

The Fine Structure Constant as a Universal Function of Causal Diamond Geometry

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Abstract

We propose that the fine structure constant can be modeled as a universal function of local causal diamond geometry, contingent on the information-processing primacy postulate and the Quantum-Thermodynamic Entropy Partition (QTEP) framework. The electromagnetic coupling emerges from three information-theoretic components—holographic projection, geometric phase space structure, and vacuum screening—whose normalizations are fixed by prior entropy mechanics analyses of black holes and collider data. The resulting formula $\alpha^{-1} = \frac{1}{2} \ln(\pi c^5 / \hbar G H^2) - \ln(4\pi^2) - 1/(2\pi)$ depends only on the Hubble parameter H and fundamental constants. Evaluating at $H = H_0$ yields $\alpha^{-1} = 137.032$, consistent with CODATA 2018 at the 0.003% level. At the Recombination epoch, it yields $\alpha^{-1} \approx 127$, providing a candidate information-theoretic boundary condition for high-energy QED running.

Keywords: Fine structure constant; Causal diamonds; Holographic principle; Universal function; Information theory; Scale invariance

1 Introduction

The fine structure constant $\alpha \approx 1/137$ characterizes the strength of electromagnetic interactions between charged particles. Since Sommerfeld’s introduction of this dimensionless quantity in 1916, its precise value has been measured with extraordinary accuracy, yet its origin remains one of the great mysteries of theoretical physics. In conventional Quantum Electrodynamics (QED), α appears as an arbitrary free parameter that must be determined experimentally. Feynman famously described it as “one of the greatest damn mysteries of physics: a magic number that comes to us with no understanding by man” [1].

Beyond the Standard Model description of α as a free parameter, recent work in entropy mechanics and Quantum-Thermodynamic Entropy Partition (QTEP) has developed a quantum-information-theoretic account of irreversibility, based on a bipartite decomposition of von Neumann entropy into coherent and decoherent components and the quantization of thermodynamic irreversibility into indivisible units called obits [8, 9]. In that framework the structure and normalization of entropy deficits associated with decoherent outcomes are fixed by consistency with black hole thermodynamics and with particle physics and antimatter gravity experiments, rather than tuned to any particular coupling. The present paper applies these established information-theoretic postulates to causal-diamond geometries and shows that, once this is done, the electromagnetic coupling emerges as a universal function of causal horizon entropy with no remaining freedom to adjust additive constants without spoiling the entropy mechanics construction.

In this paper, we investigate the consequences of treating the fine structure constant as a universal function $\alpha(\tau)$ of local causal diamond geometry, as implied by the entropy mechanics and QTEP treatment of irreversible quantum processes embedded in curved spacetime. The electromagnetic coupling at any spacetime point can be modeled as emerging from the information-processing capacity of the local causal diamond structure $I^+(p) \cap I^-(q)$ with proper time separation τ . This framework seeks

to unify seemingly disparate phenomena—the “running” of α with energy in quantum electrodynamics, the cosmic evolution of fundamental constants, and the measured low-energy value—as manifestations of one universal information-theoretic mechanism evaluated at different local conditions.

A key insight of this work is the proposal that what we categorize as atomic, nuclear, or cosmic scales represent human classifications of different accessible fractions of the holographic boundary that instantiates physical reality. There is one causal diamond—the cosmic horizon—and physical processes access different portions of its holographic surface area.

By analyzing information transfer constraints at causal diamond boundaries, we derive an analytical expression for $\alpha(H)$ depending only on the Hubble parameter and fundamental constants. When evaluated at the present cosmological expansion ($H = H_0$), this yields $\alpha^{-1} = 137.032$, in agreement with experimental measurements of low-energy electromagnetic processes. The same formula evaluated at Recombination ($z \approx 1100$) yields $\alpha^{-1} \approx 127$.

An intriguing numerical coincidence emerges: this Recombination-era value lies close to the QED coupling strength at the electroweak scale ($\alpha^{-1} \approx 128$ at the Z mass). Whether this proximity reflects a deeper physical connection or is merely accidental remains an open question that we flag for future investigation. This work does not derive a mapping between particle physics energies and cosmological epochs; rather, it presents a geometric framework for the low-energy boundary value and notes the high-energy coincidence as a curiosity.

2 Scope and Limitations

This paper proposes a geometric origin for the fine structure constant’s boundary values within the specific information-theoretic ontology of entropy mechanics and QTEP. We do not modify the Standard Model calculation of $\alpha(E)$ evolution; instead, we show that its low- and high-energy limits are consistent with a single information-geometric relation between α and causal-diamond entropy, provided the QTEP postulates about irreversibility and obit counting on null boundaries hold. While the framework identifies candidate endpoints of the renormalization group flow, the detailed trajectory $\alpha(E)$ remains the domain of conventional QED perturbation theory. The specific geometric factors introduced in the following section are motivated by holographic arguments but represent structural assumptions about how the electromagnetic sector is encoded on the causal diamond boundary.

The QTEP postulates used here are not derivable from classical general relativity or standard quantum field theory alone. They are additional information-theoretic principles motivated and tested in other contexts [10, 11], and are taken as given in this work. Within that extended ontology, the structure and normalization of the non-logarithmic terms in $\alpha^{-1}(H)$ are fixed and no longer tunable.

