

DMath_U1_bf

1.5

a.

A	B	C	$A \oplus B$	$(A \oplus B) \oplus C$
0	0	0	0	0
0	0	1	0	1
0	1	0	1	1
0	1	1	1	0
1	0	0	1	1
1	0	1	1	0
1	1	0	0	0
1	1	1	0	1

A	B	C	$B \oplus C$	$A \oplus (B \oplus C)$
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	0	1

$$(A \oplus B) \oplus C \equiv A \oplus (B \oplus C)$$

q.e.d.

b.

A	B	$\neg A$	$\neg B$	$\neg A \wedge \neg B$	$\neg(A \oplus B)$
0	0	1	1	1	1
0	1	1	0	0	0
1	0	0	1	0	0
1	1	0	0	1	1

$$\neg A \wedge \neg B \equiv \neg(A \oplus B)$$

q.e.d.

c.

truth table of F:

A	B	C	F
0	0	0	0

A	B	C	F
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

truth table of G:

A	B	C	$A \wedge B$	$(A \wedge B) \wedge C$	$(A \wedge B) \vee ((A \wedge B) \wedge C)$	$A \wedge (A \wedge B) \vee ((A \wedge B) \wedge C)$
0	0	0	0	0	0	0
0	0	1	0	1	1	1
0	1	0	1	1	0	0
0	1	1	1	0	1	1
1	0	0	1	1	0	1
1	0	1	1	0	1	0
1	1	0	0	0	0	1
1	1	1	0	1	1	0

$F \equiv A \wedge (A \wedge B) \vee ((A \wedge B) \wedge C)$
q.e.d.
