Bangladesh University of Engineering & Technology Department of Computer Science & Engineering CSE 402: Artificial Intelligence Sessional Session July 2016

Expression Generation with Genetic Algorithm

1 Introduction

In this assignment you have to implement Genetic Algorithm to solve a problem of expression generation. An expression or mathematical expression is a finite combination of symbols that is well-formed according to rules that depend on the context. In this problem, we will only consider simple expressions that contain numbers and mathematical operators. For simplicity, the numbers are in range [1,9], and operator are $\{+,-,\times\}$. So, an expression can be evaluated to get a value in range $[-\infty,\infty]$. For example, consider a simple expression.

$$8 \times 7 - 2 \times 9 \times 4 - 1 + 7 \times 7 = 32$$

This expression evaluates to the value 32. It is easy to evaluate a value from an expression. In this assignment, the task is just the opposite. You have to generate an expression from a given value (i.e. given a value 32, generate an expression that evaluates to 32).

Note that, different expressions can evaluate to a same value. It will be mentioned how many digits and operators you need in the generated expression. In the above expression, there are 8 digits and 7 operators. The number of operator will be always 1 less than the number of digits. The input will contain the number of operators and the desired value. From this information, you have to generate the best expression using Genetic Algorithm that evaluates to the value. It is possible that an expression which evaluates to the target value is not generated in possible amount of time. Here, best expression means the expression that evaluates to the closest of the desired value.

2 Implementation

Genetic Algorithm is given in Figure ??.

2.1 Representation

Each individual is a vector of length l = d + o, where d is the number of digits in the expression and o is the number of operators. You can keep two different

```
The Genetic Algorithm (GA)
 1: popsize ← desired population size
 2: P ← {}
 3: for popsize times do
        P \leftarrow P \cup \{\text{new random individual}\}
 5: Best ← □
 6: repeat
         for each individual P_i \in P do
 7:
              AssessFitness(P_i)
             if Best = \square or Fitness(P_i) > \text{Fitness}(Best) then
 9:
10:
                  Best \leftarrow P_i
11:
         Q \leftarrow \{\}
12:
         for popsize/2 times do
             Parent P_a \leftarrow \text{SelectWithReplacement}(P)
13:
             Parent P_b \leftarrow \mathsf{SelectWithReplacement}(P)
             Children C_a, C_b \leftarrow \text{Crossover}(\text{Copy}(P_a), \text{Copy}(P_b))
15:
16:
              Q \leftarrow Q \cup \{ \mathsf{Mutate}(C_a), \mathsf{Mutate}(C_b) \}
17:
18: until Best is the ideal solution or we have run out of time
19: return Best
```

Figure 1: Genetic Algorithm

arrays for keeping the digits and operators or use a string to keep them all for implementation purpose. But each individual is to considered as a vector including digits and operators in sequence as in the actual mathematical expression.

2.2 Initial Population

Let, the population size be N. Randomly generate N number of individuals of length l.

2.3 Fitness Function

Generally better fitness means a better individual that is closer to optimal solution. In this problem, fitness f_i for an individual i is the absolute difference between the desired value v and the value i evaluates.

$$f_i = -|v - evaluate(i)|$$

Here, better fitness means higher f_i value. Consider two individuals i and j. The fitness values are f_i and f_j , respectively. If $f_i > f_j$, then i is a better individual than j.

2.4 Selection

We will use Tournament Selection where you will choose t number of individuals from the population randomly, and select the best individual among the t individuals according to fitness function. Use t=5 for the experiment.

```
      Algorithm
      Tournament Selection

      1: P \leftarrow population

      2: t \leftarrow tournament size, t \geq 1

      3: Best \leftarrow individual picked at random from P with replacement

      4: for i from 2 to t do

      5: Next \leftarrow individual picked at random from P with replacement

      6: for i Fitness(Next) > Fitness(Best) then

      7: Best \leftarrow Next

      8: for i for individual picked at random from <math>P with replacement

      6: for i for individual picked at random from <math>P with replacement

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      7: for individual picked at random from <math>P with replacement

      8: for individual picked at random from <math>P with replacement

      9: for individual picked at random from <math>P with replacement

      1: for individual picked at random from <math>P with replacement

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      2: for individual picked at random from <math>P with replacement

      3: for individual picked at random from <math>P with replacement

      4: for individual picked at random from <math>P with replacement

      5: for individual picked at
```

Figure 2: Tournament Selection

2.5 Crossover

Two individuals are selected from the population for crossover, and are called parents. Let, P_a, P_b are two parents. Two types of crossovers are taken into consideration with 50% probability for each.

• One Point Crossover: It randomly picks an integer c in the range [1, l], inclusive, and swaps all the indexes greater than c.

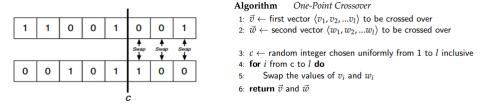


Figure 3: One Point Crossover

• Two Point Crossover: It randomly picks two numbers c and d in the range [1, l], inclusive, and swap the indexes between them.

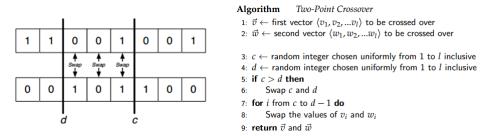


Figure 4: Two Point Crossover

2.6 Mutation

For each element of the vector, flip a coin of a certain probability p (often 1/l, where l is the length of the vector). Each time the coin comes up heads, check whether it is a digit or an operator. If it is a digit, then apply Random Walk Mutation as shown in Figure ??. If it is an operator, change it to one of the other two operators with 50% probability.

```
Algorithm 42 Random Walk Mutation
 1: \vec{v} \leftarrow \text{integer vector } \langle v_1, v_2, ... v_l \rangle to be mutated
 2: p \leftarrow \text{probability of randomizing an integer}
                                                                       \triangleright Perhaps you might set p to 1/l or lower
 3: b \leftarrow \text{coin-flip probability}
                                                                 values so the random walks are longer
 4: \mathbf{for}\ i\ \mathsf{from}\ 1\ \mathsf{to}\ l\ \mathbf{do}
        if p \geq random number chosen uniformly from 0.0 to 1.0 inclusive then
             repeat
                 n \leftarrow either a 1 or -1, chosen at random.
                 if v_i + n is within bounds for legal integer values then
q.
                     v_i \leftarrow v_i + n
                 else
10.
                     v_i \leftarrow v_i - n
11:
             until b < \text{random number chosen uniformly from 0.0 to 1.0 inclusive}
13: return \vec{v}
```

Figure 5: Random Walk Mutation

3 Input

Input consists two integers. The first integer denotes the number of operators the expression contains. The second number denotes the desired value that the expected expression evaluates to.

4 Experiment and Results

Show the best individual (expression) and generate a table as shown for each of the input given for different N.

Table 1: Experiment

Target value	No. of operators	popsize, N	No. of generations	Best-Fitness

5 Conclusion

For any query or confusion please feel free to email me at ahmaadsabbir@gmail.com.

Prepared bySabbir Ahmad
Lecturer
Department of CSE, BUET
ahmadsabbir@cse.buet.ac.bd
ahmaadsabbir@gmail.com
http://teacher.buet.ac.bd/ahmadsabbir