Importantly, this work does not derive the mapping between particle physics interaction energy E and an effective Hubble parameter $H_{\text{eff}}(E)$. The universal function $\alpha^{-1}(H)$ is well-defined for cosmological H values, but extending it to particle physics scales requires a physical principle connecting localized high-energy processes to holographic information capacity. This mapping remains an open theoretical question. When we note that the Recombination-era value $\alpha^{-1} \approx 127$ lies close to the QED value at the Z mass, this should be understood as a numerical curiosity inviting further investigation, not as a derived result.

In this sense the construction is intended to be complementary to quantum field theory rather than competitive with it. The universal function $\alpha(\tau)$ provides candidate boundary conditions that any microscopic description of the electromagnetic interaction might respect, given causal-diamond information geometry. As long as the Standard Model running of $\alpha(E)$ interpolates between values compatible with these information-theoretic endpoints, there is no conflict with QED or with the broader framework of quantum field theory in curved spacetime.

3 Universal Information-Processing Architecture

3.1 Entropy Mechanics, QTEP, and Obits

The present work builds on the entropy mechanics and Quantum-Thermodynamic Entropy Partition (QTEP) framework introduced in Refs. [8, 10, 11]. In that approach, quantum states are described on a Hilbert space confined within the geometry of a causal diamond representing the cosmic horizon

endowed with a bipartite entropy structure. The von Neumann entropy

$$S(\rho) = -\text{Tr}(\rho \ln \rho) \quad (1)$$

is partitioned into coherent and decoherent components,

$$S_{\text{total}} = S_{\text{coh}} + S_{\text{decoh}}, \quad S_{\text{coh}} = \ln 2, \quad S_{\text{decoh}} = \ln 2 - 1, \quad (2)$$

so that $S_{\text{coh}} \approx 0.693$ and $S_{\text{decoh}} \approx -0.307$ in natural information units. Coherent entropy characterizes logically reversible, phase-coherent quantum superpositions, while decoherent entropy quantifies the information deficit associated with irreversible measurement outcomes and environmental decoherence. Irreversibility is quantized in units of an obit, defined as the minimal entropy increment required for a logically irreversible quantum transition. This obit structure is fixed by demanding consistency with Landauer-type bounds and with black hole entropy counting, and has been applied successfully to the information budget of black hole evaporation and to a priori predictions for ATLAS and ALPHA-g experiments [10, 11].

Within this framework, the ratio $S_{\text{coh}}/|S_{\text{decoh}}| \approx 2.257$ and the total entropy $S_{\text{total}} = 2 \ln 2 - 1$ emerge as universal quantities that govern the balance between coherent and decoherent sectors. When QTEP is embedded in causal-diamond geometries, obits must be encoded on thermodynamic (null) boundaries, and the counting of obit channels along angular directions and light-cone sectors fixes the normalization of entropy deficits associated with vacuum polarization and phase space on the holographic boundary.

3.2 Causal Diamonds and Local Information Capacity

At every spacetime point x^μ , the geometry defines a causal diamond—the intersection of future and past light cones $I^+(p) \cap I^-(q)$ with proper time separation τ . This geometric structure, rigorously formulated by Gibbons and Solodukhin [2], provides the fundamental arena for information processing in the universe.

The Hubble parameter H characterizes the information capacity of the cosmic causal diamond through the Bekenstein-Hawking entropy [3]. In a homogeneous cosmology, H depends only on cosmic time (or equivalently, redshift z). The total holographic information available on the cosmic horizon is:

$$S_H(\tau) = \frac{\pi c^5}{\hbar G H(\tau)^2} \quad (3)$$

This holographic bound constrains the maximum information encodable on the cosmic horizon boundary. If we associate the local causal diamond duration τ with the Hubble time such that $H(\tau) \approx 2/\tau$ (corresponding to the causal horizon diameter crossing time), we recover the area-law scaling $S \propto A \propto \tau^2$. For the purposes of this derivation, we treat $H(\tau)$ as the primary defining parameter of the local information geometry.

The Margolus-Levitin theorem [4] further limits information processing rates to $\gamma = H/\ln(S_H)$, representing how quickly quantum information can be transformed.

The explicit forms of S_H and the information-processing rate γ used here follow from the entropy mechanics analysis of causal diamonds presented in Ref. [8].

Crucially, different physical processes do not probe different causal diamonds—there is one cosmic causal diamond whose holographic boundary instantiates reality. Rather, processes at different energy scales access different fractions of this total holographic information. The relationship between energy and holographic access emerges from localization: a process with characteristic energy E is spatially localized to region $\Delta x \sim \hbar c/E$. This localized region can only access the holographic information within its past light cone, which represents a fraction of the total cosmic horizon proportional to $(\Delta x/r_H)^2 \sim (\hbar c H/E)^2$.

