

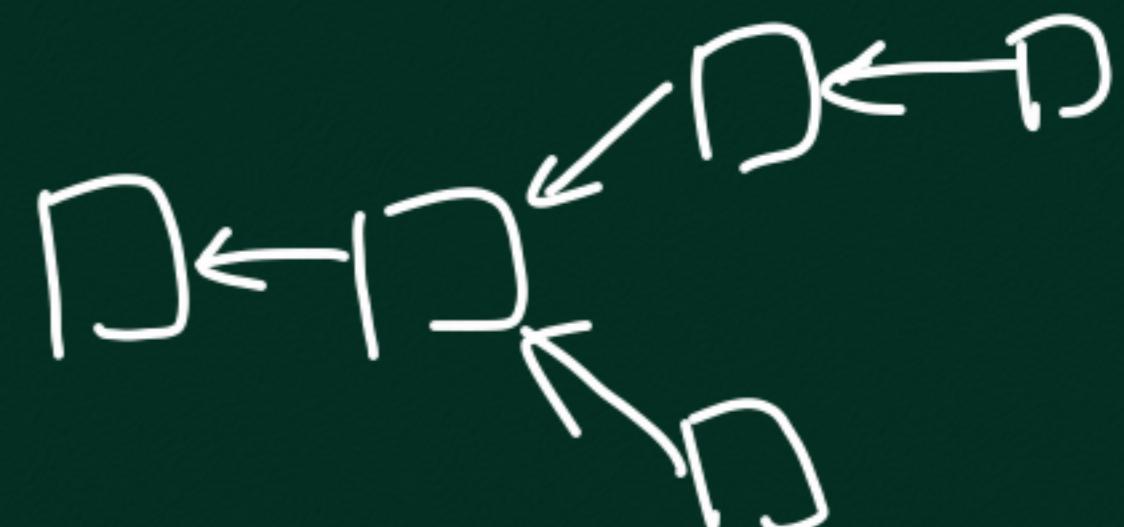
PoW, Naive PoS,
SLASHER

Eth2.0, RAFT
↓
2022, PBFT

Attendance

ALGORAND - 2017

Silvio Micali (Turing Award)



✓ Pure PoS, No Forks, Confirmation Time: 1 Minute,
Decentralized, Random Proposers, DOS Robustness
Atxns/sec ≈ 1000 >> Bitcoin's 7 txns/sec
Assume: ~85% of Stake Honest, Delay is few sec.

