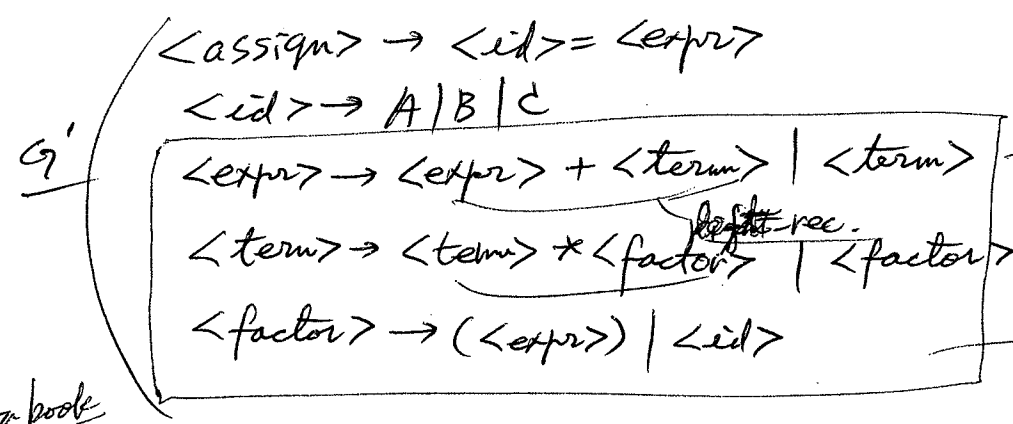
ambiguous ✓
 $\therefore (+, *)$ same precedence way,
 $()$

Stng: $A = B + C * A$ — \exists more than 1 parse trees $\Rightarrow G$ is ambiguous



\Rightarrow write unambiguous G for $\langle \text{assign} \rangle$ statement:

- Keep precedence of ops $\begin{pmatrix} + \\ * \\ () \end{pmatrix} \uparrow$
 - Keep associativity
- $+, *$ — left assoc. \Rightarrow so, G should be left-rec.



$+$ — lowest precedence
 $*$
 $()$ — highest precedence

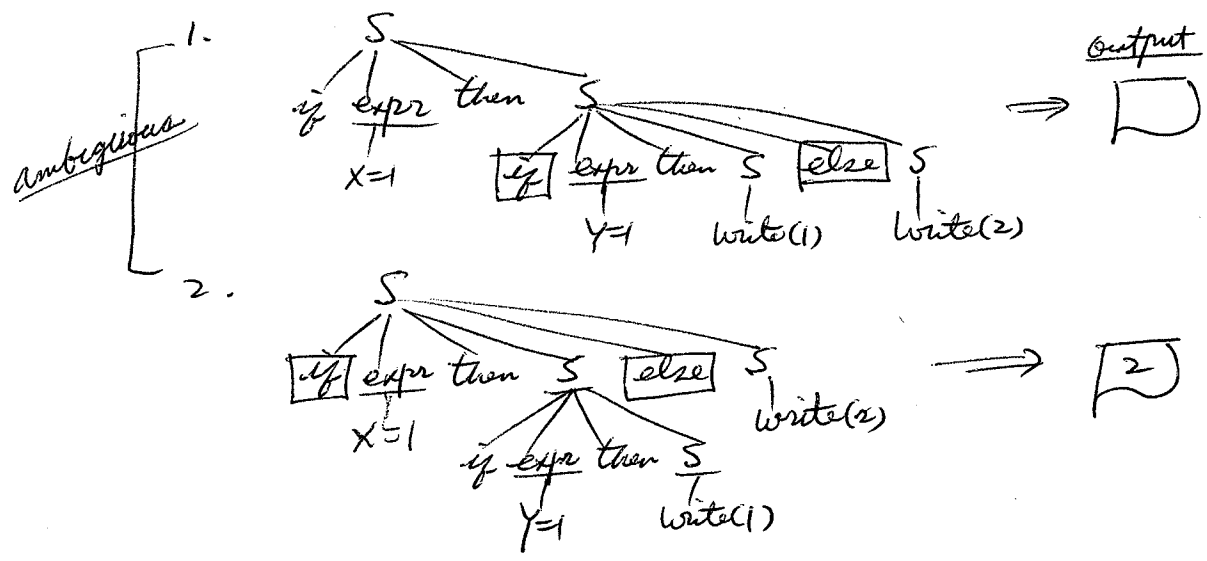
Self-starting book

24) PASCAL Syntax

$S \rightarrow \text{if expr then } S$
 $\quad | \text{if expr then } S \text{ else } S$