For high-energy processes ($E \gg \hbar c H$), spatial localization to $\Delta x \sim \hbar c/E$ restricts access to holographic information within a solid angle $\Delta\Omega \sim (\Delta x/r_H)^2 \sim (\hbar c H/E)^2$, yielding effective information capacity $S_{\text{eff}} \sim S_H \times (\hbar c H/E)^2 \ll S_H$. For low-energy processes ($E \sim \hbar c H$), nearly the full solid angle is accessible, approaching $S_{\text{eff}} \approx S_H$. This geometric relationship between energy and holographic access—not a proliferation of different-sized causal diamonds—underlies the apparent scale-dependence of electromagnetic coupling.

4 Derivation of the Universal Function $\alpha(\tau)$

4.1 Information-Theoretic Constraints on Electromagnetic Coupling

The electromagnetic coupling α is proposed to be determined by the accessible holographic information capacity. Within the entropy mechanics framework, three distinct information-geometric effects contribute to α^{-1} : holographic projection from area to linear scale, normalization of electromagnetic phase space on the causal-diamond boundary, and a universal vacuum-screening correction associated with entropy of virtual fluctuations.

4.2 Holographic Projection: Area-to-Volume Scaling

Electromagnetic interactions occur in 3-dimensional spatial volumes but access information encoded on 2-dimensional holographic screens [5, 6, 7]. In the causal-diamond geometry the Bekenstein-Hawking entropy scales as $S_H \propto A \propto L^2$, where L is the characteristic bulk linear size. Taking logarithms gives

$$\ln S_H = \ln(\kappa L^2) = \ln \kappa + 2 \ln L, \quad (4)$$

for some dimensionless constant κ . Any logarithmic dependence of the coupling on the bulk interaction scale L must therefore appear through $\ln L = \frac{1}{2}(\ln S_H - \ln \kappa)$. Additive constants in $\ln S_H$ correspond to overall rescalings of the phase-space and vacuum terms considered below, so the uniquely fixed holographic contribution takes the form

$$\alpha_{\text{holo}}^{-1}(\tau) = \frac{1}{2} \ln(S_H(\tau)) \quad (5)$$

The identification of $\frac{1}{2} \ln S_H$ as the holographic contribution to α^{-1} follows the same projection used in entropy mechanics to relate area-law entropies of causal horizons to effective bulk length scales and information-processing rates [8].

4.3 Geometric Phase Space in Curved Spacetime

Electromagnetic field modes within a causal diamond occupy a phase space constrained by the spherical holographic boundary. In flat spacetime the angular part of this phase space carries the solid angle measure $\int_{S^2} d\Omega = 4\pi$, and Maxwell theory provides two physical polarizations. In the causal-diamond setting there is, in addition, an antipodal identification between past- and future-directed null generators on the boundary, so that the effective angular phase-space weight can be written as

$$\Omega_{\text{eff}} \sim 4\pi \times \pi = 4\pi^2, \quad (6)$$

where the factor of π encodes the pairing of antipodal directions on S^2 into single boundary data on the diamond. In the small-diamond geometry analyzed by Gibbons and Solodukhin [2], the causal diamond boundary is generated by null geodesics that intersect on round two-sphere cross-sections. Each physical direction on this S^2 can be reached either along an ingoing generator from the past tip or an outgoing generator toward the future tip, and the causal diamond geometry relates these by an antipodal map. In the present framework we treat electromagnetic boundary data as living on the quotient of this double covering, so that past- and future-directed generators carrying the same physical direction are counted once in the angular phase space.

Within entropy mechanics this choice is not adjustable: the same $4\pi^2$ normalization appears in the orbit counting on causal-diamond boundaries that underlies the information pressure thresholds and discrete energy hierarchy analyzed in Refs. [10, 11]. Replacing $4\pi^2$ by $2\pi^2$ or $8\pi^2$ would spoil that consistency and would correspond to either discarding the antipodal identification or double-counting boundary channels in the underlying QTEP construction. In logarithmic information units this normalization of available field configurations appears as a subtractive term in α^{-1} ,

$$\alpha_{\text{geom}}^{-1}(\tau) = -\ln(4\pi^2) \quad (7)$$

4.4 Vacuum Polarization from Geometric Screening

Vacuum polarization screens electromagnetic coupling. In the QTEP framework, this screening is associated with a universal entropy deficit carried by virtual fluctuations that occupy part of the information-processing capacity along each angular direction on the holographic boundary. For a full angular range $0 \leq \theta < 2\pi$, and two independent light-cone sectors at the boundary, this corresponds to a constant correction of magnitude 1 distributed uniformly over 2π radians per sector. The resulting scale-independent contribution to α^{-1} is

$$\alpha_{\text{vac}}^{-1} = -\frac{1}{2\pi} \quad (8)$$

The magnitude of this universal correction is inherited directly from the QTEP assignment of one orbit of irreducible entropy deficit per full 2π angular range per light-cone sector at a thermodynamic boundary [10, 11]. In that setting the same $-1/(2\pi)$ contribution appears in the entropy budget of black hole horizons and in the analysis of information pressure at collider and antimatter gravity experiments [11]. Altering this value would break those previous applications and is therefore not regarded as a free parameter in the present work.

4.5 Universal Formula

Combining these three information-geometric contributions yields the universal expression

$$\alpha^{-1}(\tau) = \frac{1}{2} \ln\left(\frac{\pi c^5}{\hbar G H(\tau)^2}\right) - \ln(4\pi^2) - \frac{1}{2\pi} \quad (9)$$

where H characterizes the accessible holographic information through $S_H = \pi c^5 / (\hbar G H^2)$. This universal function governs electromagnetic coupling for any degree of holographic access within the entropy mechanics framework.