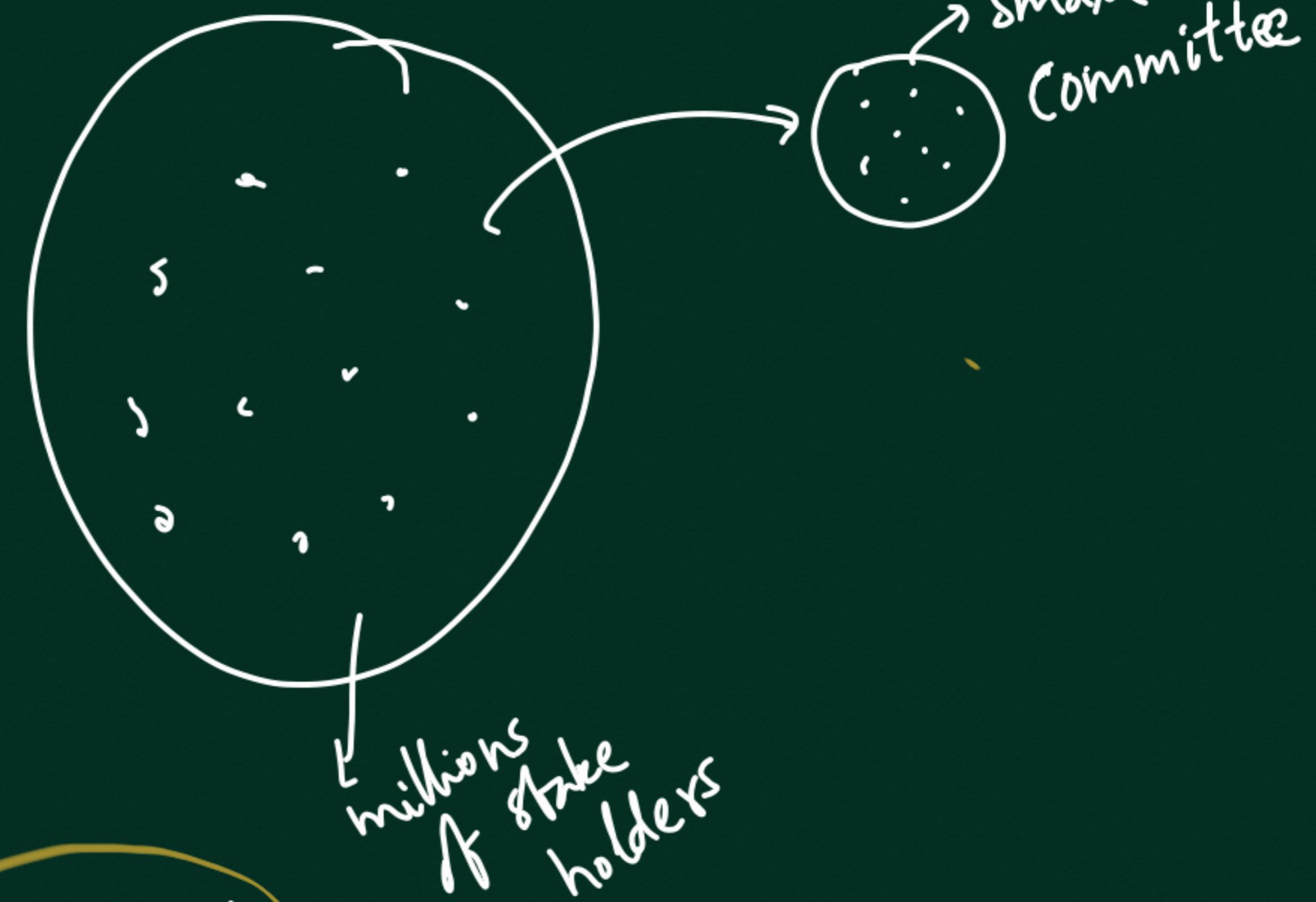
Stake and no forks

Stake & PBFT?
only N nodes

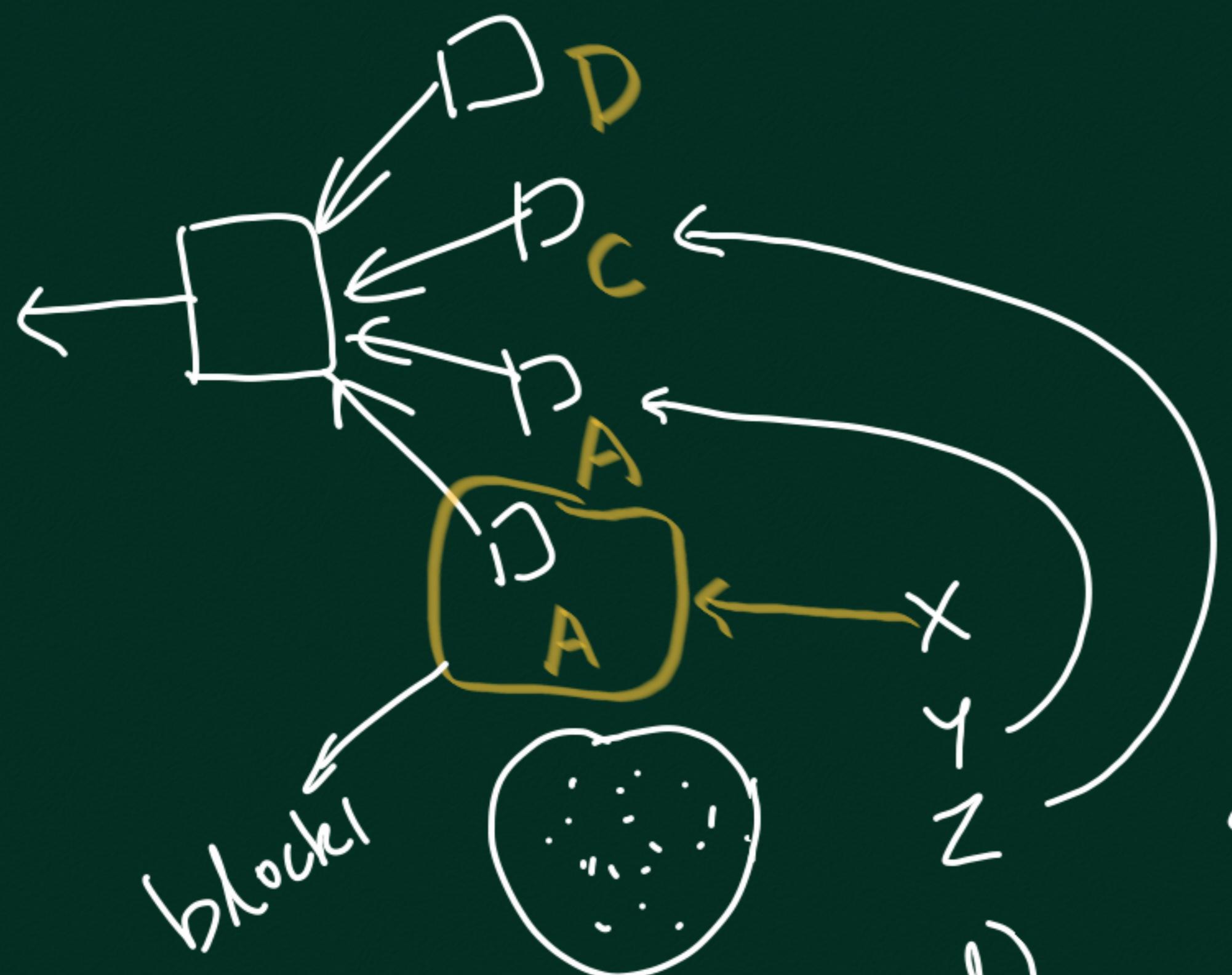
acct

bal(acct)

$$H\left(\text{acct} \parallel \dots \right) \leq \text{target} * \text{bal}(\text{acct})$$



High-Level Idea



