Fully-Connected Neural Nets

In the previous homework you implemented a fully-connected two-layer neural network on CIFAR-10. The implementation was simple but not very modular since the loss and gradient were computed in a single monolithic function. This is manageable for a simple two-layer network, but would become impractical as we move to bigger models. Ideally we want to build networks using a more modular design so that we can implement different layer types in isolation and then snap them together into models with different architectures.

In this exercise we will implement fully-connected networks using a more modular approach. For each layer we will implement a forward and a backward function. The forward function will receive inputs, weights, and other parameters and will return both an output and a cache object storing data needed for the backward pass, like this:

```
def layer_forward(x, w):
    """ Receive inputs x and weights w """
# Do some computations ...
z = # ... some intermediate value
# Do some more computations ...
out = # the output

cache = (x, w, z, out) # Values we need to compute gradients
return out, cache
```

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
    """

Receive dout (derivative of loss with respect to outputs) and cache,
    and compute derivative with respect to inputs.
    """

# Unpack cache values
    x, w, z, out = cache

# Use values in cache to compute derivatives
    dx = # Derivative of loss with respect to x
    dw = # Derivative of loss with respect to w
return dx, dw
```

After implementing a bunch of layers this way, we will be able to easily combine them to build classifiers with different architectures.

In addition to implementing fully-connected networks of arbitrary depth, we will also explore different update rules for optimization, and introduce Dropout as a regularizer and Batch/Layer Normalization as a tool to more efficiently optimize deep networks.

```
In [31]:
         # As usual, a bit of setup
         from future import print function
         import time
         import numpy as np
         import matplotlib.pyplot as plt
         from cs682.classifiers.fc_net import *
         from cs682.data utils import get CIFAR10 data
         from cs682.gradient check import eval numerical gradient, eval numerical gradient array
         from cs682.solver import Solver
         %matplotlib inline
         plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
         plt.rcParams['image.interpolation'] = 'nearest'
         plt.rcParams['image.cmap'] = 'gray'
         # for auto-reloading external modules
         # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
         %load ext autoreload
         %autoreload 2
         def rel error(x, y):
          """ returns relative error """
          return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
         The autoreload extension is already loaded. To reload it, use:
```

%reload ext autoreload

```
In [61]:
           #Load the (preprocessed) CIFAR10 data.
           data = get CIFAR10 data()
           for k, v in list(data.items()):
             print(('%s: ' % k, v.shape))
           X train = data['X train']
           y train = data['y train']
           X \text{ val} = \text{data}['X \text{ val'}]
           y val = data['y val']
           X \text{ test} = \text{data}['X \text{ test'}]
           y test = data['y test']
```

```
('X train: ', (49000, 3, 32, 32))
('y_train: ', (49000,))
('X val: ', (1000, 3, 32, 32))
('y val: ', (1000,))
('X test: ', (1000, 3, 32, 32))
('y_test: ', (1000,))
```

Affine layer: foward

Open the file cs682/layers.py and implement the affine forward function.

Once you are done you can test your implementaion by running the following:

```
In [33]:
         # Test the affine forward function
         num inputs = 2
         input shape = (4, 5, 6)
         output dim = 3
         input size = num inputs * np.prod(input shape)
         weight size = output dim * np.prod(input shape)
         x = np.linspace(-0.1, 0.5, num=input size).reshape(num inputs, *input shape)
         w = np.linspace(-0.2, 0.3, num=weight size).reshape(np.prod(input shape), output dim)
         b = np.linspace(-0.3, 0.1, num=output dim)
         out, = affine forward(x, w, b)
         correct out = np.array([[1.49834967, 1.70660132, 1.91485297],
                        [ 3.25553199, 3.5141327, 3.77273342]])
         # Compare your output with ours. The error should be around e-9 or less.
         print('Testing affine forward function:')
         print('difference: ', rel error(out, correct out))
```

Testing affine_forward function: difference: 9.769847728806635e-10

Affine layer: backward

Now implement the affine backward function and test your implementation using numeric gradient checking.