(Assume: $X=2$
 $Y=1$)

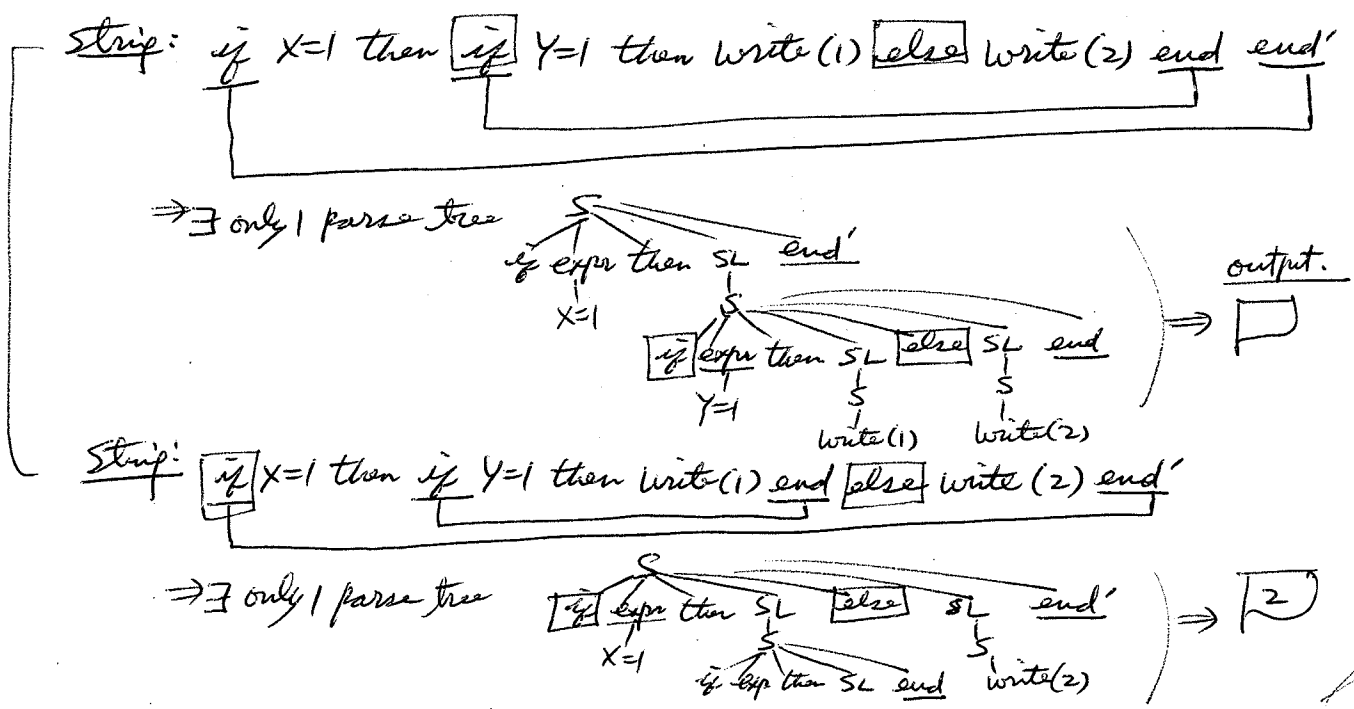
Strip: if $X=1$ then if $Y=1$ then write(1) else write(2)
 $\Rightarrow \exists 2$ parse trees



24) Modular Syntax

$S \rightarrow \text{if expr then } SL \text{ end}$
 $\quad | \text{if expr then } SL \text{ else } SL \text{ end}$

(Assume: $X=2$
 $Y=1$)



— variations of CFG notation

BNF

$\langle \rangle$ — non-terminal
 $::=$ — \rightarrow
 $|$ — choice

#1 $\langle E \rangle ::= \langle E \rangle + \langle T \rangle | \langle T \rangle$
 \Rightarrow simplified way:
 $E \rightarrow E + T | T$

(EBNF way) $\left(\begin{array}{l} \text{non-T} \\ \text{upper case} \\ T - \text{lower case} \end{array} \right)$