Phase-0
(Blk Proposal)

Step-1
Phase-1
(Reduction)

Guarantee

X → block!

Y → empty blk

Z → block!

C → block!

D → empty

E → block!

~
Honest

All
Honest
either
block!
or
empty

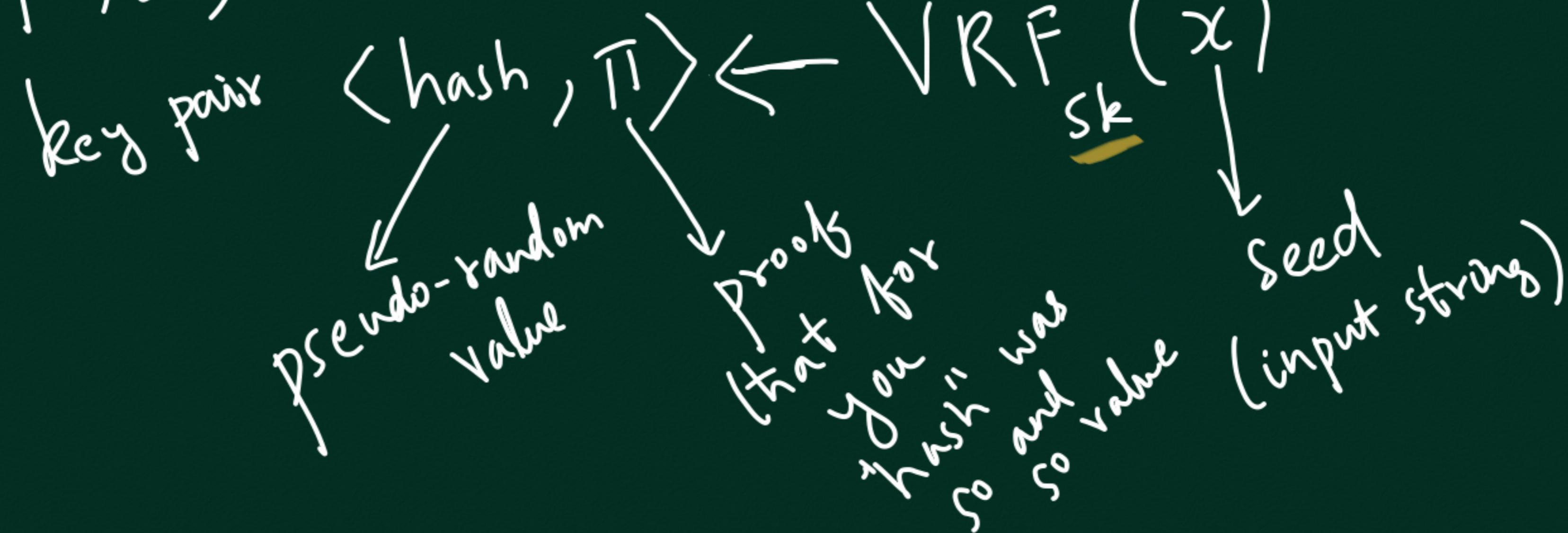
1 2 3
0 0 0 0 0
Phase-2
(Binary BAK)

