

exploratory analysis

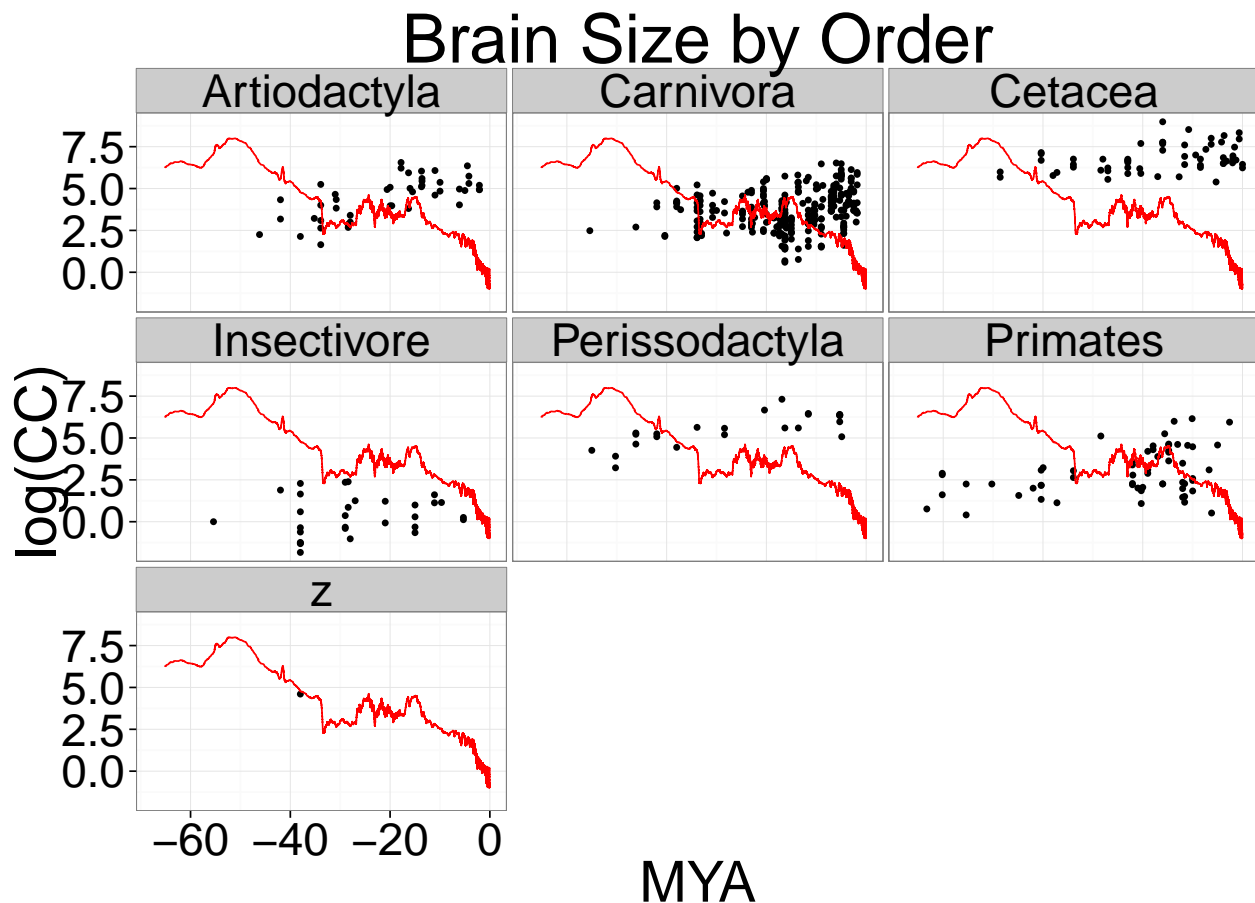
Did a bit of format cleaning, and ended up with a file called “brainclimatedata.txt”

