

- $\text{TEV}(\omega) = \sigma(r_P(\omega) - r_{\text{SPY}})$  is the '**Tracking Error Volatility**', which (if you're *really nerdy*) you can derive it as such:

$$\sigma(r_P(\omega) - r_{\text{SPY}}) = \sqrt{\omega^\top \Sigma \omega - 2\omega^\top \text{Cov}(r, r_{\text{SPY}}) + \sigma_{\text{SPY}}^2} \quad (3)$$

Oh yeah, I should probably define what '**FF3FM**' means; that would (probably) be helpful.

## 2.2 Fama–French Three-Factor Model

So, to echo the previous sentiment, we should (*almost surely*) explain what is this *funky* model we kept referencing:

$$r_i = r_f + \beta_i^3(r_M - r_f) + b_i^s r_{\text{SMB}} + b_i^v r_{\text{HML}} + \alpha_i + \epsilon_i \quad (4)$$

Sorry for writing (or, to be *really technical*, *typesetting*) more hieroglyphics. We gotta keep going for a bit—stay with me!

If we assume our *white noise/error terms*, on 'average', have a (numerical) value of 0 (i.e.,  $\mathbb{E}[\epsilon_i] = 0$ ), we can derive a new goofy equation:

$$\rho_i = r_f + \beta_i^3(\rho_M - r_f) + b_i^s \rho_{\text{SMB}} + b_i^v \rho_{\text{HML}} + \alpha_i \quad (5)$$

In the new *cursive script* defined above, the 3 coefficients  $\beta_i^3$ ,  $b_i^s$ , and  $b_i^v$  are estimated by making a *linear regression*, or, in 'plain English', drawing a *line of best fit* of the *time series*  $y_i = \rho_i - r_f$  against the other cool time series  $\rho_M - r_f$  (**Momentum Factor**),  $r_{\text{SMB}}$  (**Size Factor**), and  $\rho_{\text{HML}}$  (**Value Factor**).

I feel like I'm forgetting something . . .

Oh yeah! There's an extra (nerdy) thingy we gotta verify: (generally),  $\beta_i^m \neq \beta_i^3$  and needs to be estimated by a separate regression or directly computed.