How to randomly form a DoS-resistant Committee

Self-Select, prove later that selected

VRF: Verifiable random function (Tool used)

(pk, sk)



msg

$SIGN_{SK}(msg)$ $Verify(SIGN_{SK}(msg), msg$

Suppose:

hash = $H(SIGN_{SK}(x))^{pk}$

$\pi = SIGN_{SK}(x)$

} example VRF

SORTITION ($sk, seed, T, role, \omega, W$) \rightarrow total stake

Expect. size of committee

stake associated with (pk, sk)

changes from one step to another

SORTITION(sk , $seed$, T , $role$, w , W)

$\langle \text{hash}, \tau_1 \rangle \leftarrow \text{VRF}_{sk}(\text{Seed} \parallel \text{role}) \checkmark$

$$0 - \binom{\text{hashlen}}{2-1}$$

#times
elected to
committee
(#sub-users)

$$P \leftarrow \frac{T}{W}$$

$$j \leftarrow 0$$

while

$$\frac{\text{hash}}{2} \geq \sum_{k=0}^j B(k; w, P)$$

$j++$

unif $\xrightarrow{\text{convert}}$ Binomial

return $\langle \text{hash}, \tau_1, j \rangle$

Unit of stake



Selected or
not

T selected
on avg.

$$P = T/W$$

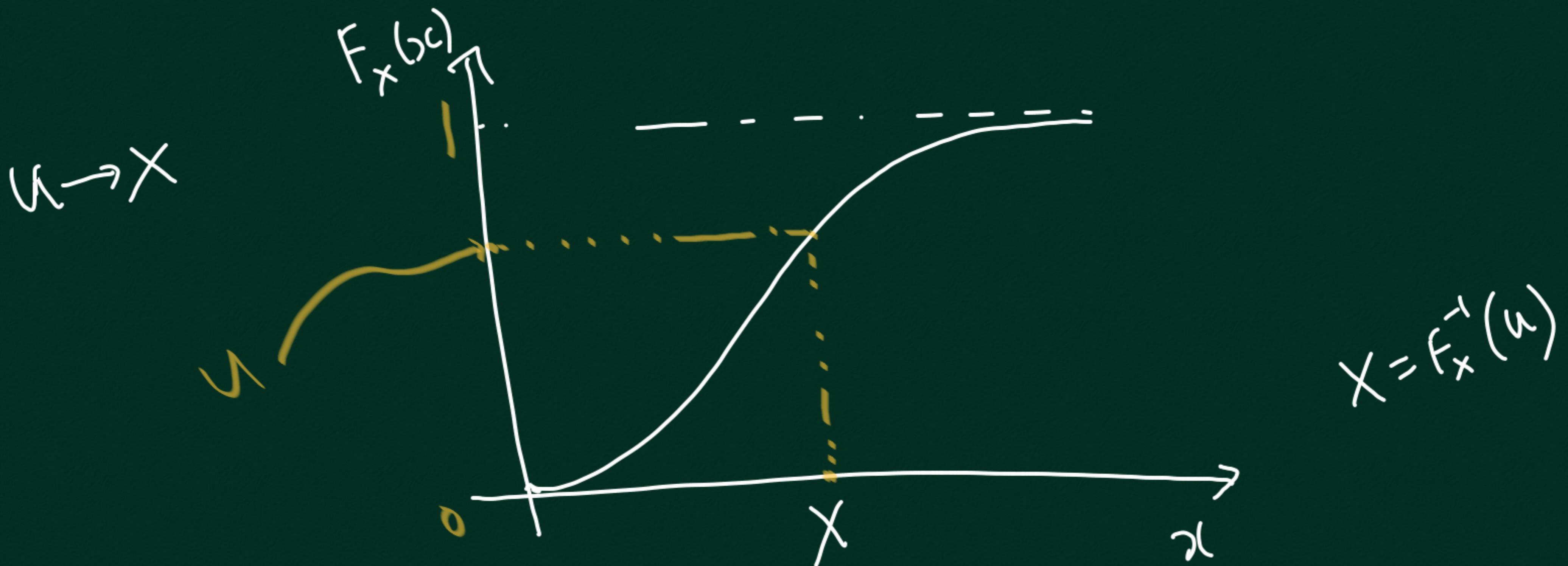
(pk, sk)

