

## Shared-memory Programming with OpenMP (MK book, Ch.5)

OpenMP with C/C++ -- higher level than PThreads

```
#include <omp.h>
$>g++ -fopenmp p1.cpp
```

error checking way:

```
#ifdef _OPENMP } //if OpenMP is available, include <omp.h>,
#include <omp.h> } //otherwise, do not;
#endif
```

in the code, use directives (parallel, parallel for, critical, etc.):

```
#pragma omp .... directive (within a line)

can be single statement or { block }

parallel block
```

- Each thread has its own PC and stack.

vs. [ #pragma omp parallel //system uses the total # of cores (logical cores)  
#pragma omp parallel num\_threads (thread\_count) //any #of cores

→ provides automatic joins (implicit barrier).

ex)

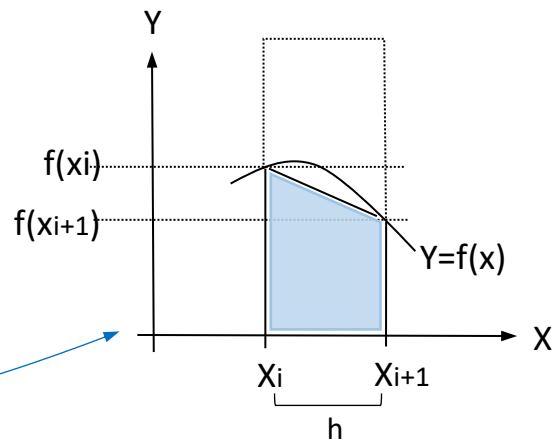
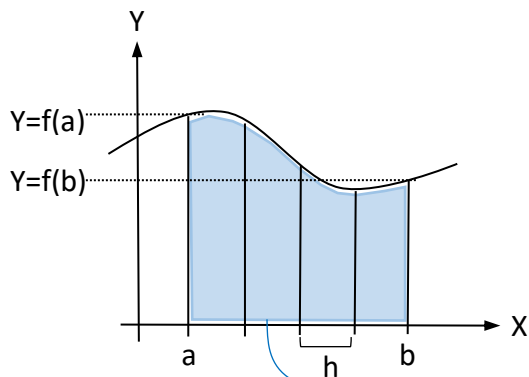
```
.... //main thread
#pragma omp parallel num_threads (4) } //total 5 threads (main + 4 forks)


Parallel block


```

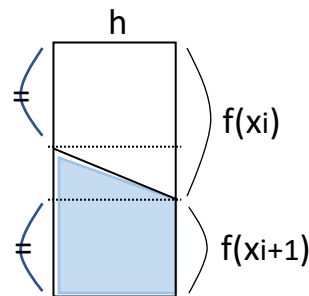
master      slaves  
└──────────┘  
a team

## Trapezoid for estimating the area under a curve – (integral $\int_{x=0}^{x=n}$ )

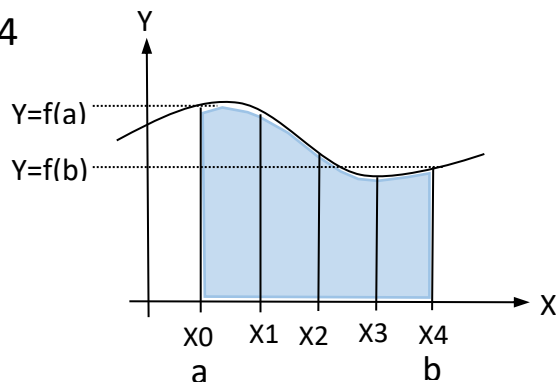


$$h = \frac{b-a}{n}, \quad n = \# \text{ of trapezoids}$$

$$\text{area} = \frac{(f(x_i) + f(x_{i+1})) * h}{2}$$



ex)  $n=4$



$$\begin{aligned} \text{total area} &= \frac{h * (f(x_0) + f(x_1))}{2} + \frac{h * (f(x_1) + f(x_2))}{2} + \frac{h * (f(x_2) + f(x_3))}{2} + \frac{h * (f(x_3) + f(x_4))}{2} \\ &= \frac{h}{2} [ (f(x_0) + f(x_1)) + (f(x_1) + f(x_2)) + (f(x_2) + f(x_3)) + (f(x_3) + f(x_4)) ] \\ &= \frac{h}{2} [ \underline{f(x_0)} + 2 * f(x_1) + 2 * f(x_2) + 2 * f(x_3) + \underline{f(x_4)} ] \end{aligned}$$