First, I want a simple figure showing brain size over time

```
library(ggplot2)
library(scales)

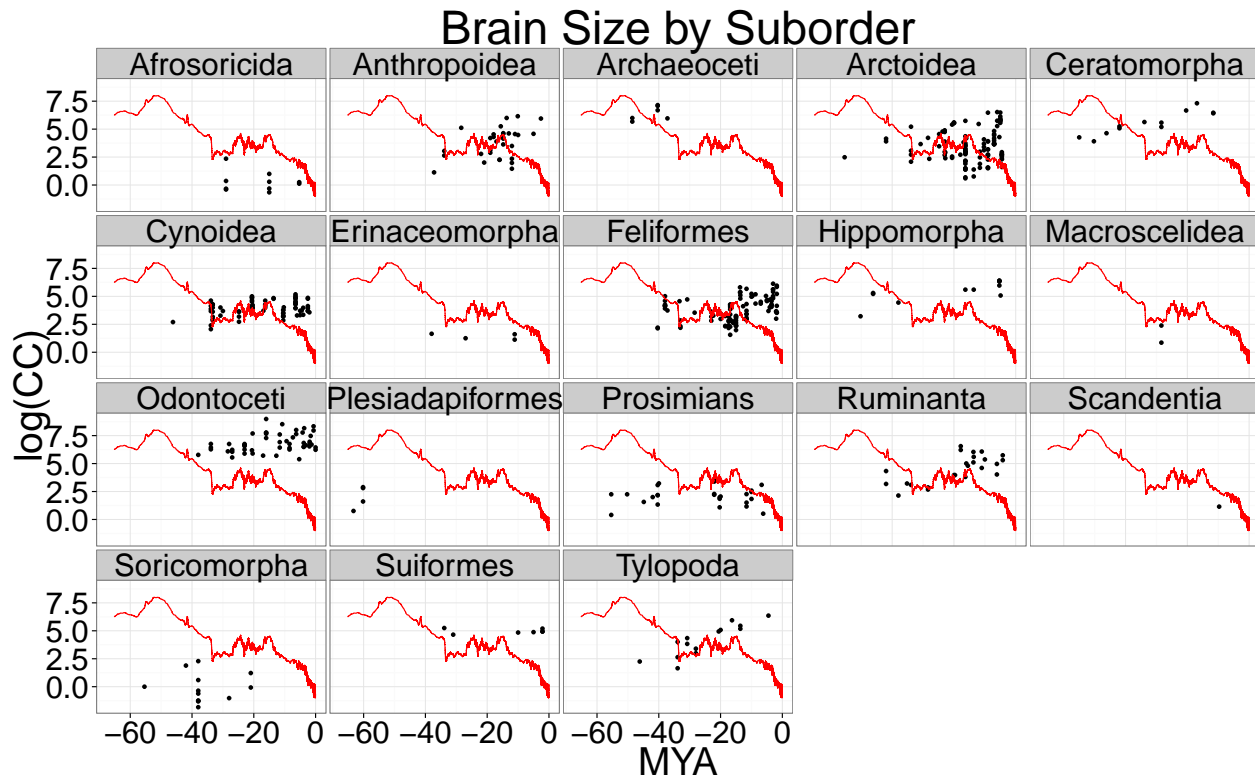
brains <- read.table("brainclimatedata.txt", header=TRUE, sep="\t")
brains$Species <- gsub(" ", "_", brains$Species) #remove spaces
zachos <- read.table("Zachos2001Climate.txt", header=TRUE, sep="\t")
zachos$filteredO18 <- filter(zachos$o18, filter = rep(1, 70), method = "convolution")

brainsOverTime_order <- ggplot(data=brains) +
  geom_point(aes(Actual.MYA, log(CC))) +
  facet_wrap(~Order) +
  geom_line(data=zachos, aes(x=age*-1, y=rescale(filteredO18*-1, c(-1,8))), color="red") +
  theme_bw(35) +
  labs(x="MYA", title="Brain Size by Order")
suppressWarnings(print(brainsOverTime_order))
```



```
suppressWarnings(ggsave("brainsOverTime_order.pdf", width=15, height=10, units="in"))
```

```
brainsOverTime_suborder <- ggplot(data=brains) +
  geom_point(aes(Actual.MYA, log(CC))) +
  facet_wrap(~Suborder) +
  geom_line(data=zachos, aes(x=age*-1, y=rescale(filtered018*-1, c(-1,8))), color="red") +
  theme_bw(35) +
  labs(x="MYA", title="Brain Size by Suborder")
suppressWarnings(print(brainsOverTime_suborder))
```



```
suppressWarnings(ggsave("brainsOverTime_suborder.pdf", width=15, height=10, units="in"))
```

Multiple regression

It strikes me that a single multiple regression is more appropriate than many individual correlation analyses. Of course, there are parametric assumptions that we need to address, and we should definitely look into doing this in a phylogenetic context, as these data are likely phylogenetically autocorrelated.

5 Ma time bins

First I did a multiple regression of $\log(CC)$ by `mean_oxy`, `sd_oxy`, and `slope_oxy`, with all possible interaction terms. This is the 'fullMod_5MA'.