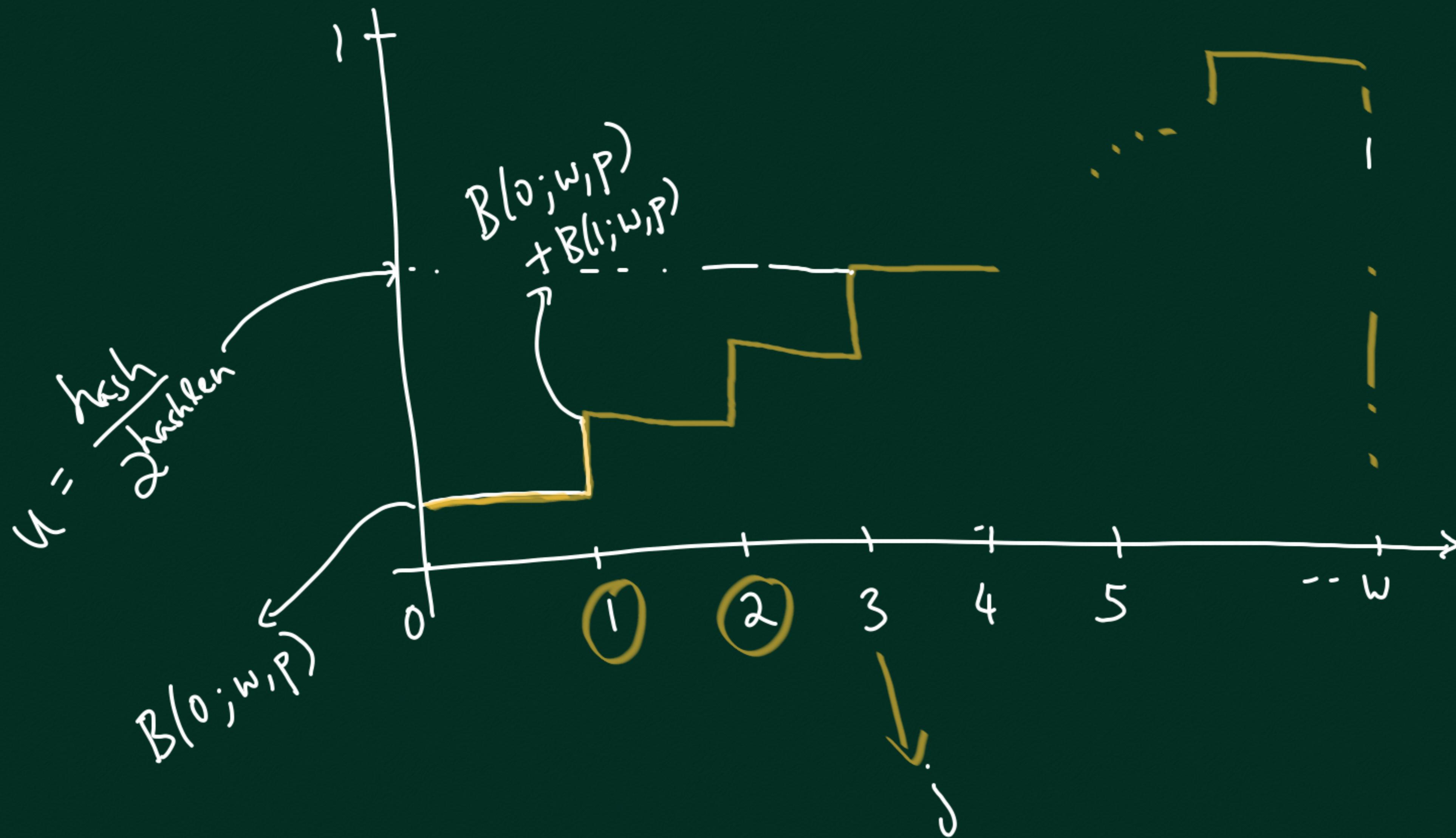


M selected
Distrib. of M? Binomial

$$B(k; \omega, p) = \text{Prob}(M=k) = \binom{\omega}{k} p^k (1-p)^{\omega-k}$$

Q. How to convert a unif r.v. $U \in [0, 1]$ to
any other r.v. X with c.d.f. $F_X(x)$





PHASE-0 (BLOCK PROPOSAL)

$$T_{\text{PROPOSER}} = 26$$

Suppose user has SOLUTION output $\langle \text{hash}, \pi, j \rangle$

$$\text{priority} = \max_{\text{of user}} \max_{i=1,2,\dots,j} H(\text{hash} \parallel i)$$

Ideally, user with highest priority is LEADER
whose block must be chosen