→ initial:  $\text{approx} = (f(x_0) + f(x_4)) / 2.0;$   
 then, for  $(i=1 \sim n-1) \{ \text{approx} += f(x_i); \}$  //  $i=1..3$   
 finally,  $\text{approx}(\text{tot\_area}) = h * \text{approx};$

## OpenMP implementation of the trapezoidal rule

- reference parameter way
- return function way
- reduction way
- parallel\_for loop way

### 1. reference parameter way

in main(..),

....

`#pragma omp parallel num_threads (thread_count)`  
`Trap (a, b, n, global_result);` *//global\_result is ref. para.*

....

`void Trap (double a, double b, int n, double& global_result)`

`{ ....`

`compute local_result;`

`#pragma omp critical`

`global_result += local_result;`

`} //global_result computation in the thread function`

### scope of variables:

- vs. {
- variables declared before parallel directive: shared scope among threads in the team;
  - variables declared in the parallel block (locals in thread func): private scope

scope can be changed with other directives;

## 2. return function way

in main(..),

....

global\_result = 0.0;

#pragma omp parallel num\_threads (thread\_count)

{ double local\_result = 0.0; *//private to each thread*

local\_result += local\_Trap (a, b, n);

#pragma omp critical

global\_result += local\_result; } *//global\_result computation in main( )*

}

## 3. reduction way (with return function)

in main(..),

....

global\_result = 0.0;

#pragma omp parallel num\_threads (thread\_count) \

reduction (+: global\_result)

global\_result += local\_Trap (a, b, n);

*//line continues*

*//reduction is done on this "+" operation  
and "global\_result" (must be shared var)*

#### 4. parallel-for loop way

without using thread function,

in main(..),

....

$h = (b - a) / n;$

$\text{approx} = (f(a) + f(b)) / 2;$

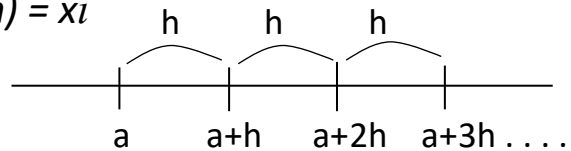
`#pragma omp parallel for num_threads (thread_count) \`

`reduction (+: approx) //parallel for must use for loop`

`for (i=1; i <= n-1; i++) //loop var i is private to each thread`

`approx += f(a + i*h);  //(a + i*h) = xi`

`approx. = h * approx;`



- parallel for must use for loop

`#pragma omp parallel for ....`

`for (i=0;... ) ....`

iterations are divided into threads, usually block division way, e.g.,

$i=0 \sim 10 \rightarrow Th_0$

$i=11 \sim 20 \rightarrow Th_1$

$i=21 \sim 30 \rightarrow Th_2$

....

## Parallel for directive

Only parallelizes for-loop, but no while/do-while loops;  
in fact, while/do-while loops can be converted to for-loop way.

- Cannot use “parallel for” for data dependent loops

ex) compute first N Fibonacci numbers:

1, 1, 2, 3, 5, 8, 13, . . . .

each loop iteration depends on previous iteration(s);

trial:

```
fibonacci[0] = fibonacci[1] = 1;
```

```
#pragma omp parallel for num_threads (thread_count)
for (i=2; i < n; i++)
    fibonacci[i] = fibonacci[i-1] + fibonacci[i-2];
```

if we use 2 threads (assume N=10),

output: 1, 1, 2, 3, 5, 8, 13, 21, 34, 55 --- if Th1 starts after Th0 finishes

or, 1, 1, 2, 3, 5, 8, 0, 0, 0, 0 --- if Th1 starts before Th0 finishes

→ not deterministic output

OpenMP compiler doesn't check for dependency among iterations.