Second, I did a sparse model, with no interaction terms. This is the `sparseMod_5MA`

```
fullMod_5MA <- lm(log(CC) ~ X5Mya_M_oxy * X5Mya_slope_oxy * X5Mya_SD_oxy, data = brains)
summary(fullMod_5MA)
```

```
##
## Call:
## lm(formula = log(CC) ~ X5Mya_M_oxy * X5Mya_slope_oxy * X5Mya_SD_oxy,
##     data = brains)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.35  -1.09  -0.07   1.10   5.64
##
## Coefficients:
##                                Estimate Std. Error t value
## (Intercept)                   0.554      2.055    0.27
## X5Mya_M_oxy                   1.756      0.947    1.85
## X5Mya_slope_oxy               42.912     15.258    2.81
## X5Mya_SD_oxy                  7.412      6.980    1.06
## X5Mya_M_oxy:X5Mya_slope_oxy   -16.175      7.141   -2.26
## X5Mya_M_oxy:X5Mya_SD_oxy      -4.294      3.257   -1.32
## X5Mya_slope_oxy:X5Mya_SD_oxy -141.389     45.461   -3.11
## X5Mya_M_oxy:X5Mya_slope_oxy:X5Mya_SD_oxy  56.863     20.938    2.72
##                                Pr(>|t|)
## (Intercept)                   0.7874
## X5Mya_M_oxy                   0.0643 .
## X5Mya_slope_oxy               0.0051 **
## X5Mya_SD_oxy                  0.2888
## X5Mya_M_oxy:X5Mya_slope_oxy   0.0239 *
## X5Mya_M_oxy:X5Mya_SD_oxy      0.1879
## X5Mya_slope_oxy:X5Mya_SD_oxy  0.0020 **
## X5Mya_M_oxy:X5Mya_slope_oxy:X5Mya_SD_oxy 0.0068 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.73 on 500 degrees of freedom
## Multiple R-squared:  0.0983, Adjusted R-squared:  0.0857
## F-statistic: 7.79 on 7 and 500 DF,  p-value: 5.81e-09
```

```
sparseMod_5MA <- lm(log(CC) ~ X5Mya_M_oxy + X5Mya_slope_oxy + X5Mya_SD_oxy, data = brains)
summary(sparseMod_5MA)
```

```
##
## Call:
## lm(formula = log(CC) ~ X5Mya_M_oxy + X5Mya_slope_oxy + X5Mya_SD_oxy,
##     data = brains)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.269  -1.044  -0.068   1.175   5.319
##
## Coefficients:
##                                Estimate Std. Error t value Pr(>|t|)
## (Intercept)                   2.384      0.426    5.59 3.7e-08 ***
## X5Mya_M_oxy                   0.734      0.124    5.93 5.6e-09 ***
## X5Mya_slope_oxy               0.424      0.680    0.62  0.53
## X5Mya_SD_oxy                 -0.153      1.011   -0.15  0.88
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.75 on 504 degrees of freedom
## Multiple R-squared:  0.0728, Adjusted R-squared:  0.0673
## F-statistic: 13.2 on 3 and 504 DF,  p-value: 2.64e-08
```

1 Ma time bins

```
fullMod_1MA <- lm(log(CC) ~ X1Mya_M_oxy * X1Mya_slope_oxy * X1Mya_SD_oxy, data = brains)
summary(fullMod_1MA)
```

```
##
## Call:
## lm(formula = log(CC) ~ X1Mya_M_oxy * X1Mya_slope_oxy * X1Mya_SD_oxy,
##     data = brains)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.498 -1.069 -0.047   1.101   5.289
##
## Coefficients:
##                                Estimate Std. Error t value
## (Intercept)                   -0.0802     1.1445   -0.07
## X1Mya_M_oxy                     1.5066     0.5258    2.87
## X1Mya_slope_oxy                 11.5317     5.5200    2.09
## X1Mya_SD_oxy                    9.5055     4.4767    2.12
## X1Mya_M_oxy:X1Mya_slope_oxy     -4.5690     2.4437   -1.87
## X1Mya_M_oxy:X1Mya_SD_oxy        -3.0095     2.0415   -1.47
## X1Mya_slope_oxy:X1Mya_SD_oxy    -32.6204    19.1550   -1.70
## X1Mya_M_oxy:X1Mya_slope_oxy:X1Mya_SD_oxy  12.8164     8.6040    1.49
##                                Pr(>|t|)
## (Intercept)                     0.9442
## X1Mya_M_oxy                      0.0043 **
## X1Mya_slope_oxy                   0.0372 *
## X1Mya_SD_oxy                      0.0342 *
## X1Mya_M_oxy:X1Mya_slope_oxy       0.0621 .
## X1Mya_M_oxy:X1Mya_SD_oxy          0.1411
## X1Mya_slope_oxy:X1Mya_SD_oxy      0.0892 .
## X1Mya_M_oxy:X1Mya_slope_oxy:X1Mya_SD_oxy  0.1370
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.74 on 500 degrees of freedom
## Multiple R-squared:  0.0964, Adjusted R-squared:  0.0837
## F-statistic: 7.62 on 7 and 500 DF,  p-value: 9.46e-09
```

```
sparseMod_1MA <- lm(log(CC) ~ X1Mya_M_oxy + X1Mya_slope_oxy + X1Mya_SD_oxy, data = brains)
summary(sparseMod_1MA)
```

```
##
## Call:
```

```
## lm(formula = log(CC) ~ X1Mya_M_oxy + X1Mya_slope_oxy + X1Mya_SD_oxy,
##     data = brains)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.432 -1.090 -0.053  1.109  5.467
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      1.979      0.381   5.19 3.1e-07 ***
## X1Mya_M_oxy       0.705      0.113   6.26 8.1e-10 ***
## X1Mya_slope_oxy  -0.132      0.263  -0.50  0.62
## X1Mya_SD_oxy      1.524      1.222   1.25  0.21
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.75 on 504 degrees of freedom
## Multiple R-squared:  0.0795, Adjusted R-squared:  0.074
## F-statistic: 14.5 on 3 and 504 DF,  p-value: 4.49e-09
```

In both the sparse and full models, mean_oxy is highly significant.

