### ENGG1003 - Friday Week 1

Algorithms and Pseudocode

Brenton Schulz

University of Newcastle

February 27, 2019



#### Algorithms

- Informally, an algorithm is a series of steps which accomplishes a task
- More accurately, the steps (instructions) must:
  - Have a strict order
  - Be unambiguous
  - Be executable
- "Executable" means that the target platform is capable of performing that task.
  - eg: An industrial welding robot can execute "move welding tip 1 cm left". A mobile phone can't.



#### Algorithms

- An algorithm exists purely as an abstract concept until it is communicated
- ► We will use:
  - Pseudocode to communicate algorithms to ourselves and other people
  - The languages C and MATLAB to communicate algorithms to computers
- Pseudocode can be very formal, but as engineers we will only use formal rules if required
  - eg: When documenting algorithms for other people
  - Your own "working out" can be anything that helps you



#### Algorithm Example 1

**Example 1:** Algorithm given to mum to start my car (2015 Tarago)

**Result:** The vehicle's engine is idling

Initialisation: stand next to the vehicle, key fob in hand

- 1. Depress the unlock button on the key fob, car will beep twice
- 2. Place key fob in your pocket
- 3. Enter the vehicle, sit in the driver's seat
- 4. Ensure that the gear selector has P engaged
- 5. Depress the brake pedal
- 6. Observe that the green LED is lit on the engine start button
- 7. Press the engine start button
- 8. If engine is not idling
  - Call me



#### **Example Discussion**

- Algorithms typically need to feel over-explained
  - Computers are really stupid; get in the habit of over-thinking everything
- The algorithm contained flow control in the form of an "if" statement
  - ► The final step ("call me") was *conditional* on the car not starting
- We will discuss logical statements later, but first...



#### Algorithm Example 2

A wife asks her husband, a programmer, "Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?

A short time later the husband comes back with 6 cartons of milk and his wife asks, "Why did you buy 6 cartons of milk?

He replies, They had eggs.

#### Algorithm Example 2a

Lets make this more realistic.

A wife asks her robot helper, "Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?

The robot replies: "Unknown instruction: 'get 6'."

#### Code Blocks

- ► A *block* is a set of instructions which are, for some reason, grouped together
- ▶ If a single condition controls multiple instructions they can go together in a block

#### **Conditions**

- Computers don't understand "maybe"
- A condition must be absolutely true or false
- Human examples:
  - ▶ I am within the boundary of the Callaghan campus
  - I am alive
  - My net worth is below AU\$100M
- Computer examples:
  - i is less than 184
  - x plus y is not equal to zero
  - Input data has been given to the program
  - A division by zero occurred



#### IF ... ENDIF and IF ... ELSEIF

# Algorithm Example 3 - Quadratic Root Finding

From high school you should know that the equation

$$ax^2 + bx + c = 0 \tag{1}$$

has solutions given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \tag{2}$$

lets write an algorithm which provides real valued solutions to a quadratic equation.

# Algorithm Example 3 - Quadratic Root Finding

**Input:** Real numbers a, b, and c **Output:** Three numbers:

- 1. The number of solutions, N
- 2. One of the roots,  $x_1$
- 3. The other root,  $x_2$

#### **Behaviour:**

- ▶ If N is 2 then  $x_1$  and  $x_2$  are different real numbers
- ▶ If N is 1 then  $x_1$  is the unique solution and  $x_2$  is undefined
- ▶ If N is 0 then  $x_1$  and  $x_2$  are undefined



## Algorithm Example 3 - Quadratic Root Finding

```
BEGIN
 D = b^2 - 4ac
 TF D < 0
   N = 0
 FLSE IF D=0
   N=1
   x_1 = \frac{-b}{2a}
 ELSE IF D > 0
   N=2
   x_1 = \frac{-b + \sqrt{D}}{2a}
   x_2 = \frac{-b - \sqrt{D}}{2}
 ENDIF
```

- Reasonably formal pseudocode
- The IF ... ELSE IF flow control construct forces exclusive execution of only one block
- The first condition that is true causes execution of that block
- Subsequent blocks ignored
- Contains 3 conditions