```
In [34]: # Test the affine backward function
         np.random.seed(231)
         x = np.random.randn(10, 2, 3)
         w = np.random.randn(6, 5)
         b = np.random.randn(5)
         dout = np.random.randn(10, 5)
         dx num = eval numerical gradient array(lambda x: affine forward(x, w, b)[0], x, dout)
         dw num = eval numerical gradient array(lambda w: affine forward(x, w, b)[0], w, dout)
         db num = eval numerical gradient array(lambda b: affine forward(x, w, b)[0], b, dout)
         , cache = affine forward(x, w, b)
         dx, dw, db = affine backward(dout, cache)
         # The error should be around e-10 or less
         print('Testing affine backward function:')
         print('dx error: ', rel error(dx num, dx))
         print('dw error: ', rel error(dw num, dw))
         print('db error: ', rel error(db num, db))
```

Testing affine_backward function: dx error: 5.399100368651805e-11 dw error: 9.904211865398145e-11 db error: 2.4122867568119087e-11

ReLU activation: forward

Implement the forward pass for the ReLU activation function in the relu_forward function and test your implementation using the following:

Testing relu_forward function: difference: 4.999999798022158e-08

ReLU activation: backward

Now implement the backward pass for the ReLU activation function in the relu_backward function and test your implementation using numeric gradient checking:

```
In [36]: np.random.seed(231)
    x = np.random.randn(10, 10)
    dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)

_, cache = relu_forward(x)
    dx = relu_backward(dout, cache)

# The error should be on the order of e-12
    print('Testing relu_backward function:')
    print('dx error: ', rel_error(dx_num, dx))
```

Testing relu_backward function: dx error: 3.2756349136310288e-12

Inline Question 1:

We've only asked you to implement ReLU, but there are a number of different activation functions that one could use in neural networks, each with its pros and cons. In particular, an issue commonly seen with activation functions is getting zero (or close to zero) gradient flow during backpropagation. Which of the following activation functions have this problem? If you consider these functions in the one dimensional case, what types of input would lead to this behaviour?

- 1. Sigmoid
- 2. ReLU
- 3. Leaky ReLU

Answer:

Sigmoid and ReLU will have this problem. For sigmoid, the inputs that are small. For ReLU, it is inputs that are negative.

"Sandwich" layers

There are some common patterns of layers that are frequently used in neural nets. For example, affine layers are frequently followed by a ReLU nonlinearity. To make these common patterns easy, we define several convenience layers in the file $cs682/layer_utils.py$.

For now take a look at the affine_relu_forward and affine_relu_backward functions, and run the following to numerically gradient check the backward pass:

```
In [37]:
        from cs682.layer_utils import affine relu forward, affine relu backward
         np.random.seed(231)
         x = np.random.randn(2, 3, 4)
         w = np.random.randn(12, 10)
         b = np.random.randn(10)
         dout = np.random.randn(2, 10)
         out, cache = affine relu forward(x, w, b)
         dx, dw, db = affine relu backward(dout, cache)
         dx num = eval numerical gradient array(lambda x: affine relu forward(x, w, b)[0], x, dout)
         dw num = eval numerical gradient array(lambda w: affine relu forward(x, w, b)[0], w, dout)
         db num = eval numerical gradient array(lambda b: affine relu forward(x, w, b)[0], b, dout)
         # Relative error should be around e-10 or less
         print('Testing affine relu forward and affine relu backward:')
         print('dx error: ', rel error(dx num, dx))
         print('dw error: ', rel error(dw num, dw))
         print('db error: ', rel error(db num, db))
```

Testing affine_relu_forward and affine_relu_backward:

dx error: 6.750562121603446e-11 dw error: 8.162015570444288e-11 db error: 7.826724021458994e-12

Loss layers: Softmax and SVM

You implemented these loss functions in the last assignment, so we'll give them to you for free here. You should still make sure you understand how they work by looking at the implementations in cs682/layers.py.

You can make sure that the implementations are correct by running the following:

```
In [38]:
         np.random.seed(231)
         num classes, num inputs = 10, 50
         x = 0.001 * np.random.randn(num inputs, num classes)
         y = np.random.randint(num classes, size=num inputs)
         dx num = eval numerical gradient(lambda x: svm loss(x, y)[0], x, verbose=False)
         loss, dx = svm loss(x, y)
         # Test sym loss function. Loss should be around 9 and dx error should be around the order of e-9
         print('Testing svm loss:')
         print('loss: ', loss)
         print('dx error: ', rel error(dx num, dx))
         dx num = eval numerical gradient(lambda x: softmax loss(x, y)[0], x, verbose=False)
         loss, dx = softmax loss(x, y)
         # Test softmax loss function. Loss should be close to 2.3 and dx error should be around e-8
         print('\nTesting softmax loss:')
         print('loss: ', loss)
         print('dx error: ', rel error(dx num, dx))
```

Testing svm loss:

loss: 8.999602749096233

dx error: 1.4021566006651672e-09

Testing softmax_loss: loss: 2.302545844500738

dx error: 9.384673161989355e-09

Two-layer network

In the previous assignment you implemented a two-layer neural network in a single monolithic class. Now that you have implemented modular versions of the necessary layers, you will reimplement the two layer network using these modular implementations.

Open the file cs682/classifiers/fc_net.py and complete the implementation of the TwoLayerNet class. This class will serve as a model for the other networks you will implement in this assignment, so read through it to make sure you understand the API. You can run the cell below to test your implementation.