PGLS

PGLS using the Bininda-Emonds tree, and the brain data for extant taxa that match the names in the tree.

```
library(caper)
```

```
## Loading required package: ape
## Loading required package: MASS
## Loading required package: mvtnorm
```

```
treez <- read.nexus("Bininda_Emonds_correctedDates_FULLPHYLOG.txt")
tree <- treez[[grep(pattern = "bestDates", names(treez))]] #get the best dates tree
rm(treez)
```

```
#remove a few rows that don't have real species names. Otherwise comparative.data() complains about dup
brains <- brains[brains$Species != "new_species", ]
```

```
#make comparative data object
braintree <- comparative.data(tree, brains, "Species")
```

Using the 228 taxa with exact matches in the Bininda Emonds tree

PGLS with 5 Mya Bins

```
PGLS_5Mya_sparse <- pgls(formula = log(CC) ~ X5Mya_M_oxy + X5Mya_slope_oxy + X5Mya_SD_oxy, data = brains)
sumMod_sparse <- summary(PGLS_5Mya_sparse)
sumMod_sparse
```

```
##
## Call:
## pgls(formula = log(CC) ~ X5Mya_M_oxy + X5Mya_slope_oxy + X5Mya_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.4841 -0.1239 -0.0197  0.0860  0.5910
##
## Branch length transformations:
##
## kappa  [Fix]  : 1.000
## lambda [ ML]  : 0.995
## lower bound : 0.000, p = <2e-16
## upper bound : 1.000, p = 0.56
## 95.0% CI    : (0.972, NA)
## delta  [Fix]  : 1.000
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.2969     0.7275   3.16  0.0018 **
## X5Mya_M_oxy     0.2554     0.1477   1.73  0.0851 .
## X5Mya_slope_oxy 0.3392     0.6853   0.49  0.6211
## X5Mya_SD_oxy   -0.0689     1.0823  -0.06  0.9493
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.163 on 224 degrees of freedom
## Multiple R-squared: 0.0168, Adjusted R-squared: 0.00364
## F-statistic: 1.28 on 3 and 224 DF, p-value: 0.283
```

```
PGLS_5Mya_full <- pgls(formula = log(CC) ~ X5Mya_M_oxy * X5Mya_slope_oxy * X5Mya_SD_oxy, data = braintree)
sumMod_full <- summary(PGLS_5Mya_full)
sumMod_full
```

```
##
## Call:
## pgls(formula = log(CC) ~ X5Mya_M_oxy * X5Mya_slope_oxy * X5Mya_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.4611 -0.0992 -0.0016  0.1158  0.6085
##
## Branch length transformations:
##
## kappa  [Fix]  : 1.000
## lambda [ ML]  : 0.993
## lower bound : 0.000, p = <2e-16
## upper bound : 1.000, p = 0.42
## 95.0% CI    : (0.969, NA)
## delta  [Fix]  : 1.000
##
## Coefficients:
```

```
##                                Estimate Std. Error t value
## (Intercept)                   -2.957      3.524   -0.84
## X5Mya_M_oxy                    2.587      1.636    1.58
## X5Mya_slope_oxy               -0.989     14.253   -0.07
## X5Mya_SD_oxy                  20.978     14.306    1.47
## X5Mya_M_oxy:X5Mya_slope_oxy    1.633      6.302    0.26
## X5Mya_M_oxy:X5Mya_SD_oxy      -9.645      6.945   -1.39
## X5Mya_slope_oxy:X5Mya_SD_oxy  -27.502     50.144   -0.55
## X5Mya_M_oxy:X5Mya_slope_oxy:X5Mya_SD_oxy  11.253     23.441    0.48
##                                Pr(>|t|)
## (Intercept)                    0.40
## X5Mya_M_oxy                    0.12
## X5Mya_slope_oxy                0.94
## X5Mya_SD_oxy                   0.14
## X5Mya_M_oxy:X5Mya_slope_oxy    0.80
## X5Mya_M_oxy:X5Mya_SD_oxy      0.17
## X5Mya_slope_oxy:X5Mya_SD_oxy  0.58
## X5Mya_M_oxy:X5Mya_slope_oxy:X5Mya_SD_oxy  0.63
##
## Residual standard error: 0.161 on 220 degrees of freedom
## Multiple R-squared: 0.0433, Adjusted R-squared: 0.0129
## F-statistic: 1.42 on 7 and 220 DF, p-value: 0.197
```