It is useful to summarize which elements of this construction are inherited from earlier work and which steps are specific to the present application. The appearance of $S_H = \pi c^5 / (\hbar G H^2)$ as the relevant entropy scale follows from the standard Bekenstein-Hawking relation applied to causal horizons [3] and from the small-diamond geometry of Ref. [2]. The logarithmic dependence $\frac{1}{2} \ln S_H$ is the same holographic projection used in entropy mechanics to relate area-law entropies to bulk length scales [8]. On top of these geometric ingredients, we import two information-theoretic postulates from the QTEP framework: the $4\pi^2$ normalization of electromagnetic phase space on the causal-diamond boundary, and the universal $-1/(2\pi)$ entropy deficit per angular channel. Once these elements are in place, there is no remaining freedom to tune an arbitrary constant in $\alpha^{-1}(\tau)$.

The key properties of this formula are: universal mechanism (same formula for all holographic access fractions), access-dependent results (different accessible S_H yields different α), no additional fit parameters beyond the fixed structural constants encoded in the geometric and vacuum terms, and dimensional consistency (all terms dimensionless).

5 Universal Application Within A Causal Diamond Geometry

5.1 Evaluating $\alpha(\tau)$ at Different Local Conditions

The universal formula applies identically across vastly different accessible fractions of the holographic boundary. We demonstrate this by evaluating at representative conditions spanning cosmic history and particle physics.

5.1.1 Present Cosmological Expansion ($\tau = 1/H_0$)

At the present epoch, cosmic expansion defines causal diamonds with:

$$\tau_0 = \frac{1}{H_0} = \frac{1}{2.18 \times 10^{-18} \text{ s}^{-1}} \approx 4.58 \times 10^{17} \text{ s} \quad (10)$$

Evaluating the universal formula:

$$\begin{aligned}\alpha^{-1}(\tau_0) &= \frac{1}{2} \ln\left(\frac{\pi c^5}{\hbar G H_0^2}\right) - \ln(4\pi^2) - \frac{1}{2\pi} \\ &= 140.867 - 3.676 - 0.159 = 137.032\end{aligned}\tag{11}$$

This matches low-energy electromagnetic measurements (CODATA 2018: $\alpha^{-1} = 137.035999084$) with 0.003% accuracy. The numerical value quoted here is stable under small variations of H_0 and of the fundamental constants, as detailed in Sec. ??, but the dominant theoretical uncertainty is set by the approximations entering the causal-diamond geometry and the cosmological determination of H_0 . The 0.003% agreement with the CODATA low-energy value should therefore be interpreted as an internally consistent numerical check of the framework rather than as a claim of predictive accuracy at the 10^{-5} level.

5.1.2 Cosmic Recombination ($\tau \approx 10^{13}$ s)

At recombination ($z \approx 1100$), $H(z) = 4.47 \times 10^{-14}$ s $^{-1}$, giving $\tau_{\text{rec}} \approx 2.24 \times 10^{13}$ s:

$$\alpha^{-1}(\tau_{\text{rec}}) = \frac{1}{2} \ln\left(\frac{\pi c^5}{\hbar G H(z=1100)^2}\right) - \ln(4\pi^2) - \frac{1}{2\pi} \approx 127.1\tag{12}$$

This value corresponds, within the present framework, to the bare electromagnetic coupling associated with the causal-diamond geometry at early times, before local atomic processes probe smaller τ values. It should therefore be regarded as a geometric boundary condition on the high-energy behavior of α , not as a replacement for the detailed renormalization group evolution computed in QED.

5.1.3 High-Energy Particle Physics and Recombination Limit

Conventional Quantum Electrodynamics observes that α^{-1} decreases to approximately 128 at the electroweak scale ($E \sim 91$ GeV) [12]. In our framework, this value corresponds to the fundamental holographic saturation limit defined by the Recombination era.

At recombination ($z \approx 1100$), the Hubble parameter $H(z) \approx 4.5 \times 10^{-14}$ s $^{-1}$ defines a causal diamond with $\tau_{\text{rec}} \approx 2.2 \times 10^{13}$ s. Evaluating the universal formula at this epoch yields:

$$\alpha^{-1}(\tau_{\text{rec}}) = \frac{1}{2} \ln\left(\frac{\pi c^5}{\hbar G H(z=1100)^2}\right) - \ln(4\pi^2) - \frac{1}{2\pi} \approx 127.1\tag{13}$$

This result lies within about 1% of the value of α^{-1} at the Z boson mass (≈ 128). In the information-theoretic picture adopted here, this numerical proximity suggests that the causal-diamond geometry at Recombination provides a natural upper bound on the effective electromagnetic coupling reached in high-energy processes. The resulting value $\alpha^{-1}(\tau_{\text{rec}}) \approx 127.1$ lies within about one percent of the Standard Model value of α^{-1} at the Z mass. Given the theoretical and cosmological uncertainties entering the present estimate, and the fact that the mapping between local interaction energy and effective H is not derived here, we interpret this proximity as a suggestive boundary-condition consistency rather than as a precise high-energy prediction. We emphasize that our calculation supplies a candidate boundary value compatible with QED evolution; it does not attempt to reproduce the full renormalization group trajectory or its scheme dependence.

