## Practical Problem for the Midterm Exam -Fall 2023

## FE-570

## 23 October 2023

## **Problem 11.** (20pt)

The data for this problem is contained in the file taqdata\_BTCUSD.RData. This is a trade-and-quote file giving the trade price, size, and the quotes at the time of each trade for Bitcoin trades during 24 hours (19-Apr-2023).

- i) Report the number of trades in the dataset, and the minimum and maximum trade price during the time interval in the dataset.
  - ii) For each transaction, compute the spread measures:
  - Quoted spread  $qs_t = ask_t bid_t$
  - Effective spread  $es_t = 2d_t(p_t mid_t)$  where  $mid_t = \frac{1}{2}(ask_t + bid_t)$  is the mid-price, and  $d_t$  is the trade sign ( $\pm 1$  for buy/sell). The dataset has a column "SIDE" which reports the trade sign. Use this instead of the Lee-Ready rule for computing the effective spread. Note that using getLiquidityMeasures will return the incorrect result, as it assumes the Lee-Ready rule.

Compute the averages of these two measures over all transactions.

iii) Compute the Roll's estimate of the bid-ask spread.

Hint. Start with the time series of  $p_t$  (the trade prices). Compute the covariances acf(type="covariance") of the price changes  $\Delta p_t = p_t - p_{t-1}$ . Denoting the covariances at lags 0 and 1 as  $\gamma_0$  and  $\gamma_1$ , respectively, proceed as in the lecture on the Roll model.

**Extra credit.** (iv) Compare the trade sign in SIDE with the prediction of the Lee-Ready empirical rule. What is the accuracy of the Lee-Ready rule? This can be measured as the percentage of trade signs which are predicted correctly by the Lee-Ready rule.