Predicting Stock Prices Using Long Short-Term Memory (LSTM) and Gated Recurrent Units (GRUs)

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Abstract

Accurate predictions of stock prices can result in large financial gain. The goal of this paper was to make S&P 500 stock price predictions using two deep learning methods, namely, Long Short-Term Memories (LSTMs) and Gated Recurrent Units (GRUs). Predictions were also made using a linear time series model and results were compared to our deep learning models. We opted to evaluate our model's performances using root mean square error (RMSE) which can be interpreted as the average difference between the models' predicted stock price to the actual stock price in USD. Test RMSE for the LSTM, GRU and linear time series models were 7.09, 5.97 and 24.93 respectively. Training times were 10.32, 8.3 and 0.002 seconds respectively. Training times significantly higher for the deep learning models which may pose an issue when dealing with larger amounts of data, however, the deep learning models appear to be significantly more accurate.

26 1 Introduction

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Accurate predictions of stock prices can result in large financial gain. During times of recession, individuals or companies may be motivated to make more informed investing decision. Overall, the goal is to buy stocks at a low price and then later sell them at a higher price than which you bought them. The challenge lies in knowing whether you should buy a particular stock and when the right time to sell it is.

For example, if you knew that a given stock's price was going to rise, you would buy that stock knowing that its value was about to increase. Likewise, if you knew a stock's price was about to fall, you may decide to sell that stock before it loses its value. Knowing for certain whether a stock's price will rise, or fall is unfortunately not possible but, given the profit that there is to be made with even just relatively accurate predictions, stock market forecasting has been a major research topic in the financial area.

47 2 Related Work

Traditionally, linear models were used for stock forecasting, however, stock price behaviour over time is noisy and non-linear (Grudnitski & Osburn, 1993) and therefore, linear models do not have the capabilities to follow their trends. Abhyankar et al. (1997) suggested applying non-linear methods to obtain more accurate predictions and with advancements in the field of machine learning, applying these non-linear methods have been possible for quite some time.

Donaldson and Kamstra (1996) applied neural networks to stock market forecasting and found that they outperformed the traditional linear models. More recent studies have found that deep learning-based methods tend to outperform non-deep learning-based methods in stock price prediction (Hu et al., 2021) (Nikou et al., 2019). As a result, research as a of late has looked to deep learning to provide state of the art stock price predictions. Some studies have found success in using convolutional neural networks (CNN) to predict stock prices (Chen et al., 2016) (Tsantekidis

70 et al., 2017). As stock data can be seen as 71 sequential, recurrent neural networks (RNN) have 72 been a popular deep learning method of choice for 73 stock price prediction. Long Short-Term Memory 74 (LSTM) is a special type of RNN which allows for 75 the learning of long-term dependencies. LSTMs 76 have also seen success in stock price prediction due 77 to their ability to make predictions based off long 78 sequences of previous inputs (Chen et al., 2015) 79 (Nelson et al., 2017).

80 3 Data

The dataset we used contains five years' worth of
Apple stock data and was retrieved from Kaggle
(Nugent, 2018). The dataset contains 1,259 rows
and seven variables. Each row refers to stock
data for a particular day. Variable descriptions
are detailed in table 1 below (note that all prices
are in USD). Note, there are 252 trading days in
a year.

Date	In format: yy-mm-dd		
Open	Price of the stock at		
	market open		
High	Highest price reached		
	in the day		
Low	Lowest price reached		
	in the day		
Close	Price of stock at		
	market close		
Volume	Number of shares		
	traded		
Name	Stock ticker's name		

Table 1. Variable Description

	open	high	low	close	volume
count	1259	1259	1259	1259	1259
mean	109.05	109.95	108.14	109.06	54047899.7
std	30.54	30.68	30.37	30.55	33468353.3
min	55.42	57.08	55.01	55.79	11475922
25%	84.64	85.33	84.25	84.83	29694376.5
50%	108.97	110.03	108.05	109.01	45668931
75%	127.33	128.1	126.29	127.12	68708720
max	179.37	180.1	178.25	179.26	266833581

Table 2. Descriptive Statistics

4 Methods

93 We opted to train two specialized types of 94 Recurrent Neural Networks (RNNs), namely, a 95 Long Short-Term Memory (LSTM) network and 96 Gated Recurrent Unit (GRU) network to predict 97 the highest price reached in each day. RNNs 98 work with sequence data to use past elements of 99 a given sequence (or past inputs) to predict the 100 next element of that sequence (i.e., the output) 101 (Bengio, Simard, & Frasconi, 1994). RNNs pass both the input at a given time step and the hidden 103 state from the previous time step/element of the 104 sequence through an activation layer to obtain a 105 new hidden state. At the last time step, a final 106 hidden state is calculated (using information from both the input at that time step as well as all 108 previous hidden states) and used to compute an 109 output.

As the number of time steps increases, 110 traditional RNNs fail to use information held in the earlier time steps in the computation of an output due to the vanishing gradient problem 114 (Gers, 1999). This is where the signal (gradient) sent to update the weight at a given layer during 116 back propagation decreases across layers. These small gradient values essentially prevent the 118 weight from being updated. To solve this problem, Schmidhuber and Hochreiter (1997) 120 introduced LSTMs. LSTMs use a gating mechanism to control the flow of information. At a given time step in RNNs, the network receives information from the current input and the previous time step's hidden state. At a given time step in LSTMs, the network receives information 126 from the current input as well as the previous 127 time step's short-term memory and long-term memory. An input gate decides what information should be stored in the long-term memory. A 130 forget gate decides what information should be discarded from the long-term memory and an output gate produces a new short term memory.