```
In [39]: | np.random.seed(231)
         N, D, H, C = 3, 5, 50, 7
         X = np.random.randn(N, D)
         y = np.random.randint(C, size=N)
         std = 1e-3
         model = TwoLayerNet(input dim=D, hidden dim=H, num classes=C, weight scale=std)
         print('Testing initialization ... ')
         W1 \text{ std} = abs(model.params['W1'].std() - std)
         b1 = model.params['b1']
         W2 \text{ std} = abs(model.params['W2'].std() - std)
         b2 = model.params['b2']
         assert W1 std < std / 10, 'First layer weights do not seem right'
         assert np.all(b1 == 0), 'First layer biases do not seem right'
         assert W2 std < std / 10, 'Second layer weights do not seem right'
         assert np.all(b2 == 0), 'Second layer biases do not seem right'
         print('Testing test-time forward pass ... ')
         model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
         model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
         model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
         model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
         X = \text{np.linspace}(-5.5, 4.5, \text{num}=N*D).\text{reshape}(D, N).T
         scores = model.loss(X)
         correct scores = np.asarray(
          [[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.57198434, 15.33206765, 16.09215096],
           [12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.49994135, 16.18839143],
           [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.66781506, 16.2846319]])
         scores diff = np.abs(scores - correct scores).sum()
         assert scores diff < 1e-6, 'Problem with test-time forward pass'
         print('Testing training loss (no regularization)')
         y = np.asarray([0, 5, 1])
         loss, grads = model.loss(X, y)
         correct loss = 3.4702243556
         assert abs(loss - correct loss) < 1e-10, 'Problem with training-time loss'
         model.reg = 1.0
         loss, grads = model.loss(X, y)
         correct loss = 26.5948426952
         assert abs(loss - correct loss) < 1e-10, 'Problem with regularization loss'
         # Errors should be around e-7 or less
         for reg in [0.0, 0.7]:
          print('Running numeric gradient check with reg = ', reg)
          model.reg = reg
          loss, grads = model.loss(X, y)
          for name in sorted(grads):
            f = lambda : model.loss(X, y)[0]
            grad num = eval numerical gradient(f, model.params[name], verbose=False)
            print('%s relative error: %.2e' % (name, rel error(grad num, grads[name])))
```

```
Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.52e-08
W2 relative error: 3.48e-10
b1 relative error: 6.55e-09
b2 relative error: 4.33e-10
Running numeric gradient check with reg = 0.7
W1 relative error: 8.18e-07
W2 relative error: 7.98e-08
b1 relative error: 1.09e-09
b2 relative error: 7.76e-10
```

Solver

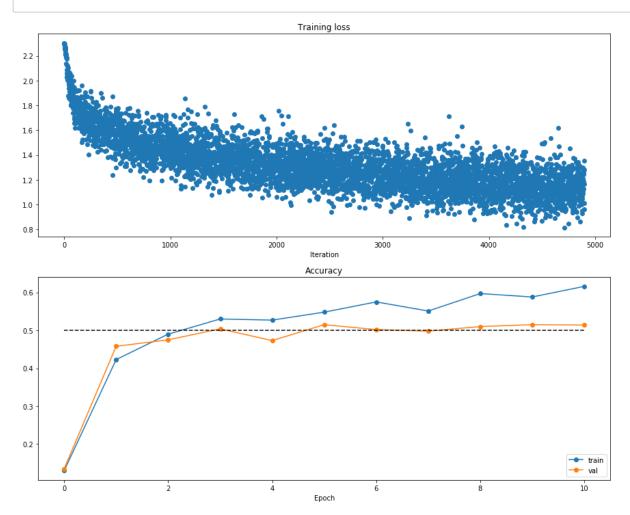
In the previous assignment, the logic for training models was coupled to the models themselves. Following a more modular design, for this assignment we have split the logic for training models into a separate class.

Open the file cs682/solver.py and read through it to familiarize yourself with the API. After doing so, use a Solver instance to train a TwoLayerNet that achieves at least 50% accuracy on the validation set.