→ programmer's responsibility

ex) for (i=0; i < n; i++)

```
{ x[i] = a + i*h;
```

→

```
  y[i] = exp(x[i]);
```

```
}
```

// ~~not~~ loop dependency

```
#pragma omp parallel for . . . .
```

```
for (i=0; i < n; i++)
```

```
{ x[i] = a + i*h;
```

```
  y[i] = exp(x[i]);
```

```
}
```

```
//executed in the
//same thread in
//the same iteration
//→ no problem
```

## Loop carried dependency

ex) estimating  $\pi$  (other examples: prefix sum, Flbo#, etc.)

$$\pi = 4 \left( 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots \right)$$
$$= 4 \sum_{k=0}^{\infty} \frac{(-1)^k}{2k+1}$$

serial algorithm:

```
double factor = 1.0;
double sum = 0.0;
for (k=0; k < n; k++)
    sum += factor / (2*k + 1);
    factor = - factor;
pi_approx = 4.0 * sum;
```

factor is updated in iteration\_i  
(ex, assigned to Thread\_i);  
This affects factor of iteration\_i+1  
(ex, assigned to Thread\_i+1)  
→ loop-carried dependency problem  
→ so, cannot use parallel-for

trial:

```
double factor = 1.0;
double sum = 0.0;
#pragma omp parallel for num_threads (thread_count) \
    reduction (+: sum)
for (k=0; k < n; k++)
{
    sum += factor / (2*k + 1);
    factor = - factor;
}
pi_approx = 4.0 * sum;
```

→ *incorrect result since  $\exists$  loop carried dependency*

correct version:

```
double factor = 1.0; //factor is shared_var  
double sum = 0.0;
```

```
#pragma omp parallel for num_threads (thread_count) \  
    reduction (+: sum) private (factor)
```

```
for (k=0; k < n; k++)  
{ if (k % 2 == 0)  
    factor = 1.0;  
  else  
    factor = -1.0;  
  sum += factor / (2*k + 1);  
}  
pi_approx = 4.0 * sum;
```

//Each thread has a private  
copy of factor (not shared)

- scope of private variables

ex) int x = 5; *//shared (since declared out of parallel block)*

```
#pragma omp parallel num_threads (thread_count) private (x)
```

```
{ int my_rank = omp_get_thread_num( );
```

```
  cout<<x; //x? unspecified
```

```
  x = 2*my_rank + 2;
```

```
  cout<<x;
```

```
}
```

```
cout<<x; //x=5
```

//Now, x is private to each thread;  
Value of x is unspecified at the  
beginning of parallel or parallel-  
for block.

Variables declared inside of a parallel block are always private, i.e.,  
each thread has a stack.



## Scope of variables – more

In a parallel block, programmer can specify the scope of variables.

#pragma omp parallel (or, parallel for) . . . . default (none) . . . .

//we need to provide scope of variables  
declared out of the parallel block

Basically,

```
. . . . //variables declared out of block are shared (to all threads);  
parallel . . . .  
{ . . . . //variables declared in the block are private (to each thread);  
}
```

With parallel . . . . default (none),

→ We need to provide the scope of variables, which are declared out of the block (and used in the block).

ex) . . . .

```
double sum = 0.0;  
  
#pragma omp parallel for num_threads (thread_count) \  
    default (none) reduction (+: sum) \  
    private (k, factor) shared (n)  
  
for (k=0; k < n; k++)  
{ if (k % 2 == 0) factor = 1.0;  
  else factor = -1.0;  
  sum += factor / (2*k + 1);  
}
```

//sum is both private and shared,  
since it is a reduction var.  
So, don't have to specify scope

shared var – not updated in the block;

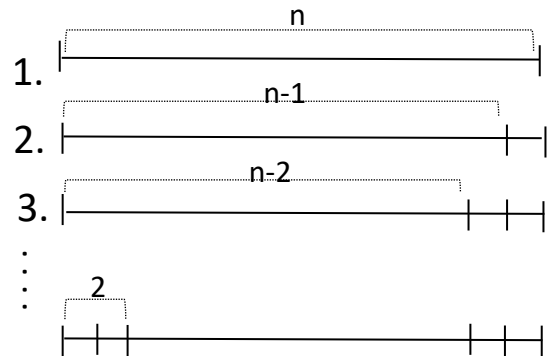
private var – updated in the block;

## Loops in OpenMP

ex) bubble sort

algorithm:

```
for (len=n; len >= 2; len--)  
  for (i=0; i < len-1; i++)  
    if (a[i] > a[i+1])  
      swap (a[i], a[i+1]);
```



Q1: Is there loop-carried dependency in the outer loop?

