An Analysis of Image Denoising Techniques

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Abstract

Digital de-noising techniques are used to filter out unwanted noise in a signal. In images, noisy signals are present in the form of non coherent salt and pepper noise and Gaussian noises to coherent noise introduced inherently from the imager or from signal processing algorithms. This paper examines some of the common methods for removing unwanted noise, along with implementing more complex filtering techniques in the form of wavelet filtering.

1 Introduction

This paper explores noise filtering techniques implemented in Python and an available Python image processing library OpenCV. The filters are implemented on images with random Gaussian noise and Salt and Pepper noise, and their output Peak Signal to Noise Ratios are compared. The two python files are detailed in section 5. The underlying input image FIGUREX and it's corresponding noisy images NoisyIMAGES are in this figure. The standard filters that were implemented using the OpenCV library were the: blur, $gaussian\ blur$, median and bilateral filter and the filter windows were varied in order to generate the optimal resulting filter. The Haar Wavelet Transform was implemented by hand, and the Daubechies 4 wavelet was implemented using the available PyWavelets library after an attempt by hand of the algorithm was unsuccessful.

2 Methods/Approach

2.1 Noise Generation

Two images were generated with different noise distributions for the purpose of analyzing the efficacy of the different applied filtering techniques. The first noisy image was generated with a normal Gaussian distribution that had been scaled by a factor of 10. The noise was scaled in order to be more visually evident in the image along with increasing the noise power in the image. Gaussian noise is generally a common form of noise that principally arises in images during acquisition and is caused by a number of factors, a few being poor illumination, high circuitry temperature, and electronic interference. The second noisy image was generated through adding a 0.4% Salt and Pepper (S&P) distribution. The S&P noise added was equally distributed "Salt" white pixels, and "Pepper" black pixels. S&P noise potentially occurs in images were intermittent and non-reliable image communication systems are present as they can elicit sharp and sudden disturbances in the image signal.

2.2 Haar Wavelet Transform

The Haar Wavelet Transform (HWT), proposed by the Hungarian mathematician Alfréd Haar is a computationally efficient method for analyzing the local aspects of an image. A key advantage to

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the use and implementation of the HWT is in it simplicity to compute, along with it being easier to understand than most other wavelet transforms. A great benefit to using the HWT is that it is effective in signal and image compression. The HWT can be expressed in terms of matrix operations such that the Forward HWT is:

$$y_n = W_n v_n \tag{1}$$

where v_n is the input vector to be transformed, W_n is the HWT matrix, and y_n is the transformed output vector. This calculation can be even more easily illustrated in the form of the following expanded graphic that details the Haar transform of an input vector of length 8, its corresponding Haar Matrix W_8 , and its output vector which is simply the mean of two sequential pixel elements for the first half of the vector, and then the difference of two sequential pixel elements divided by two for the second half of the output vector.

$$\tilde{W}_8 \mathbf{v} = \begin{bmatrix} 1/2 & 1/2 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1/2 & 1/2 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1/2 & 1/2 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1/2 & 1/2 & 0 & 0 \\ -1/2 & 1/2 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -1/2 & 1/2 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1/2 & 1/2 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -1/2 & 1/2 \end{bmatrix} \cdot \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \\ v_6 \\ v_7 \\ v_8 \end{bmatrix} = \begin{bmatrix} (v_1 + v_2)/2 \\ (v_3 + v_4)/2 \\ (v_5 + v_6)/2 \\ (v_7 + v_8)/2 \\ (v_2 - v_1)/2 \\ (v_4 - v_3)/2 \\ (v_6 - v_5)/2 \\ (v_8 - v_7)/2 \end{bmatrix} = \mathbf{y}$$

Figure 1: Haar Transform

The algorithm for this vector-wise HWT can be found in the $OneD_HWT$ function in the DWT.py file. On a 2D image the HWT is first calculated on the rows of the image, and then the HWT is calculated on the columns of the image and this implementation can be found in the $TwoD_HWT$ in the DWT.py file. This 2D function also accounts for multiple iterations of the HWT in that each following iteration will reduce the image into smaller sub-wavelets. And the Inverse HWT can be calculated by the following equation with the same variables:

$$x_n = H^T y_n \tag{2}$$

The HWT can be

2.3 Thresholding

Pixel thresholding is often a simple but efficient non-linear denoising approach during the application of a wavelet transform. The thresholding is performed on the wavelet transformed image, and then the image is inverse wavelet transformed to yield a filtered output image. To determine the best threshold value to set, the detThreshold function from dataSetup.py was used. The function first iterates through threshold values, then thresholds the Haar Wavelet Transformed image, then inverse Haar Wavelet Transforms the thresholded image, and finally calculates the Peak Signal to Noise ratio of the filtered image. The threshold is chosen based off of the one that results in the largest Peak Signal to Noise Ratio.

Hard Thresholding

$$D^{H}(d|T) = \begin{cases} 0, & \text{if } |d| \le T \\ d, & \text{if } |d| > T \end{cases}$$

$$(3)$$

Soft Thresholding

$$D^{S}(d|T) = \begin{cases} 0, & \text{if } |d| \le T \\ d - T, & \text{if } d > T \\ d + T, & \text{if } d < -T \end{cases}$$
 (4)

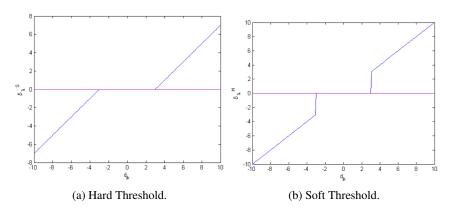


Figure 2: Thresholding Methods

3 Results

3.1 Peak Signal to Noise Ratio

In order to analyze the utility of the aforementioned filtering techniques the Peak Signal to Noise Ratios (PSNR) for each filtered image was calculated. The PSNR of an image is the maximum power of an image and the power of the image noise. The following equation 5 details the calculations for PSNR.

$$PSNR = 10 * log_{10} \left(\frac{MAX^2}{MSE}\right) \tag{5}$$

Where MAX is the maximum grayscale pixel value for the image which in this case 256, and MSE is the Mean Squared Error between the filtered output image and the noisy image. By taking the maximum pixel

4 Conclusion

Filter	PSNR Gaussian	PSNR SP
Blur	33.651	51.42
Gaussian Blur	33.91	51.42
Meidan	34.07	51.42
Bilateral	33.043	33.293
Soft HWT	26.055	26.684
Hard HWT	30.849	31.156

References

References follow the acknowledgments. Use unnumbered first-level heading for the references. Any choice of citation style is acceptable as long as you are consistent. It is permissible to reduce the font size to small (9 point) when listing the references. Remember that you can use a ninth page as long as it contains *only* cited references.

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- [3] Hasselmo, M.E., Schnell, E. & Barkai, E. (1995) Dynamics of learning and recall at excitatory recurrent synapses and cholinergic modulation in rat hippocampal region CA3. *Journal of Neuroscience* **15**(7):5249-5262.

- **5** Software Lisiting
- 5.1 dataSetup
- 5.2 DWT