5 Mya summary

- full Model
 - overall P value = 0.1971
 - ML value for lambda = 0.9931
 - adjusted R^2 = 0.0129
- sparse Model
 - overall P value for sparse model = 0.2832
 - ML value for lambda sparse model = 0.9953
 - adjusted R^2 = 0.0036

PGLS with 1 Mya Bins

```
PGLS_1Mya_sparse <- pgls(formula = log(CC) ~ X1Mya_M_oxy + X1Mya_slope_oxy + X1Mya_SD_oxy, data = brain)
sumMod_sparse <- summary(PGLS_1Mya_sparse)
sumMod_sparse
```

```
##
## Call:
## pgls(formula = log(CC) ~ X1Mya_M_oxy + X1Mya_slope_oxy + X1Mya_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min      1Q  Median      3Q      Max
## -0.594 -0.110 -0.009  0.109  0.397
##
```

```
## Branch length transformations:
##
## kappa [Fix] : 1.000
## lambda [ ML] : 0.996
## lower bound : 0.000, p = <2e-16
## upper bound : 1.000, p = 0.59
## 95.0% CI : (0.973, NA)
## delta [Fix] : 1.000
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.5251 0.6902 3.66 0.00032 ***
## X1Mya_M_ox 0.2301 0.1540 1.49 0.13640
## X1Mya_slope_ox 0.0703 0.2774 0.25 0.80015
## X1Mya_SD_ox -0.8666 1.1975 -0.72 0.47005
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.164 on 224 degrees of freedom
## Multiple R-squared: 0.0164, Adjusted R-squared: 0.00319
## F-statistic: 1.24 on 3 and 224 DF, p-value: 0.295

PGLS_1Mya_full <- pgls(formula = log(CC) ~ X1Mya_M_ox * X1Mya_slope_ox * X1Mya_SD_ox, data = braintree)
sumMod_full <- summary(PGLS_1Mya_full)
sumMod_full
```

```
##
## Call:
## pgls(formula = log(CC) ~ X1Mya_M_ox * X1Mya_slope_ox * X1Mya_SD_ox,
## data = braintree, lambda = "ML")
##
## Residuals:
## Min 1Q Median 3Q Max
## -0.5877 -0.1029 -0.0192 0.0704 0.5635
##
## Branch length transformations:
##
## kappa [Fix] : 1.000
## lambda [ ML] : 0.994
## lower bound : 0.000, p = <2e-16
## upper bound : 1.000, p = 0.48
## 95.0% CI : (0.970, NA)
## delta [Fix] : 1.000
##
## Coefficients:
## Estimate Std. Error t value
## (Intercept) 0.424 1.815 0.23
## X1Mya_M_ox 0.932 0.665 1.40
## X1Mya_slope_ox -1.634 8.221 -0.20
## X1Mya_SD_ox 6.863 6.702 1.02
## X1Mya_M_ox:X1Mya_slope_ox 0.878 3.317 0.26
## X1Mya_M_ox:X1Mya_SD_ox -2.421 2.499 -0.97
## X1Mya_slope_ox:X1Mya_SD_ox 8.420 29.333 0.29
## X1Mya_M_ox:X1Mya_slope_ox:X1Mya_SD_ox -3.961 11.892 -0.33
```



```
##                                Pr(>|t|)
## (Intercept)                   0.82
## X1Mya_M_oxy                   0.16
## X1Mya_slope_oxy              0.84
## X1Mya_SD_oxy                 0.31
## X1Mya_M_oxy:X1Mya_slope_oxy  0.79
## X1Mya_M_oxy:X1Mya_SD_oxy     0.33
## X1Mya_slope_oxy:X1Mya_SD_oxy 0.77
## X1Mya_M_oxy:X1Mya_slope_oxy:X1Mya_SD_oxy 0.74
##
## Residual standard error: 0.163 on 220 degrees of freedom
## Multiple R-squared: 0.0291, Adjusted R-squared: -0.00176
## F-statistic: 0.943 on 7 and 220 DF, p-value: 0.474
```

1 Mya summary

- full Model
 - overall P value = 0.4741
 - ML value for lambda = 0.9942
 - adjusted R^2 = -0.0018
- sparse Model
 - overall P value for sparse model = 0.2951
 - ML value for lambda sparse model = 0.9957
 - adjusted R^2 = 0.0032

