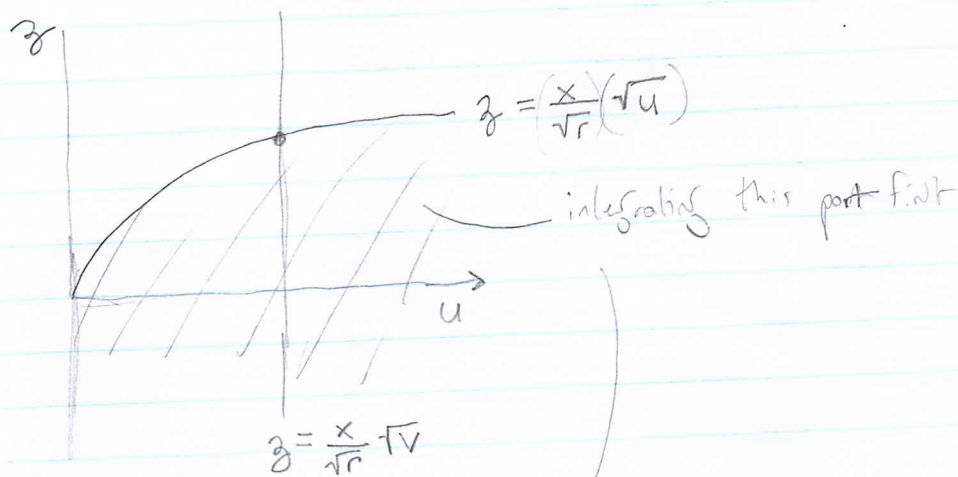


For any $x \in (-\infty, \infty)$,

$$P[T \leq x] = P\left[\left(\frac{Z}{\sqrt{V/r}}\right) \leq x\right] = P\left[Z \leq (\sqrt{V/r})x\right]$$



$$= \iint_{\Delta} g(z, u) dz du$$

$$= \int_0^{\infty} \int_{-\infty}^{\left(\frac{x}{\sqrt{r}}\right)\sqrt{u}} \frac{1}{\sqrt{2\pi}} e^{-\frac{z^2}{2}} \frac{1}{\Gamma(\frac{r}{2}) 2^{r/2}} u^{\frac{(r-1)}{2}-1} e^{-\frac{u}{2}} dz du$$

$$= \int_0^{\infty} \frac{1}{\sqrt{\pi} \Gamma(\frac{r}{2})} \left[\int_{-\infty}^{\frac{x}{\sqrt{r}}\sqrt{u}} e^{-\frac{z^2}{2}} dz \right] \frac{1}{2^{\frac{(r-1)}{2}}} u^{\frac{(r-1)}{2}-1} e^{-\frac{u}{2}} du$$

And we differentiate w.r.t. x to get

$$f(x) = \frac{1}{\sqrt{\pi} \Gamma(\frac{r}{2})} \int_0^{\infty} \left[e^{-\frac{(\frac{x}{\sqrt{r}}\sqrt{u})^2}{2}} \frac{\sqrt{u}}{\sqrt{r}} \right] \frac{1}{2^{\frac{(r-1)}{2}}} u^{\frac{(r-1)}{2}-1} e^{-\frac{u}{2}} du$$

$$f(x) = \frac{1}{\sqrt{\pi} \Gamma(\frac{r}{2})} \int_0^{\infty} \left[e^{-\frac{(\frac{x}{\sqrt{r}}\sqrt{u})^2}{2}} \frac{\sqrt{u}}{\sqrt{r}} \right] \frac{1}{2^{\frac{(r-1)}{2}}} u^{\frac{(r-1)}{2}-1} e^{-\frac{u}{2}} du$$