The physical significance of this match lies in the nature of the Recombination Surface as the boundary of the electromagnetic phase space. Since photons decoupled from matter at this epoch, the Recombination Surface represents the maximum information horizon for electromagnetic interactions. High-energy processes, by probing the saturation limits of the field, are holographically constrained by the information capacity of this boundary. The "running" of α thus describes the transition between the information capacity of the present cosmic horizon ($\alpha^{-1} \approx 137$) and the limiting capacity of the Recombination horizon.

5.2 Reinterpreting QED Running as Boundary Conditions

Quantum electrodynamics describes α as “running” with energy according to renormalization group equations. The entropy mechanics framework interprets this running as the transition between two holographically defined boundary conditions.

Low-energy processes access the full information content of the current cosmic horizon (H_0), yielding $\alpha^{-1} \approx 137$. As interaction energy increases, the system is expected to approach, but not exceed, the holographic density characteristic of the Recombination era, where the electromagnetic sector decoupled from the primordial plasma.

This framework does not replace the Renormalization Group (RG) evolution, but rather provides a geometric interpretation for the boundary values that the RG flow appears to approach at low and high energies. Standard QED describes how the coupling evolves between these limits, including loop corrections, particle content, and scheme dependence. In the present picture the ratio between the present Hubble scale and the Recombination scale constrains the total span of the running coupling, anchoring but not determining the detailed RG trajectory.

5.3 Why Atomic Measurements Show No Variation

There is no compensation mechanism between cosmic evolution and QED running. Both arise from evaluating the same universal function.

At recombination ($z = 1100$): the cosmic causal diamond has $\tau_{\text{cosmic}} \sim 10^{13}$ s yielding $\alpha^{-1} \approx 127$, while local atomic processes have $\tau_{\text{atom}} \sim 10^{-15}$ s yielding $\alpha^{-1} \approx 137$.

At present ($z = 0$): the cosmic causal diamond has $\tau_{\text{cosmic}} \sim 10^{18}$ s yielding $\alpha^{-1} \approx 137$, while local atomic processes still have $\tau_{\text{atom}} \sim 10^{-15}$ s yielding $\alpha^{-1} \approx 137$.

Atomic measurements always probe τ_{atom} determined by binding energies, not τ_{cosmic} determined by cosmological expansion. As the universe evolves, τ_{cosmic} changes, but τ_{atom} remains constant. The measured α from atomic spectroscopy reflects the local physics (small τ), not the cosmic background (large τ).

This explains why quasar absorption spectroscopy shows no variation in α despite cosmic evolution [14, 15]: all such measurements probe atomic transitions with fixed $\tau_{\text{atom}} \sim 10^{-15}$ s, yielding constant $\alpha^{-1} \approx 137$ at all redshifts.

5.4 Theoretical Scope

Within the entropy mechanics framework, a single universal function relates electromagnetic coupling to accessible holographic information. No additional independent mechanism is introduced to account for energy dependence of α (same formula, different τ), cosmic evolution of bare coupling (changing τ_{cosmic} with redshift), constancy of measured α (fixed τ_{atom} in atomic processes), or the boundary values of QED renormalization group running.

All of these phenomena are interpreted as the same information-theoretic architecture evaluated at different causal diamond geometries, while the detailed form of $\alpha(E)$ between the low- and high-energy limits remains described by conventional QED perturbation theory.

6 Experimental Validation at Cosmological τ

We now validate the universal formula by evaluating at $\tau = 1/H_0$, corresponding to causal diamonds defined by present cosmological expansion. This particular evaluation should match low-energy electromagnetic measurements, which probe similar large- τ regimes through atomic processes.

6.1 Calculation of Information Parameters

Converting the Hubble constant to SI units:

$$H_0 = 67.4 \text{ km s}^{-1} \text{ Mpc}^{-1} \approx 2.184 \times 10^{-18} \text{ s}^{-1} \quad (14)$$

The logarithmic information term:

$$\ln(S_H) = \ln\left(\frac{\pi c^5}{\hbar G H_0^2}\right) \approx 281.733 \quad (15)$$

Using fundamental constants $c = 2.9979 \times 10^8$ m/s, $\hbar = 1.0546 \times 10^{-34}$ J s, and $G = 6.6743 \times 10^{-11}$ m³ kg⁻¹ s⁻².

6.2 Prediction

Evaluating each term:

$$\text{Holographic term: } \frac{1}{2} \ln(S_H) = 140.867 \quad (16)$$

$$\text{Geometric term: } -\ln(4\pi^2) = -3.676 \quad (17)$$

$$\text{Vacuum term: } -\frac{1}{2\pi} = -0.159 \quad (18)$$

The universal formula evaluated at present cosmological conditions:

$$\alpha^{-1}(\tau_0 = 1/H_0) = 137.032 \quad (19)$$

6.3 Comparison with Experiment

The CODATA 2018 recommended value [16]:

$$\alpha_{\text{exp}}^{-1} = 137.035999084(21) \quad (20)$$

The relative difference of 0.003% is consistent with the information-theoretic mechanism within current experimental and cosmological uncertainties. In this sense, the present-epoch evaluation of the universal function provides a nontrivial numerical check on the framework at one particular τ value that happens to match the regime probed by laboratory measurements.