EBNF

non-T starts with capital
 $|$ — choice
 $()$ — group
 $\{ \}$ — ϕ or more times repeat
 $[]$ — optional (ϕ or 1 time)

Syntax chart

\rightarrow — derivation
 \square — non-T
 \bigcirc — Terminal

#1 BNF

2 productions $\left(\begin{array}{l} \langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{term} \rangle | \langle \text{term} \rangle \\ \langle \text{term} \rangle ::= \langle \text{term} \rangle * \langle \text{factor} \rangle | \langle \text{factor} \rangle \\ \langle \text{factor} \rangle ::= \langle \text{digit} \rangle \\ \langle \text{digit} \rangle ::= 0 | 1 | 2 | \dots | 9 \end{array} \right)$

vs.

EBNF

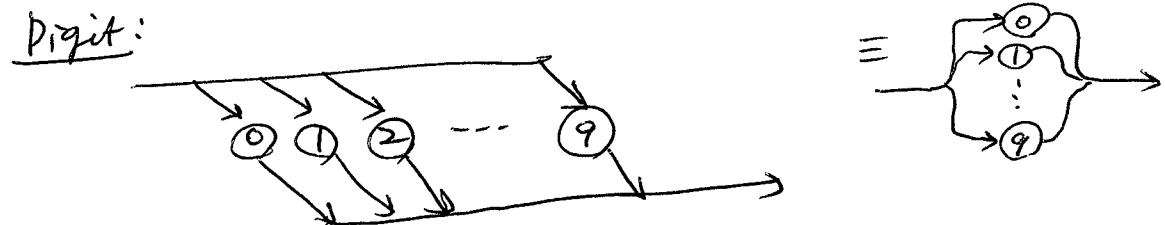
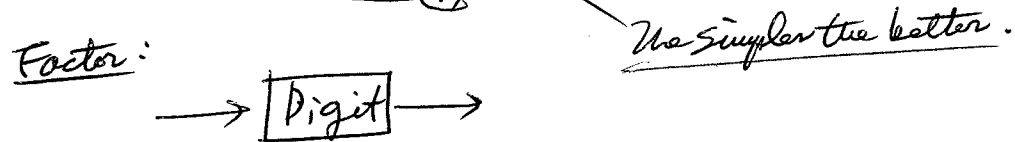
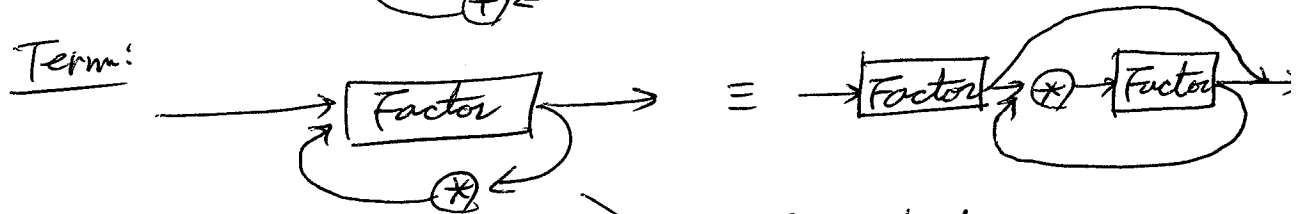
1 production $\left(\begin{array}{l} \text{Expr} ::= \text{Term} \{ '+' \text{Term} \} \\ \text{Term} ::= \text{Factor} \{ '*' \text{Factor} \} \\ \text{Factor} ::= \text{Digit} \\ \text{Digit} ::= 0 | 1 | 2 | \dots | 9 \end{array} \right)$

Syntax chart

each non-T has a chart

↓

↓
Syntax chart



Convert EBNF \rightarrow BNF

EBNF

optional:

$S \rightarrow ab[c]d$

for more times:

$S \rightarrow ab\{c\}d$

mixed:

$S \rightarrow ab\{c\}[d]e$

BNF

$S \rightarrow abcd$
 $\quad \quad | abd$

$S \rightarrow ab\underline{X}d$
 $X \rightarrow \epsilon$
 $\quad \quad | cX$ *new nonT*

$S \rightarrow ab\underline{X}\underline{d}e$
 $\quad \quad | ab\underline{X}e$
 $X \rightarrow \epsilon$
 $\quad \quad | cX$