GRUs were introduced by Cho et al. (2014) and are similar to LSTMs except that they have two gates. An update gate decides how much previous information should be passed on to the next state and a reset gate decides how much previous information can be disregarded. A major benefit of this alternative gating mechanism is that there is less computational

141 cost resulting in faster processing times (Yang et al., 2020). 175 more complex deep learning models. As 176 expected, training time for the GRU was

43 5 Experiment

we performed traditional linear regression using time steps as the sole predictor with an 80/20 train/test split. This was done in order to have a control group to compare the results of the LSTM and GRU against. The PyTorch framework was used to train and test the LSTM and GRU models. Data was normalized and the sliding window method was used to create all possible sequences of a given length in the data. The data was split into training and testing (the 80/20 was used again). The training and testing data were transformed into tensors. The hyper parameter values that were used for both models can be seen below.

Input dimension = 1

Hidden dimension = 32

Number of layers = 2

Output dimension = 1

Number of epochs = 100

Both models used the adam optimizer and Mean Squared Error (MSE) loss function. All models were evaluated using Root Mean Square Frror (RMSE).

167 6 Results

	Linear Regression	LSTM	GRU
Train RMSE	13.93	2.14	1.37
Test RMSE	24.93	7.09	5.97
Training	0.002s	10.32s	8.30s
Time			

Table 3. Comparison of RMSE and Training Time Among Models

168 As seen in table 3 above, the GRU and LSTM far 169 outperformed the linear regression model based 170 off both train and test RMSE values. The linear 171 regression model took far less time to train 172 however this won't matter in cases like this 173 whereby the amount of data does not impose 174 heavy computational cost, even when training

more complex deep learning models. As expected, training time for the GRU was lower than the LSTM. Again, this was not an issue for this experiment given the size of the data but would be important to consider should one want to train an LSTM or GRU on large amounts of data. Figures 1, 2 and 3 below provide a visual aid on how well the models predicted the stock prices.

Results (Linear Regression)



Figure 1. Linear Regression Predictions vs. Actuals



Figure 2. LSTM Predictions vs. Actuals



Figure 3. GRU Predictions vs. Actuals

The above figures clearly illustrate the LSTM and GRU's superior predictive ability as is evident by the orange test prediction lines versus the green actual values. What is also interesting to see is that the GRU's test predictions better picked up on the non-linear behaviour of the stock price compared to the

194 LSTM. While their test RMSE were similar, this 195 may point to the GRU being a better model of 196 choice when predicting stock price.

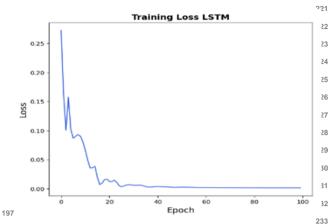


Figure 4. LSTM Training Loss Across Epochs

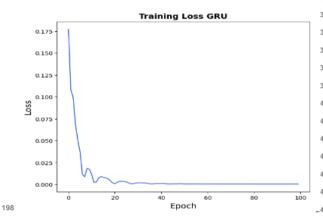


Figure 5. GRU Training Loss Across Epochs

Figures 4 and 5 respectively show that the default 100 epochs were not necessary as model convergence occurred after approximately thirty 202 to forty epochs.

Conclusion 7

204 GRU outperformed LSTM in terms of time 254 Data Processing – Barbara Schmitz and Conor 205 complexity and loss as well as captured nuances in 255 Dempsey 206 data better. However, both GRU and LSTM 256 Mid Term Write Up – Conor Dempsey outperformed using a traditional linear regression ²⁵⁷ Poster – Barbara Schmitz for forecasting. The GRU model is more sensitive to noise than the LSTM, and thus, captures the volatility more accurately than the LSTM model. 211 The LSTM model's prediction of stock behavior 212 tended to smooth out the noise. In this economic 213 domain, we did not want a smoothed trend. Instead, 214 a model that can capture market volatility is much 262 $_{215}$ better in this context. For the deep learning models, $_{263}$ 216 thirty to forty epochs were sufficient to train the 264 217 data.

For future improvements, now that we 219 know the data is sufficiently trained at thirty to 220 forty epochs and does not need the full 100, we 221 could include a validation set for the data and train the LSTM and GRU models at forty epochs. In addition, more data could have used more years of 24 data and more stocks added into the mix to evaluate 25 the whole of the S&P 500 portfolio. However, we were intentional in choosing five years (2013-27 2018) as they were not recession or COVID-28 afflicted years. There is opportunity to experiment 29 with different hyper parameters such as the input 30 dimensions, hidden dimensions, number of layers, a different optimizer, etc.

One of the drawbacks with deep learning 233 methods, however, is that it is not intuitive which parameters to initialize the architecture with. This 35 rings particularly true when the user has little to no domain knowledge or is not a subject matter expert.

Despite the training times for these models being relatively low, for a more robust analysis and data, this would have benefitted from a CUDA enabled GPU or using Google Colab to achieve the same goal.

To take this experiment even further, this could 43 be a robust analysis of three traditional forecasting models versus three deep learning forecasting models. The three traditional models could include ₄₆ the linear regression, moving day average, and a 247 statistically advanced model i.e., the ARIMA The three deep learning forecasting 248 model. 249 methods could include the LSTM and GRU models 250 along with the newer and rising in popularity 251 architecture, the transformer model.

Contributions 252 8

253 Data Collection – Barbara Schmitz

258 Final Report Write Up - Barbara Schmitz and 259 Conor Dempsey

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