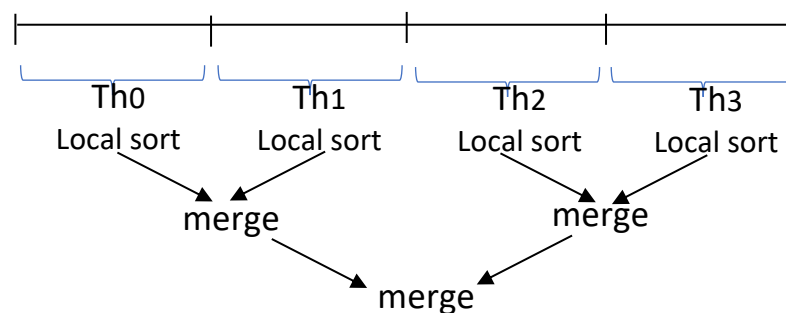
→ Yes, since the current list depends on the previous iterations.

Q2: Is there loop-carried dependence in the inner loop?

→ Yes, since the current pair depends on previous iterations.

So, we cannot apply parallel-for to bubble sort.

Any idea of parallelization?



- parallel-for vs. for

```
#pragma omp parallel num_threads (thread_count) . . .
```

```
{ . . .
```

```
#pragma omp parallel for  
for (i=0; i<n; i++)
```

vs.

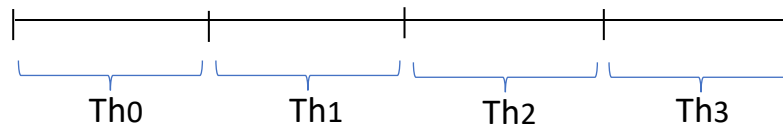
```
#pragma omp for  
for (i=0; i<n; i++)
```

*//with current  
team of threads,  
perform parallel-for*

```
. . . . //with forking a new team of  
threads, perform parallel-for  
}
```

## Scheduling loops – for parallel-for (or, for)

Parallel-for: most systems assign block-divide way;



→ problem: possibly unbalanced load

```
ex) sum = 0.0;
    for (i=0; i<n; i++)
        sum += f(i);
```

//if  $f(i)$  time depends on  $i$  linearly, i.e., bigger  $i$  yields bigger  $f(i)$  time,  $Th_0$  takes the least time while  $Th_{p-1}$  takes the longest time; → load unbalanced

→ better to use cyclic assignment (scheduling):

$Th_0$ : 0,  $0+P$ ,  $0+2P$ ,  $0+3P$ , . . . .

$Th_1$ : 1,  $1+P$ ,  $1+2P$ ,  $1+3P$ , . . . .

$Th_2$ : 2,  $2+P$ ,  $2+2P$ ,  $2+3P$ , . . . .

. . . .

$Th_{p-1}$ :  $P-1$ ,  $(P-1)+P$ ,  $(P-1)+2P$ ,  $(P-1)+3P$ , . . . .

→ *still problem!!*

## Schedule clause with parallel-for (or, for)

ex) default block scheduling

```
sum = 0.0;
```

```
#pragma omp parallel for num_threads (thread-count) reduction (+: sum)
```


```
for (i=0; i<=n; i++)
```

```
    sum += f(i);
```

ex) cyclic scheduling

```
sum = 0.0;
```

```
#pragma omp parallel for num_threads (thread-count) \  
    reduction (+: sum) schedule (static, 1)  
for (i=0; i<=n; i++)  
    sum += f(i);
```



The diagram shows the text "schedule (static, 1)" from the code block above. Two blue lines point from the words "static" and "1" to the labels "schedule type" and "chunk size" respectively.