```
In [58]:
     model = TwoLayerNet()
     solver = None
     # TODO: Use a Solver instance to train a TwoLayerNet that achieves at least #
     # 50% accuracy on the validation set.
     data = {
       'X train': X_train,
       'y train': y train,
       'X_val': X val,
       'y val': y val,
     solver = Solver(model, data,
          update rule='sgd',
          optim_config={
           'learning rate': 1e-3,
          verbose = False,
          lr decay=0.95,
          num epochs=10, batch size=100,
          print every=100)
     solver.train()
     END OF YOUR CODE
```

In [59]: #Run this cell to visualize training loss and train / val accuracy

plt.subplot(2, 1, 1)
 plt.plot(solver.loss_history, 'o')
 plt.subplot(2, 1, 2)
 plt.subplot(2, 1, 2)
 plt.title('Accuracy')
 plt.plot(solver.train_acc_history, '-o', label='train')
 plt.plot(solver.val_acc_history, '-o', label='val')
 plt.plot([0.5] * len(solver.val_acc_history), 'k--')
 plt.legend(loc='lower right')
 plt.gcf().set_size_inches(15, 12)
 plt.show()



Multilayer network

Next you will implement a fully-connected network with an arbitrary number of hidden layers.

Read through the FullyConnectedNet class in the file cs682/classifiers/fc net.py.

Implement the initialization, the forward pass, and the backward pass. For the moment don't worry about implementing dropout or batch/layer normalization; we will add those features soon.

Initial loss and gradient check

As a sanity check, run the following to check the initial loss and to gradient check the network both with and without regularization. Do the initial losses seem reasonable?

For gradient checking, you should expect to see errors around 1e-7 or less.

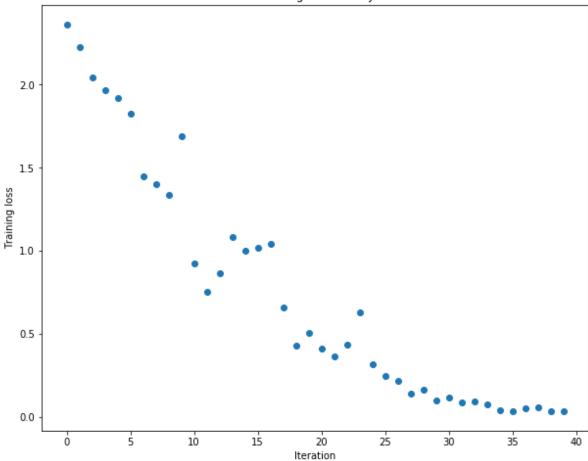
```
In [43]:
        np.random.seed(231)
         N, D, H1, H2, C = 2, 15, 20, 30, 10
         X = np.random.randn(N, D)
         y = np.random.randint(C, size=(N,))
         for reg in [0, 3.14]:
          print('Running check with reg = ', reg)
          model = FullyConnectedNet([H1, H2], input dim=D, num classes=C,
                          reg=reg, weight scale=5e-2, dtype=np.float64)
          loss, grads = model.loss(X, y)
          print('Initial loss: ', loss)
          # Most of the errors should be on the order of e-7 or smaller.
          #NOTE: It is fine however to see an error for W2 on the order of e-5
          # for the check when reg = 0.0
          for name in sorted(grads):
           f = lambda : model.loss(X, y)[0]
           grad num = eval numerical gradient(f, model.params[name], verbose=False, h=1e-5)
           print('%s relative error: %.2e' % (name, rel error(grad num, grads[name])))
```

Running check with reg = 0Initial loss: 2.3004790897684924 W1 relative error: 1.48e-07 W2 relative error: 2.21e-05 W3 relative error: 3.53e-07 b1 relative error: 5.38e-09 b2 relative error: 2.09e-09 b3 relative error: 5.80e-11 Running check with reg = 3.14Initial loss: 7.052114776533016 W1 relative error: 7.36e-09 W2 relative error: 6.87e-08 W3 relative error: 3.48e-08 b1 relative error: 1.48e-08 b2 relative error: 1.72e-09 b3 relative error: 1.80e-10

As another sanity check, make sure you can overfit a small dataset of 50 images. First we will try a three-layer network with 100 units in each hidden layer. In the following cell, tweak the learning rate and initialization scale to overfit and achieve 100% training accuracy within 20 epochs.

TODO: Use a three-layer Net to overfit 50 training examples by In [45]: # tweaking just the learning rate and initialization scale. num train = 50 $small data = {$ 'X_train': data['X_train'][:num_train], 'y_train': data['y_train'][:num_train], 'X val': data['X val'], 'y_val': data['y_val'], weight scale = 1e-2learning rate = 9e-3model = FullyConnectedNet([100, 100], weight scale=weight scale, dtype=np.float64) solver = Solver(model, small data, print every=10, num epochs=20, batch size=25, update rule='sgd', optim config={ 'learning rate': learning_rate, verbose = False) solver.train() plt.plot(solver.loss history, 'o') plt.title('Training loss history') plt.xlabel('Iteration') plt.ylabel('Training loss') plt.show()