PGLS with 400 Ka Bins

```
PGLS_400k_sparse <- pgls(formula = log(CC) ~ X400k_M_oxy + X400k_slope_oxy + X400k_SD_oxy, data = brain)
sumMod_sparse <- summary(PGLS_400k_sparse)
sumMod_sparse
```

```
##
## Call:
## pgls(formula = log(CC) ~ X400k_M_oxy + X400k_slope_oxy + X400k_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.4077 -0.1064 -0.0096  0.0966  0.5907
##
## Branch length transformations:
##
## kappa  [Fix]  : 1.000
## lambda [ ML]  : 0.996
##   lower bound : 0.000, p = <2e-16
##   upper bound : 1.000, p = 0.59
##   95.0% CI    : (0.973, NA)
## delta  [Fix]  : 1.000
##
```

```

## Coefficients:
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)      2.556      0.634   4.03 7.6e-05 ***
## X400k_M_oxy       0.176      0.127   1.38   0.17
## X400k_slope_oxy   0.137      0.139   0.98   0.33
## X400k_SD_oxy     -0.464      1.065  -0.44   0.66
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.163 on 224 degrees of freedom
## Multiple R-squared:  0.0189, Adjusted R-squared:  0.00575
## F-statistic: 1.44 on 3 and 224 DF,  p-value: 0.233

PGLS_400k_full <- pgls(formula = log(CC) ~ X400k_M_oxy * X400k_slope_oxy * X400k_SD_oxy, data = braintree)
sumMod_full <- summary(PGLS_400k_full)
sumMod_full

##
## Call:
## pgls(formula = log(CC) ~ X400k_M_oxy * X400k_slope_oxy * X400k_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.4798 -0.1070 -0.0290  0.0625  0.6185
##
## Branch length transformations:
##
## kappa  [Fix]  : 1.000
## lambda [ ML]  : 0.995
## lower bound : 0.000, p = <2e-16
## upper bound : 1.000, p = 0.51
## 95.0% CI    : (0.972, NA)
## delta  [Fix]  : 1.000
##
## Coefficients:
##                                     Estimate Std. Error t value
## (Intercept)                        1.426      1.355    1.05
## X400k_M_oxy                        0.607      0.472    1.29
## X400k_slope_oxy                    2.558      2.720    0.94
## X400k_SD_oxy                      4.240      5.109    0.83
## X400k_M_oxy:X400k_slope_oxy       -1.211      1.095   -1.11
## X400k_M_oxy:X400k_SD_oxy          -1.737      1.861   -0.93
## X400k_slope_oxy:X400k_SD_oxy      -7.245     10.499   -0.69
## X400k_M_oxy:X400k_slope_oxy:X400k_SD_oxy  3.808      4.169    0.91
##                                     Pr(>|t|)
## (Intercept)                        0.29
## X400k_M_oxy                        0.20
## X400k_slope_oxy                    0.35
## X400k_SD_oxy                      0.41
## X400k_M_oxy:X400k_slope_oxy       0.27
## X400k_M_oxy:X400k_SD_oxy          0.35
## X400k_slope_oxy:X400k_SD_oxy      0.49
## X400k_M_oxy:X400k_slope_oxy:X400k_SD_oxy 0.36

```

```
##
## Residual standard error: 0.163 on 220 degrees of freedom
## Multiple R-squared: 0.032, Adjusted R-squared: 0.0012
## F-statistic: 1.04 on 7 and 220 DF, p-value: 0.405
```

400Ka summary

- full Model
 - overall P value = 0.4048
 - ML value for lambda = 0.9946
 - adjusted R^2 = 0.0012
- sparse Model
 - overall P value for sparse model = 0.2325
 - ML value for lambda sparse model = 0.9957
 - adjusted R^2 = 0.0058