### Scheduling types:

1. **static** – iterations are assigned to threads before loop executes;
2. **dynamic** – iterations are assigned to threads at run time (during loop exec.);  
possibly, some threads more, some threads less;
3. **auto** – compiler and/or run-time system determines and assigns;
4. **run time** – run-time system determines scheduling;

ex)  $n=12$ ,  $P=3$

schedule (static, 1) → Th0: 0, 3, 6, 9

Th1: 1, 4, 7, 10

Th2: 2, 5, 8, 11

schedule (static, 2) → Th0: 0, 1, 6, 7

Th1: 2, 3, 8, 9

Th2: 4, 5, 10, 11

schedule (static, n/P) → Th0: 0, 1, 2, 3

//same as default Th1: 4, 5, 6, 7

//block scheduling Th2: 8, 9, 10, 11

## dynamic scheduling

Each thread requests the next chunk (to the run-time system) when current chunk is done; this repeats until all done.

ex) `schedule (dynamic, 1)` //each time, chunk size 1

```
schedule (dynamic, 2)  //each time, chunk size 2
```

...

schedule (guided) //a kind of dynamic scheduling

Each chunk size is reduced by  $n/P$  and assigned to available threads at run time.

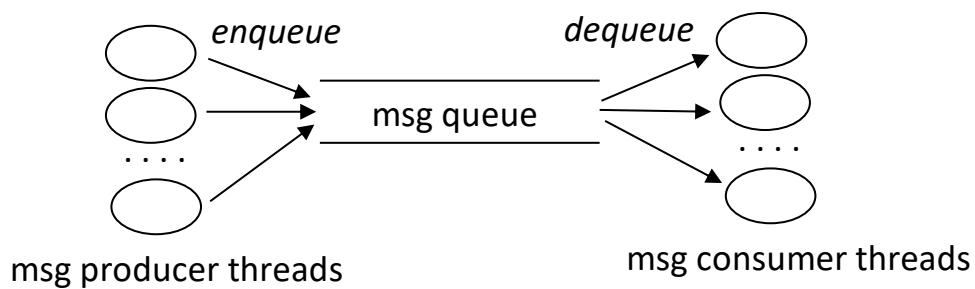
ex)  $n=1000$ ,  $P=2$

schedule (guided) → Tho: 500 (1~500)

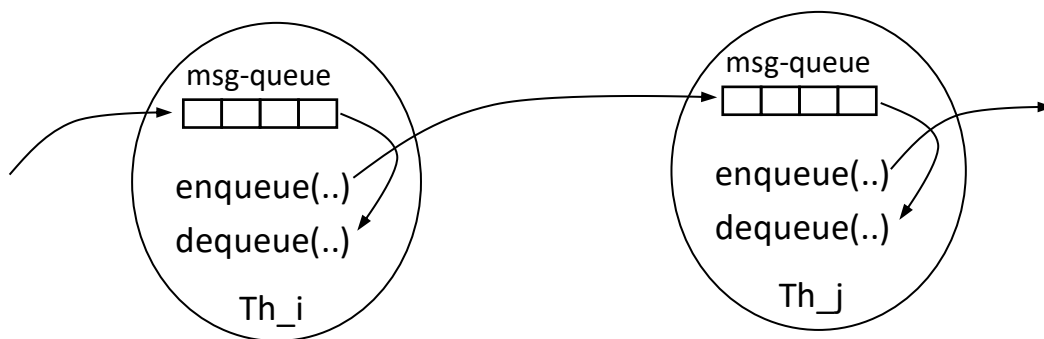
Th<sub>1</sub>: 250 (501~750)

Th<sub>1</sub>: 125 (751~875)

## Producers-consumers with OpenMP

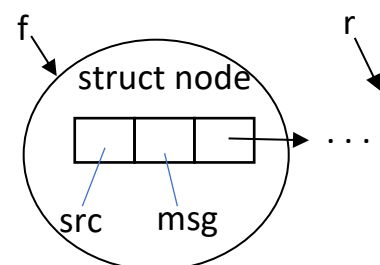
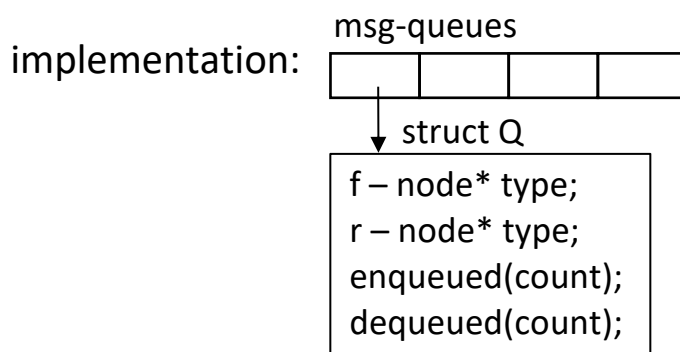
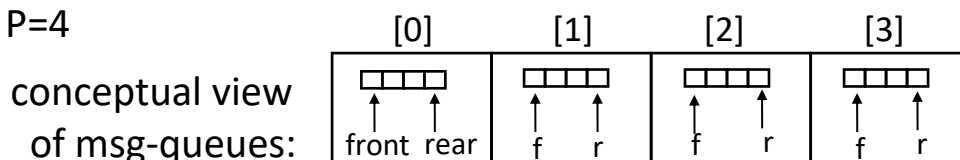