Training loss history

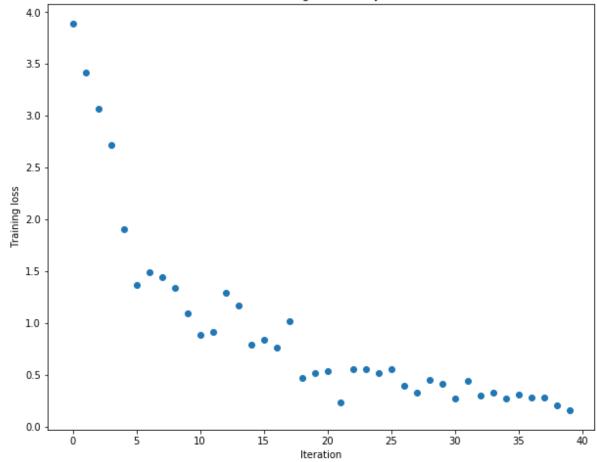


Now try to use a five-layer network with 100 units on each layer to overfit 50 training examples. Again you will have to adjust the learning rate and weight initialization, but you should be able to achieve 100% training accuracy within 20 epochs.

In [49]: # TODO: Use a five-layer Net to overfit 50 training examples by # tweaking just the learning rate and initialization scale. num train = 50 $small data = {$ 'X_train': data['X_train'][:num_train], 'y_train': data['y_train'][:num_train], 'X val': data['X val'], 'y_val': data['y_val'], $learning_rate = 2e-3$ weight scale = 5e-2model = FullyConnectedNet([100, 100, 100, 100], weight scale=weight scale, dtype=np.float64) solver = Solver(model, small data, print every=10, num epochs=20, batch size=25, update rule='sgd', optim config={ 'learning rate': learning rate, verbose = True) solver.train() plt.plot(solver.loss history, 'o') plt.title('Training loss history') plt.xlabel('Iteration') plt.ylabel('Training loss') plt.show()

(Iteration 1 / 40) loss: 3.892097 (Epoch 0 / 20) train acc: 0.260000; val acc: 0.140000 (Epoch 1 / 20) train acc: 0.300000; val acc: 0.118000 (Epoch 2 / 20) train acc: 0.400000; val acc: 0.105000 (Epoch 3 / 20) train acc: 0.500000; val acc: 0.122000 (Epoch 4 / 20) train acc: 0.560000; val acc: 0.129000 (Epoch 5 / 20) train acc: 0.660000; val acc: 0.126000 (Iteration 11 / 40) loss: 0.886108 (Epoch 6 / 20) train acc: 0.660000; val acc: 0.125000 (Epoch 7 / 20) train acc: 0.780000; val acc: 0.125000 (Epoch 8 / 20) train acc: 0.820000; val acc: 0.120000 (Epoch 9 / 20) train acc: 0.920000; val acc: 0.147000 (Epoch 10 / 20) train acc: 0.920000; val acc: 0.126000 (Iteration 21 / 40) loss: 0.538654 (Epoch 11 / 20) train acc: 0.940000; val acc: 0.128000 (Epoch 12 / 20) train acc: 0.940000; val acc: 0.131000 (Epoch 13 / 20) train acc: 0.960000; val acc: 0.142000 (Epoch 14 / 20) train acc: 0.960000; val acc: 0.136000 (Epoch 15 / 20) train acc: 0.960000; val acc: 0.137000 (Iteration 31 / 40) loss: 0.272727 (Epoch 16 / 20) train acc: 0.980000; val acc: 0.141000 (Epoch 17 / 20) train acc: 0.980000; val acc: 0.140000 (Epoch 18 / 20) train acc: 0.980000; val acc: 0.148000 (Epoch 19 / 20) train acc: 1.000000; val acc: 0.150000 (Epoch 20 / 20) train acc: 0.980000; val acc: 0.149000

Training loss history



Inline Question 2:

Did you notice anything about the comparative difficulty of training the three-layer net vs training the five layer net? In particular, based on your experience, which network seemed more sensitive to the initialization scale? Why do you think that is the case?

Answer:

The five layer neural network needed to be initalize with smaller weights. I think this is because there are more layers and more backpropagation happening, and larger weights may cause exploding gradients.

Update rules

So far we have used vanilla stochastic gradient descent (SGD) as our update rule. More sophisticated update rules can make it easier to train deep networks. We will implement a few of the most commonly used update rules and compare them to vanilla SGD.

SGD+Momentum

Stochastic gradient descent with momentum is a widely used update rule that tends to make deep networks converge faster than vanilla stochastic gradient descent. See the Momentum Update section at https://compsci682-fa18.github.io/notes/neural-networks-3/#sgd (https://compsci682-fa18.github.io/notes/neural-networks-3/#sgd) for more information.

Open the file cs682/optim.py and read the documentation at the top of the file to make sure you understand the API. Implement the SGD+momentum update rule in the function $sgd_momentum$ and run the following to check your implementation. You should see errors less than e-8.