END

#### Boolean Algebra Basics

- What if we want more complicated conditions? Boolean algebra is needed!
- Boolean algebra (or Boolean logic) is a field of mathematics which evaluates combinations of logical variables as either true or false
- Boolean variables can only take the values true (or 1) or false (or 0)
- Boolean algebra defines three operators:
  - ► OR
  - AND
  - ► NOT



#### Boolean Algebra Basics

- Boolean variables can be allocated any symbols (just like in "normal" algebra)
  - ► Typically get upper-case letters
  - ightharpoonup eg: X = A OR B
- Various symbols can be used for OR/AND/NOT, we will only use the words here
  - Write them in capitals to remove ambiguity
  - C and MATLAB have their own symbols for Boolean algebra
  - Other courses (eg: ELE17100) will use different symbols again



#### **Boolean Operators**

- An operand is a value on which a mathematical operation takes place
  - ightharpoonup eg: In "1 + 2" the 1 and 2 are operands and + is the operator
- OR Evaluates true if either operand is true
  - $\triangleright$  X = A OR B
  - X is true if A or B is true
- AND- Evaluates true only when both operands are true
  - $\triangleright$  X = A AND B
  - X is true only if both A and B is true



#### **Boolean Operators**

- Observe that OR and AND are binary operators
  - They operate on two operands
  - From Latin "bini" meaning "two together"
- The NOT operator is unitary
  - ie: it only operates on one operand
  - NB: The operand could be a single variable or complex expression
- NOT performs a logical inversion
  - ▶ NOT true = false
  - ► NOT false = true



#### Boolean Condition Examples

- My car needs a service if, since the last service, (more than 6 months has past) OR (more than 15000km have been travelled)
- ➤ You will pass this course if (you score 40% or more in the final exam) AND (the weighted sum of all assessments is more than 50%)
- ➤ A computer program repeats an algorithm if (there is still data to process) AND (errors have not occurred) AND (NOT (the user has terminated the program))



### Algorithm Example 4 - Boolean Conditions

**Problem:** How can trigonometric functions be calculated by a computer?

One Solution: Series expansion! (Seen in MATH1120).

The function cos(x) can be evaluated with arithmetic as:

$$\cos(x) = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} = \frac{-x^2}{2!} + \frac{x^4}{4!} + \frac{-x^6}{6!} + \frac{x^8}{8!} \dots$$
 (3)

Evaluation of this series needs two things:

- 1. The *loop* flow control concept
- 2. Some kind of stop condition



### Algorithm Example 4 - Boolean Conditions

- Computers can't count to infinity, we need to know when to stop
- ightharpoonup Computers have limited precision, around  $10^{-16}$  is typical
- ▶ Observe that as k increases in Equation 4 the denominator increases really fast (4!=24, 10!=3628800)
- ► This implies that the value of  $\frac{(-1)^k x^{2k}}{(2k)}!$  tends to drop as k increases
- ► Therefore, we can add terms until they are "too small"
- ▶ A maximum value of k can also be specified for safety

$$\cos(x) = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} \tag{4}$$



#### Loops

- ➤ A loop causes an algorithm to execute a given block of instruction multiple times
- Loops typically require an exit condition
  - Without an exit condition they are called infinite loops
    - Yes, these have a purpose
- Multiple types of loops
  - WHILE condition...ENDWHILE
  - ▶ DO...WHILE condition
  - ► FOR counter FROM 1 TO something



### Algorithm Example 4 - Boolean Conditions

```
BEGIN tmp = 1
k = 0
WHILE (k<10) AND (tmp>1e-6) tmp = \frac{(-1)^k x^{2k}}{(2k)!}
x = x + tmp
k = k + 1
ENDWHILE
```

- The while loop repeats a block of steps until the condition becomes false
- We loop until 10 iterations have occurred OR a precision limit is reached

END

#### Loop Details

WHILE condition tested before "entering" loop Tested before every repeat Variables in the condition should change inside the loop

#### DO ... WHILE

Same as WHILE except executes at least once

#### FOR Loops

Used when the number of loop repeats is known before entering the loop