- Message passing mechanism is implemented in shared-mem programming.
- In each thread, enqueue/dequeue operations may repeat; and a thread may send (enqueue) message to any other thread.



Implementation: 2D dynamic array of msg-queues (one for each thread);  
each msg-queue is implemented with linked-list of nodes;

ex) P=4



in master thread (main),

```
declare (new) msg_queues (struc Q** type); //new 1st dimension
```

• • • •

```
#pragma omp parallel . . . .
```

$$\{ \dots \}$$

```
msg_queues [my_rank] = new struct Q; //in each thread_i, new 2nd dim.
```

```
#pragma omp barrier; //don't let any threads send msgs until all  
                      //msg queues are constructed by all threads
```

```

//msg queues are constructed by all threads
possibly, repeats {
    #pragma omp critical
    enqueue (msg_queues [dest], my_rank, msg); //send msg -mutex needed
    dequeuer (msg_queues [my_rank], src, msg); //receive msg
    .....
}

```

```
free/delete msg queues [my rank]; //free 2nd dimension in each thread
```

```
} //pragma omp parallel
```

```
free/delete msg_queues; //free 1st dimension
```

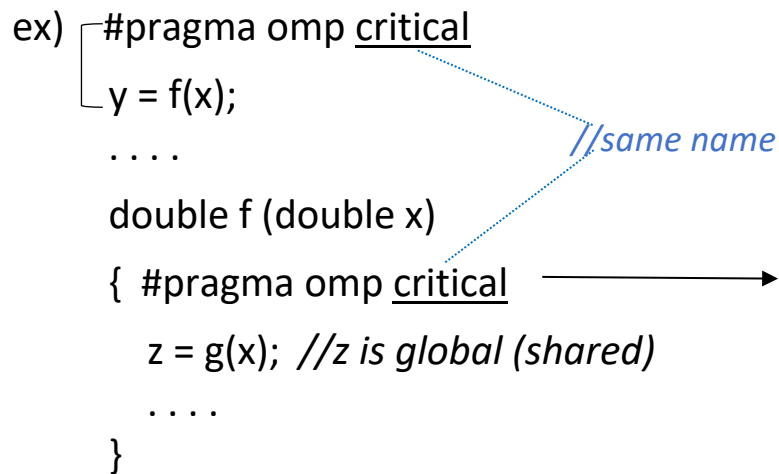
enqueue(..) and dequeue(..) use linked-list implementation of queue;

enqueue(..) operation is C.S. → needs mutex mechanism;

- `#pragma omp barrier` – provides barrier synchronization;
- `#pragma omp atomic` – similar to “critical”, but used for only single assignment statement in the form of load-modify-store, e.g., `x += 5`, which needs load x; modify x; then, store x;  
*//more efficient than critical*  
 ex) `x += <exp>; -=, *=, /=`  
`x++, x--, ++x, --x`

## dead-lock case with nested critical

```
ex) { #pragma omp critical
      y = f(x);
      ....
      double f (double x)
      { #pragma omp critical
        z = g(x); //z is global (shared)
        ....
      }
```



At this moment of time,  
"critical" is locked by myself  
(in this thread) and cannot  
unlock it. → **dead-locked**

→ Sol: using named critical *//any name*

```
ex) { #pragma omp critical (one)
      y = f(x);
      ....
      double f (double x)
      { #pragma omp critical (two)
        z = g(x);
        ....
      }
```