PGLS with 200 Ka Bins

```
PGLS_200k_sparse <- pgls(formula = log(CC) ~ X200k_M_oxy + X200k_slope_oxy + X200k_SD_oxy, data = brain)
sumMod_sparse <- summary(PGLS_200k_sparse)
sumMod_sparse
```

```
##
## Call:
## pgls(formula = log(CC) ~ X200k_M_oxy + X200k_slope_oxy + X200k_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.4549 -0.1151 -0.0087  0.1004  0.5766
##
## Branch length transformations:
##
## kappa  [Fix]   : 1.000
## lambda [ ML]   : 0.995
##   lower bound : 0.000, p = <2e-16
##   upper bound : 1.000, p = 0.57
##   95.0% CI    : (0.973, NA)
## delta  [Fix]   : 1.000
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.7548    0.6207    4.44 1.4e-05 ***
## X200k_M_oxy     0.1285    0.1234    1.04  0.299
## X200k_slope_oxy 0.1546    0.0704    2.20  0.029 *
## X200k_SD_oxy   -0.5548    0.6161   -0.90  0.369
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 0.162 on 224 degrees of freedom
## Multiple R-squared: 0.0388, Adjusted R-squared: 0.026
## F-statistic: 3.02 on 3 and 224 DF, p-value: 0.0307
```

```
PGLS_200k_full <- pglS(formula = log(CC) ~ X200k_M_oxy * X200k_slope_oxy * X200k_SD_oxy, data = braintr
sumMod_full <- summary(PGLS_200k_full)
sumMod_full
```

```
##
## Call:
## pglS(formula = log(CC) ~ X200k_M_oxy * X200k_slope_oxy * X200k_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.5664 -0.1066 -0.0143  0.0934  0.4415
##
## Branch length transformations:
##
## kappa  [Fix]  : 1.000
## lambda [ ML]  : 0.993
##   lower bound : 0.000, p = <2e-16
##   upper bound : 1.000, p = 0.39
##   95.0% CI   : (0.970, NA)
## delta  [Fix]  : 1.000
##
## Coefficients:
##                                     Estimate Std. Error t value
## (Intercept)                        1.30899     1.26926    1.03
## X200k_M_oxy                        0.73779     0.44322    1.66
## X200k_slope_oxy                    -0.07114     0.75770   -0.09
## X200k_SD_oxy                       5.08864     4.84320    1.05
## X200k_M_oxy:X200k_slope_oxy        -0.00537     0.22605   -0.02
## X200k_M_oxy:X200k_SD_oxy          -2.34662     1.73828   -1.35
## X200k_slope_oxy:X200k_SD_oxy      -0.19718     2.55672   -0.08
## X200k_M_oxy:X200k_slope_oxy:X200k_SD_oxy 0.49015     0.73657    0.67
##                                     Pr(>|t|)
## (Intercept)                        0.304
## X200k_M_oxy                        0.097
## X200k_slope_oxy                    0.925
## X200k_SD_oxy                       0.295
## X200k_M_oxy:X200k_slope_oxy        0.981
## X200k_M_oxy:X200k_SD_oxy          0.178
## X200k_slope_oxy:X200k_SD_oxy      0.939
## X200k_M_oxy:X200k_slope_oxy:X200k_SD_oxy 0.506
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.16 on 220 degrees of freedom
## Multiple R-squared: 0.0512, Adjusted R-squared: 0.021
## F-statistic: 1.7 on 7 and 220 DF, p-value: 0.111
```

200Ka summary

- full Model
 - overall P value = 0.1109
 - ML value for lambda = 0.9931
 - adjusted R^2 = 0.021
- sparse Model
 - overall P value for sparse model = 0.0307
 - ML value for lambda sparse model = 0.9955
 - adjusted R^2 = 0.026

PGLS with 100 Ka Bins

```
PGLS_100k_sparse <- pglS(formula = log(CC) ~ X100k_M_oxy + X100k_slope_oxy + X100k_SD_oxy, data = brain)
sumMod_sparse <- summary(PGLS_100k_sparse)
sumMod_sparse
```

```
##
## Call:
## pglS(formula = log(CC) ~ X100k_M_oxy + X100k_slope_oxy + X100k_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.4023 -0.0994 -0.0021  0.0989  0.5890
##
## Branch length transformations:
##
## kappa  [Fix]   : 1.000
## lambda [ ML]   : 0.995
##   lower bound : 0.000, p = <2e-16
##   upper bound : 1.000, p = 0.56
##   95.0% CI    : (0.972, NA)
## delta  [Fix]   : 1.000
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.6094     0.6149   4.24 3.2e-05 ***
## X100k_M_oxy     0.1820     0.1094   1.66  0.097 .
## X100k_slope_oxy  0.0315     0.0188   1.67  0.095 .
## X100k_SD_oxy   -0.6700     0.6605  -1.01  0.312
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.162 on 224 degrees of freedom
## Multiple R-squared: 0.0301, Adjusted R-squared: 0.0171
## F-statistic: 2.32 on 3 and 224 DF, p-value: 0.0762
```

```
PGLS_100k_full <- pglS(formula = log(CC) ~ X100k_M_oxy * X100k_slope_oxy * X100k_SD_oxy, data = braintr
sumMod_full <- summary(PGLS_100k_full)
sumMod_full
```

```
##
## Call:
## pglS(formula = log(CC) ~ X100k_M_oxy * X100k_slope_oxy * X100k_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.3979 -0.0959  0.0191  0.1056  0.5773
##
## Branch length transformations:
##
## kappa  [Fix]  : 1.000
## lambda [ ML]  : 0.995
##   lower bound : 0.000, p = <2e-16
##   upper bound : 1.000, p = 0.58
##   95.0% CI    : (0.972, NA)
## delta  [Fix]  : 1.000
##
## Coefficients:
##                                     Estimate Std. Error t value
## (Intercept)                       2.61606     0.96440    2.71
## X100k_M_oxy                        0.19745     0.30752    0.64
## X100k_slope_oxy                    -0.17391     0.43303   -0.40
## X100k_SD_oxy                      -0.79354     2.68392   -0.30
## X100k_M_oxy:X100k_slope_oxy         0.11951     0.16610    0.72
## X100k_M_oxy:X100k_SD_oxy            0.00419     0.95873    0.00
## X100k_slope_oxy:X100k_SD_oxy        0.48051     1.38692    0.35
## X100k_M_oxy:X100k_slope_oxy:X100k_SD_oxy -0.32485     0.53719   -0.60
##                                     Pr(>|t|)
## (Intercept)                       0.0072 **
## X100k_M_oxy                        0.5215
## X100k_slope_oxy                    0.6884
## X100k_SD_oxy                      0.7678
## X100k_M_oxy:X100k_slope_oxy         0.4726
## X100k_M_oxy:X100k_SD_oxy            0.9965
## X100k_slope_oxy:X100k_SD_oxy        0.7293
## X100k_M_oxy:X100k_slope_oxy:X100k_SD_oxy 0.5460
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.163 on 220 degrees of freedom
## Multiple R-squared: 0.0416, Adjusted R-squared: 0.0111
## F-statistic: 1.36 on 7 and 220 DF, p-value: 0.222
```