```
In [50]:
        from cs682.optim import sgd momentum
        N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
         dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
         v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
         config = {'learning rate': 1e-3, 'velocity': v}
         next w, = sgd momentum(w, dw, config=config)
         expected next w = np.asarray([
                     0.20738947, 0.27417895, 0.34096842, 0.40775789],
         [ 0.1406,
         [0.47454737, 0.54133684, 0.60812632, 0.67491579, 0.74170526],
         [0.80849474, 0.87528421, 0.94207368, 1.00886316, 1.07565263],
         [1.14244211, 1.20923158, 1.27602105, 1.34281053, 1.4096 ]])
         expected velocity = np.asarray([
                     0.55475789, 0.56891579, 0.58307368, 0.59723158],
         [ 0.5406,
         [0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
          [0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
         [0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096]])
         # Should see relative errors around e-8 or less
         print('next w error: ', rel error(next w, expected next w))
         print('velocity error: ', rel error(expected velocity, config['velocity']))
```

next_w error: 8.882347033505819e-09 velocity error: 4.269287743278663e-09

Once you have done so, run the following to train a six-layer network with both SGD and SGD+momentum. You should see the SGD+momentum update rule converge faster.

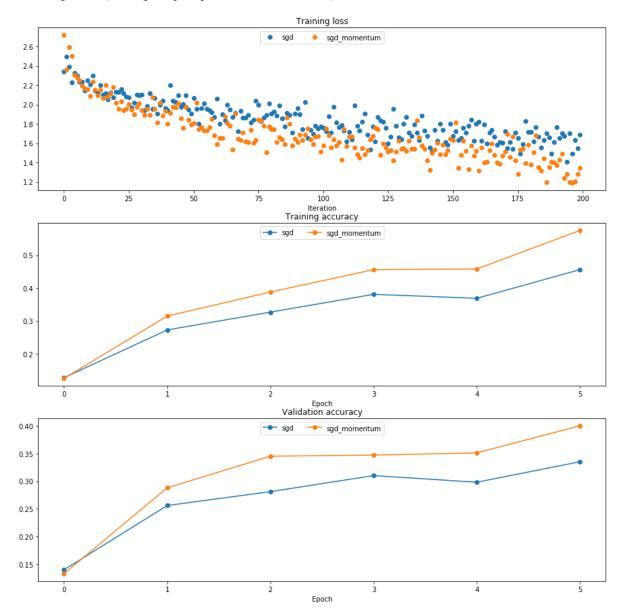
```
In [52]:
         num train = 4000
          small data = {
           'X train': data['X train'][:num train],
           'y train': data['y train'][:num train],
           'X val': data['X val'],
           'y val': data['y val'],
          solvers = \{\}
          for update rule in ['sgd', 'sgd momentum']:
           print('running with ', update rule)
           model = FullyConnectedNet([100, 100, 100, 100, 100], weight scale=5e-2)
           solver = Solver(model, small data,
                     num epochs=5, batch size=100,
                     update rule=update rule,
                     optim config={
                      'learning rate': 1e-2,
                     verbose=False)
           solvers[update rule] = solver
           solver.train()
           print()
          plt.subplot(3, 1, 1)
          plt.title('Training loss')
          plt.xlabel('Iteration')
          plt.subplot(3, 1, 2)
          plt.title('Training accuracy')
          plt.xlabel('Epoch')
          plt.subplot(3, 1, 3)
          plt.title('Validation accuracy')
          plt.xlabel('Epoch')
          for update rule, solver in list(solvers.items()):
           plt.subplot(3, 1, 1)
           plt.plot(solver.loss history, 'o', label=update rule)
           plt.subplot(3, 1, 2)
           plt.plot(solver.train acc history, '-o', label=update rule)
           plt.subplot(3, 1, 3)
           plt.plot(solver.val acc history, '-o', label=update rule)
          for i in [1, 2, 3]:
           plt.subplot(3, 1, i)
           plt.legend(loc='upper center', ncol=4)
          plt.gcf().set size inches(15, 15)
          plt.show()
```

running with sgd

running with sgd momentum

C:\Users\kucharskib\AppData\Roaming\Python\Python36\site-packages\matplotlib\cbook\deprecation.py: 106: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Mea nwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

warnings.warn(message, mplDeprecation, stacklevel=1)



RMSProp and Adam

RMSProp [1] and Adam [2] are update rules that set per-parameter learning rates by using a running average of the second moments of gradients.

In the file cs682/optim.py, implement the RMSProp update rule in the rmsprop function and implement the Adam update rule in the adam function, and check your implementations using the tests below.

NOTE: Please implement the *complete* Adam update rule (with the bias correction mechanism), not the first simplified version mentioned in the course notes.

[1] Tijmen Tieleman and Geoffrey Hinton. "Lecture 6.5-rmsprop: Divide the gradient by a running average of its recent magnitude." COURSERA: Neural Networks for Machine Learning 4 (2012).

[2] Diederik Kingma and Jimmy Ba, "Adam: A Method for Stochastic Optimization", ICLR 2015.