6.4 Sensitivity to Hubble Parameter

Table 1 presents the universal formula evaluated at different H_0 values:

Table 1: Universal function $\alpha^{-1}(\tau = 1/H_0)$ evaluated for various Hubble parameter values.

| H_0 Source | H_0 (km/s/Mpc) | α^{-1} | Error (%) |
|-----------------------|------------------|---------------|-----------|
| Planck 2018 (low) | 66.9 | 137.039 | 0.002 |
| Planck 2018 (central) | 67.4 | 137.032 | 0.003 |
| Planck 2018 (high) | 67.9 | 137.024 | 0.009 |
| ACT DR6 | 68.3 | 137.018 | 0.013 |
| Intermediate | 70.0 | 136.994 | 0.031 |
| SH0ES (central) | 73.0 | 136.952 | 0.061 |

The systematic trend reflects the logarithmic dependence on $H(\tau)$: larger H_0 corresponds to smaller τ_0 , yielding smaller α^{-1} (stronger coupling). Within this framework, a larger H_0 corresponds to a slightly stronger predicted low-energy electromagnetic coupling. This mapping is not an independent determination of H_0 , since it relies on importing the QTEP postulates and on the causal-diamond interpretation adopted here, but it does provide a way to confront the combined structure with future improvements in both α and H_0 measurements.

7 Discussion

7.1 Scale Invariance in Information Processing

The central idea of this work is the proposal that scale dependence in physics may be emergent from a unified information-processing architecture. Given the information-primacy postulate and the QTEP realization of quantum irreversibility, the electromagnetic coupling $\alpha(\tau)$ is modeled as emerging from local causal diamond geometry at every spacetime point.

Within this construction, the holographic relation provides a scale-invariant organizing principle: the same information-processing mechanism

$$S_H(\tau) = \frac{\pi c^5}{\hbar G H(\tau)^2} \approx \frac{\pi c^5 \tau^2}{4 \hbar G} \quad (21)$$

applies whether $\tau = 10^{-43}$ s (Planck scale) or $\tau = 10^{18}$ s (horizon scale), where the approximate equality uses $H(\tau) \approx 2/\tau$ corresponding to the causal horizon diameter crossing time. Different τ values yield different coupling strengths, but this reflects evaluating one universal function at different arguments rather than altering the underlying microscopic quantum field theory.

7.2 Unification of Apparently Disparate Phenomena

This framework offers a common information-theoretic perspective on phenomena that are traditionally treated as distinct.

QED Running: In this picture the energy-dependence $\alpha(E)$ is interpreted as arising from high-energy processes accessing reduced fractions of the holographic boundary, subject to the constraint that the effective coupling should remain between the values associated with the present horizon and with Recombination. The Recombination era then appears as a natural saturation limit for this running, while the detailed shape of $\alpha(E)$ between those limits is still governed by QED.

Cosmic Evolution: As the universe expands, the cosmic Hubble parameter evolves, changing the total holographic information capacity. The full-access coupling tracks this evolution in the present framework, yet atomic measurements access fixed fractions determined by atomic binding energies, yielding constant observed α for local processes even as the cosmic boundary conditions change.

Lorentz Invariance: Boosted observers probe electromagnetic interactions at different effective energies, corresponding to different τ values. The universal function $\alpha(\tau)$ can in principle be evaluated consistently in any local rest frame, but the underlying Lorentz invariance remains that of the Standard Model; the information-theoretic architecture is required to be compatible with, not a modification of, this symmetry.

All three phenomena can thus be viewed as arising from a single organizing mechanism: the holographic information-processing architecture evaluated at locally relevant causal diamond geometries, subject to the requirement that it remain consistent with known quantum field theory behavior in each regime.

From a conventional field-theoretic perspective, the most important open tasks are to derive the mapping between local interaction energy E and effective expansion rate $H_{\text{eff}}(E)$ from a more microscopic treatment of quantum fields in causal diamonds, and to understand whether the QED β -function can itself be obtained from the orbit-based entropy counting that underlies entropy mechanics. At present we only require that the Standard Model running of $\alpha(E)$ interpolate between values compatible with the low- and high-energy boundary conditions implied by $\alpha^{-1}(H)$, while leaving the detailed trajectory and scheme dependence to conventional renormalization group analyses.

7.3 Why $\alpha \approx 1/137$

Within this framework the numerical value $\alpha \approx 1/137$ can be traced to three universal constraints: holographic projection (factor 1/2 from area-volume dimensional reduction), geometric structure ($-\ln(4\pi^2)$ from electromagnetic field phase space in curved spacetime), and vacuum screening ($-1/(2\pi)$ from the inverse angular measure of holographic boundary integration).

Evaluated at $\tau \sim 10^{18}$ s (present cosmological expansion) or $\tau \sim 10^{-15}$ s (atomic binding), these constraints yield $\alpha^{-1} \approx 137$ within the approximations used here. At smaller τ (higher energies), the logarithmic term dominates, giving stronger coupling.

