

Inertia Identification

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I. SUMMARY

The general model we are using for surge and yaw is

$$m\dot{y} + k_1y + k_2y^2 = F$$

where $y(t)$ is the forward speed or yaw rate, m is the inertia, k_1 is the linear drag term, k_2 is the quadratic term, and F is the constant thrust or torque. If we assume $k_1 = 0$, so there is only quadratic drag, the solution to the differential equation takes the form

$$y(t) = y_{ss} \tanh\left(y_{ss} \frac{k_2}{m} t\right)$$

where y_{ss} is the steady state velocity. We know the drag coefficient, k_2 , from the steady-state experiment results, so there are two unknown parameters, the total inertia (m) and the steady-state velocity (y_{ss}).

Experimentally we measured step response in surge and yaw. The result is data for each step response experiment. We can use MATLAB to fit a curve of the form above to the data, which results in something like...

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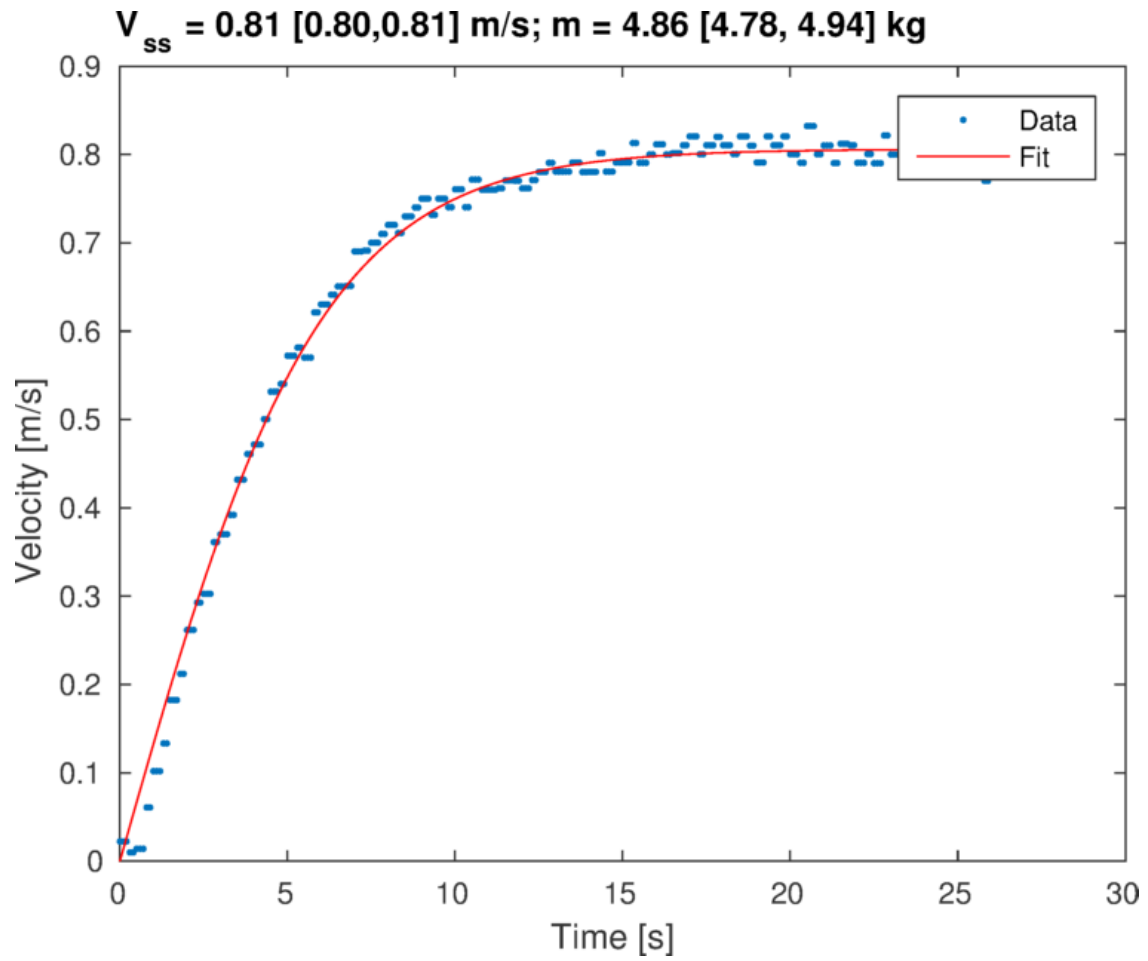


Fig. 1. Results from curve fit. Parameter values are given as final value and 9% confidence bounds.