100ka summary

- full Model
 - overall P value = 0.2217

- ML value for $\lambda = 0.9955$
- adjusted $R^2 = 0.0111$
- sparse Model
 - overall P value for sparse model = 0.0762
 - ML value for λ sparse model = 0.9953
 - adjusted $R^2 = 0.0171$

PGLS with 40 Ka Bins

```
PGLS_40k_sparse <- pglS(formula = log(CC) ~ X40k_M_oxy + X40k_slope_oxy + X40k_SD_oxy, data = braintree, lambda = "ML")
sumMod_sparse <- summary(PGLS_40k_sparse)
sumMod_sparse
```

```
##
## Call:
## pglS(formula = log(CC) ~ X40k_M_oxy + X40k_slope_oxy + X40k_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.4939 -0.1207 -0.0246  0.0772  0.5918
##
## Branch length transformations:
##
## kappa  [Fix]   : 1.000
## lambda [ ML]   : 0.995
## lower bound : 0.000, p = <2e-16
## upper bound : 1.000, p = 0.53
## 95.0% CI    : (0.972, NA)
## delta  [Fix]   : 1.000
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.39753    0.59599   4.02 7.9e-05 ***
## X40k_M_oxy      0.23948    0.11276   2.12  0.035 *
## X40k_slope_oxy -0.00158    0.00488  -0.32  0.746
## X40k_SD_oxy    -0.39129    0.60688  -0.64  0.520
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.162 on 224 degrees of freedom
## Multiple R-squared: 0.0238, Adjusted R-squared: 0.0107
## F-statistic: 1.82 on 3 and 224 DF, p-value: 0.145
```

```
PGLS_40k_full <- pglS(formula = log(CC) ~ X40k_M_oxy * X40k_slope_oxy * X40k_SD_oxy, data = braintree, lambda = "ML")
sumMod_full <- summary(PGLS_40k_full)
sumMod_full
```

```
##
## Call:
```

```
## pglS(formula = log(CC) ~ X40k_M_oxy * X40k_slope_oxy * X40k_SD_oxy,
##       data = braintree, lambda = "ML")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.5974 -0.1091 -0.0239  0.0590  0.6155
##
## Branch length transformations:
##
## kappa  [Fix]  : 1.000
## lambda [ ML]  : 0.994
##   lower bound : 0.000, p = <2e-16
##   upper bound : 1.000, p = 0.45
##   95.0% CI    : (0.970, NA)
## delta  [Fix]  : 1.000
##
## Coefficients:
##                                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)                        2.2300     0.8230    2.71  0.0073
## X40k_M_oxy                         0.2871     0.2616    1.10  0.2737
## X40k_slope_oxy                     -0.0629     0.0424   -1.48  0.1398
## X40k_SD_oxy                       -0.1017     2.9128   -0.03  0.9722
## X40k_M_oxy:X40k_slope_oxy          0.0263     0.0178    1.47  0.1423
## X40k_M_oxy:X40k_SD_oxy             -0.0798     1.0759   -0.07  0.9409
## X40k_slope_oxy:X40k_SD_oxy         0.0733     0.1032    0.71  0.4778
## X40k_M_oxy:X40k_slope_oxy:X40k_SD_oxy -0.0307     0.0364   -0.85  0.3989
##
## (Intercept)                        **
## X40k_M_oxy
## X40k_slope_oxy
## X40k_SD_oxy
## X40k_M_oxy:X40k_slope_oxy
## X40k_M_oxy:X40k_SD_oxy
## X40k_slope_oxy:X40k_SD_oxy
## X40k_M_oxy:X40k_slope_oxy:X40k_SD_oxy
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.162 on 220 degrees of freedom
## Multiple R-squared: 0.0341, Adjusted R-squared: 0.00336
## F-statistic: 1.11 on 7 and 220 DF, p-value: 0.358
```

40ka summary

- full Model
 - overall P value = 0.3581
 - ML value for lambda = 0.9939
 - adjusted R^2 = 0.0034
- sparse Model
 - overall P value for sparse model = 0.1448
 - ML value for lambda sparse model = 0.9949
 - adjusted R^2 = 0.0107