The resulting value can be interpreted as the binding factor required to maintain electromagnetic coherence across many orders of magnitude in τ , from Planck scale to horizon scale. In this interpretation the apparent fine-tuning is attributed to geometric and information-theoretic constraints rather than to anthropic selection.

7.4 Testable Predictions and Inferred H_0

The universal formula makes several testable predictions and also permits an inverse inference of the present Hubble parameter from the measured low-energy value of α .

For H_0 dependence, evaluating at different cosmological H_0 values (Planck versus SH0ES, for example) predicts different α^{-1} ranging from 137.032 ($H_0 = 67.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$) to 136.952 ($H_0 = 73.0 \text{ km s}^{-1} \text{ Mpc}^{-1}$). The trend is monotonic: larger H_0 leads to smaller α^{-1} (stronger coupling). This means that, within the entropy mechanics framework, any independently measured H_0 value immediately maps to a predicted low-energy electromagnetic coupling that can be checked against laboratory determinations.

Conversely, one may invert the relation to infer an effective H_0 from the CODATA value of α . Using Eq. (39) and treating c , \hbar , G , and $\alpha_{\exp}^{-1} = 137.035999084(21)$ as inputs, one obtains an inferred Hubble parameter $H_{0,\text{inf}}$ that is numerically close to the Planck 2018 value and in tension with the higher SH0ES determination. The precise numbers depend only weakly on the fundamental constants through logarithms, and a quantitative comparison can be made by propagating the CODATA uncertainty on α together with current cosmological error bars on H_0 . In this sense the framework provides a mapping between electromagnetic precision measurements and cosmological parameters that can be sharpened as both sets of observations improve.

At high redshift, the same formula evaluated at $z \approx 1100$ with $H(z)$ from Λ CDM yields a bare coupling $\alpha_{\text{bare}}^{-1} \approx 127$ associated with the Recombination-era causal diamond. High-energy probes of the early universe that are sensitive to the effective strength of the electromagnetic interaction at that epoch (for example through detailed CMB damping-tail physics) could, in principle, test whether this boundary value is compatible with cosmological data, although working out such implications lies beyond the scope of the present paper.

7.5 Implications for Fundamental Physics

If further developed and supported, this line of reasoning would suggest that at least some dimensionless constants are not arbitrary parameters but emerge from the information-processing architecture of spacetime. In that case such constants would more naturally be viewed as universal functions of local causal diamond geometry.

This suggests a deep unity between quantum mechanics (through QTEP entropy partition), general relativity (through causal diamond geometry), thermodynamics (through holographic information bounds), and information theory (through Margolus-Levitin processing rates).

The framework indicates that what we perceive as fundamental forces may be different manifestations of information-processing constraints evaluated at different local conditions.

7.6 Relationship to Quantum Field Theory

This work does not replace quantum electrodynamics but reveals a potential information-theoretic foundation for its boundary conditions. QED's perturbative expansion remains valid as a computational tool for the trajectory between endpoints.

The renormalization group β -function $\beta(\alpha) = \alpha^2/(3\pi)$ describes how α varies with energy. The entropy mechanics framework suggests this β -function itself might be derivable from counting information degrees of freedom in multi-scale holographic processing architectures. The coefficient $1/(3\pi)$ likely reflects geometric factors and fermionic degrees of freedom projected onto holographic screens.

8 Conclusion

We have proposed that the fine structure constant can be modeled as a universal function of local causal diamond geometry:

$$\alpha^{-1}(\tau) = \frac{1}{2} \ln\left(\frac{\pi c^5}{\hbar G H(\tau)^2}\right) - \ln(4\pi^2) - \frac{1}{2\pi} \quad (22)$$

This formula applies at every spacetime point, with τ determined by local physical conditions. The three terms represent universal information-theoretic constraints within the entropy mechanics framework: holographic projection from 2D boundaries to 3D bulk (factor 1/2), geometric phase space structure of electromagnetic fields in curved spacetime ($-\ln 4\pi^2$), and vacuum polarization screening from the inverse angular measure of holographic boundary integration ($-1/2\pi$).

Evaluating at present cosmological expansion $\tau = 1/H_0$ yields $\alpha^{-1} = 137.032$, coinciding with experimental measurements at the 0.003% level. The same universal formula evaluated at recombination ($\tau \sim 10^{13}$ s) yields $\alpha^{-1} \approx 127$, lying close to the high-energy saturation value observed in particle physics. This suggests that the strongest possible electromagnetic coupling is constrained by the information capacity of the Recombination Surface, while remaining consistent with the established QED description of running between these boundary values.

The framework therefore offers a consistent description of limiting values of the coupling constant, interpreted as arising from the information capacity of causal-diamond geometries. What QED describes as “running” is interpreted here as the transition between the information capacity of the present cosmic horizon and the limiting capacity of the Recombination horizon. This transforms the question “Why does α equal 1/137?” into “Why does the universal function $\alpha(\tau)$, when evaluated at τ values relevant to electromagnetic interactions, yield the binding factor needed for Lorentz-invariant physics across many orders of magnitude?”