```
In [53]:
         # Test RMSProp implementation
         from cs682.optim import rmsprop
        N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
         dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
         cache = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
         config = {'learning rate': 1e-2, 'cache': cache}
         next w, = rmsprop(w, dw, config=config)
         expected next w = np.asarray([
         [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
          [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
         [0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
         [0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
         expected cache = np.asarray([
         [ 0.5976,
                     0.6126277, 0.6277108, 0.64284931, 0.65804321]
          [0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
         [0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936],
         [0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926]
         # You should see relative errors around e-7 or less
         print('next w error: ', rel error(expected next w, next w))
         print('cache error: ', rel error(expected cache, config['cache']))
```

next_w error: 9.524687511038133e-08 cache error: 2.6477955807156126e-09

In [54]: # Test Adam implementation from cs682.optim import adam N, D = 4, 5w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)m = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)v = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)config = {'learning rate': 1e-2, 'm': m, 'v': v, 't': 5} next w, = adam(w, dw, config=config) expected next w = np.asarray([[-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],[-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],[0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],[0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])expected v = np.asarray([0.68908382, 0.67851319, 0.66794809, 0.65738853,], [0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385,][0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,][0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966,]])expected m = np.asarray([0.49947368, 0.51894737, 0.53842105, 0.55789474], [0.48,[0.57736842, 0.59684211, 0.61631579, 0.63578947, 0.65526316],[0.67473684, 0.69421053, 0.71368421, 0.73315789, 0.75263158],[0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85]# You should see relative errors around e-7 or less print('next w error: ', rel error(expected next w, next w)) print('v error: ', rel error(expected v, config['v'])) print('m error: ', rel error(expected m, config['m']))

next_w error: 1.1395691798535431e-07 v error: 4.208314038113071e-09 m error: 4.214963193114416e-09

Once you have debugged your RMSProp and Adam implementations, run the following to train a pair of deep networks using these new update rules:

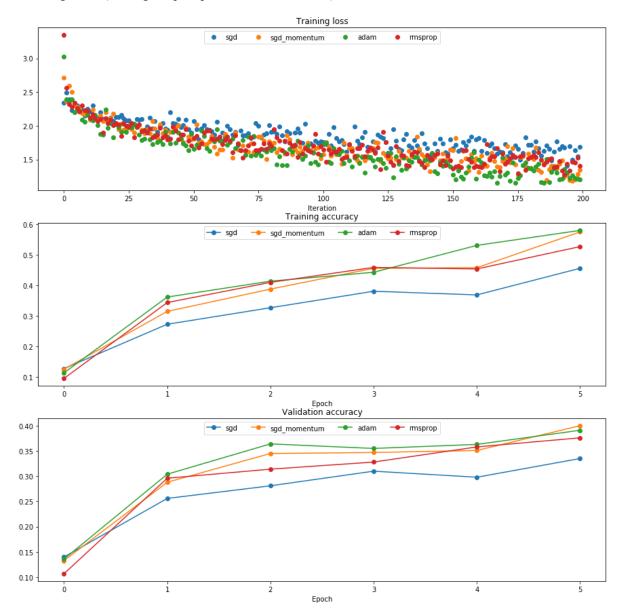
```
In [55]:
         learning rates = {'rmsprop': 1e-4, 'adam': 1e-3}
          for update rule in ['adam', 'rmsprop']:
           print('running with ', update rule)
           model = FullyConnectedNet([100, 100, 100, 100, 100], weight scale=5e-2)
           solver = Solver(model, small data,
                     num epochs=5, batch size=100,
                     update rule=update rule,
                     optim config={
                      'learning rate': learning rates[update rule]
                     verbose=False)
           solvers[update rule] = solver
           solver.train()
           print()
          plt.subplot(3, 1, 1)
          plt.title('Training loss')
          plt.xlabel('Iteration')
          plt.subplot(3, 1, 2)
          plt.title('Training accuracy')
         plt.xlabel('Epoch')
          plt.subplot(3, 1, 3)
          plt.title('Validation accuracy')
          plt.xlabel('Epoch')
          for update rule, solver in list(solvers.items()):
           plt.subplot(3, 1, 1)
           plt.plot(solver.loss history, 'o', label=update rule)
           plt.subplot(3, 1, 2)
           plt.plot(solver.train acc history, '-o', label=update rule)
           plt.subplot(3, 1, 3)
           plt.plot(solver.val acc history, '-o', label=update rule)
          for i in [1, 2, 3]:
           plt.subplot(3, 1, i)
          plt.legend(loc='upper center', ncol=4)
          plt.gcf().set size inches(15, 15)
          plt.show()
```

running with adam

running with rmsprop

C:\Users\kucharskib\AppData\Roaming\Python\Python36\site-packages\matplotlib\cbook\deprecation.py: 106: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Mea nwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

warnings.warn(message, mplDeprecation, stacklevel=1)



Inline Question 3:

AdaGrad, like Adam, is a per-parameter optimization method that uses the following update rule:

```
cache += dw**2
w += - learning rate * dw / (np.sqrt(cache) + eps)
```

John notices that when he was training a network with AdaGrad that the updates became very small, and that his network was learning slowly. Using your knowledge of the AdaGrad update rule, why do you think the updates would become very small? Would Adam have the same issue?

Answer:

The updates become very small because of the squared dw term. Since the dw is squared, the cache will also be positive, which will learn to the divison of a larger and larger number over time. This leads to smaller updates over time.

Train a good model!

Train the best fully-connected model that you can on CIFAR-10, storing your best model in the best_model variable. We require you to get at least 50% accuracy on the validation set using a fully-connected net.

If you are careful it should be possible to get accuracies above 55%, but we don't require it for this part and won't assign extra credit for doing so. Later in the assignment we will ask you to train the best convolutional network that you can on CIFAR-10, and we would prefer that you spend your effort working on convolutional nets rather than fully-connected nets.

You might find it useful to complete the BatchNormalization.ipynb and Dropout.ipynb notebooks before completing this part, since those techniques can help you train powerful models.

```
In [29]:
     best model = None
     # TODO: Train the best FullyConnectedNet that you can on CIFAR-10. You might #
     # find batch/layer normalization and dropout useful. Store your best model in #
     # the best model variable.
     weight scale = 5e-2
     learning rate = 1e-3
     model = FullyConnectedNet([200, 100, 50, 25],normalization='batchnorm', weight scale=weight scale, dty
     pe=np.float64)
     solver = Solver(model, data,
           print every=100,
           num epochs=5,
           batch size=64,
           update rule='adam',
           optim config={
            'learning rate': learning rate,
           verbose = False
     solver.train()
     best model = model
     END OF YOUR CODE
```

Test your model!

Run your best model on the validation and test sets. You should achieve above 50% accuracy on the validation set.

```
In [62]: y_test_pred = np.argmax(best_model.loss(data['X_test']), axis=1)
y_val_pred = np.argmax(best_model.loss(data['X_val']), axis=1)
print('Validation set accuracy: ', (y_val_pred == data['y_val']).mean())
print('Test set accuracy: ', (y_test_pred == data['y_test']).mean())
```

Validation set accuracy: 0.523 Test set accuracy: 0.488