The answer suggested here is geometric constraint: the holographic information-processing architecture of spacetime selects this particular binding function within the entropy mechanics assumptions. In that sense fundamental constants are reinterpreted as universal functions, and their numerical values emerge from information-theoretic constraints on local causal diamond geometries, subject to the requirement that they remain compatible with standard quantum field theory.

The present analysis should therefore be viewed as a conditional statement: if the entropy mechanics and QTEP description of quantum irreversibility embedded in causal-diamond geometries is correct, then the fine structure constant at cosmological and recombination scales is constrained by a universal information-theoretic function of H . This conditional structure provides a clear target for future observational tests and for deeper theoretical derivations of the underlying information-theoretic postulates.

A Geometric and Entropic Ingredients

This appendix summarizes the geometric and entropic ingredients that enter the universal function $\alpha(\tau)$ and collects the main assumptions that go beyond standard general relativity and quantum field theory.

The Bekenstein-Hawking entropy for a causal horizon of Hubble radius $r_H = c/H$ is given by

$$S_H = \frac{k_B A}{4\ell_P^2} = \frac{\pi c^3}{G\hbar} \frac{c^2}{H^2} = \frac{\pi c^5}{\hbar G H^2}, \quad (23)$$

where $A = 4\pi r_H^2$ is the area of the horizon, $\ell_P^2 = G\hbar/c^3$ is the Planck area, and we set $k_B = 1$. This is the entropy bound used throughout the main text. In small-diamond constructions [2], the same scaling with H^{-2} appears for causal diamonds defined by local curvature.

Projecting this area-law entropy to an effective bulk length scale L proceeds by writing $S_H = \kappa L^2$ for some dimensionless constant κ that encodes the details of the causal-diamond embedding. Taking logarithms yields

$$\ln S_H = \ln \kappa + 2 \ln L. \quad (24)$$

Any dependence of the electromagnetic coupling on the bulk scale L that is logarithmic in information units must therefore appear through $\ln L = \frac{1}{2}(\ln S_H - \ln \kappa)$. Since additive constants in $\ln S_H$ are degenerate with rescalings of other information-theoretic contributions, the term $\frac{1}{2} \ln S_H$ is regarded as the uniquely fixed holographic projection in this framework, while $\ln \kappa$ is absorbed into the structural constants encoded by the geometric and vacuum-screening terms.

The $4\pi^2$ normalization of electromagnetic phase space on the causal-diamond boundary is motivated by two ingredients. First, the angular part of the bulk phase space on a round two-sphere carries the solid angle measure $\int d\Omega = 4\pi$, reflecting the usual S^2 geometry. Second, in the small-diamond picture there is an antipodal identification between past- and future-directed null generators on the boundary, so that boundary data at antipodal points correspond to the same physical direction of propagation. In the entropy mechanics framework this pairing is treated as supplying an additional factor of π in the effective angular phase-space weight, leading to the combined factor $4\pi^2$. Other numerical choices would correspond to discarding the antipodal relation ($2\pi^2$) or double-counting independent angular sectors ($8\pi^2$), and are therefore not adopted here.

Finally, the vacuum-screening term $-1/(2\pi)$ is associated with a universal entropy deficit carried by virtual fluctuations along each angular direction of the holographic boundary. In the QTEP construction this deficit is normalized to one unit of information per full 2π angular range per light-cone sector, yielding a constant correction $-1/(2\pi)$ when expressed in the logarithmic units that enter α^{-1} . This assignment is a structural assumption of the entropy mechanics framework rather than a consequence of conventional QED, and is therefore kept explicit whenever the universal function is used.

The same orbit-based normalization of entropy deficits is used in Refs. [10, 11] to account for black hole evaporation entropy budgets and for the discrete energy hierarchy inferred from ATLAS and ALPHA-g data. The appearance of identical constants in the present $\alpha^{-1}(H)$ formula should therefore be understood as a reuse of previously fixed QTEP structure, not as a new numerical choice introduced for the purpose of matching electromagnetic data.

B Numerical Stability Analysis

Table 2 presents the response of α^{-1} to variations in fundamental constants:

Table 2: Numerical stability of universal formula under parameter perturbations.

| Parameter Change | α^{-1} | $\Delta\alpha^{-1}$ | Change (%) |
|------------------|---------------|---------------------|------------|
| $c + 0.1\%$ | 137.0341 | +0.0025 | +0.0018 |
| $c - 0.1\%$ | 137.0292 | -0.0025 | -0.0018 |
| $\hbar + 0.1\%$ | 137.0312 | -0.0005 | -0.0004 |
| $\hbar - 0.1\%$ | 137.0322 | +0.0005 | +0.0004 |
| $G + 0.1\%$ | 137.0312 | -0.0005 | -0.0004 |
| $G - 0.1\%$ | 137.0322 | +0.0005 | +0.0004 |
| $H_0 + 0.1\%$ | 137.0307 | -0.0010 | -0.0007 |
| $H_0 - 0.1\%$ | 137.0327 | +0.0010 | +0.0007 |

The formula exhibits smooth, continuous dependence on all parameters with no artificial tuning requirements. This stability supports the claim that the information-theoretic framework relies on structural constraints rather than delicate parameter tuning to match experimental values.

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