ENGG1003 - Monday Week 6
Interpolation, Assignment 1 and Mid-term quiz

Steve Weller

University of Newcastle

29 March 2021

Last compiled: March 29, 2021 12:06pm +11:00

Lecture overview

1. Interpolation

2. Assignment 1

3. Mid-term quiz

The story so far

- variables and data types
- arrays (using `numpy`)
- plotting (using `matplotlib`)
- flow control
  - ▶ `if`
  - ▶ `while`
  - ▶ `for`
- functions

Most of ENGG1003 from here uses these elements of Python to solve Engineering problems

1) Interpolation

Two common forms of *curve-fitting* in Engineering applications:
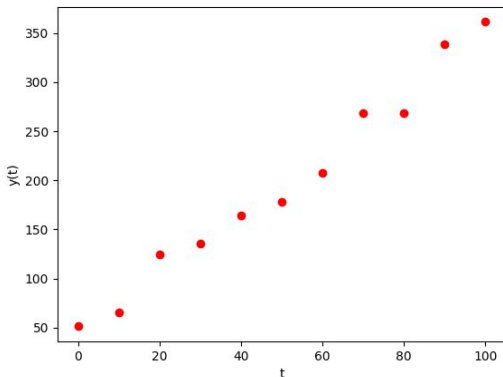
1. *interpolation*
   - ▶ today's lecture

2. *regression*
   - ▶ considered in detail later in ENGG1003

- we now demonstrate both curve-fitting methods applied to the same dataset
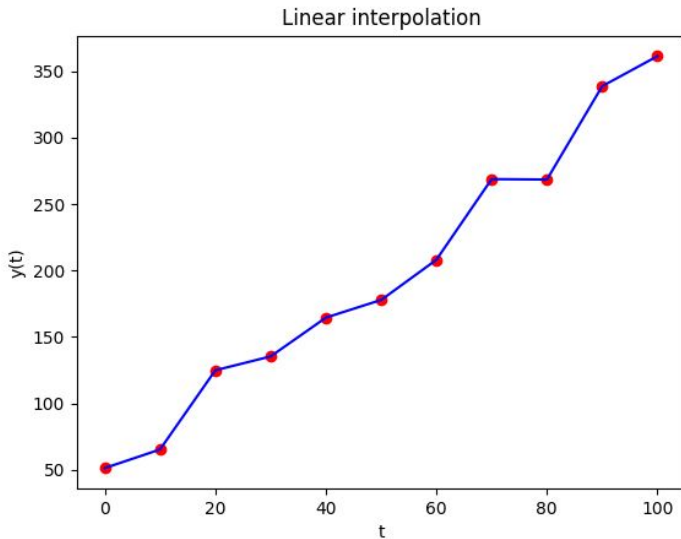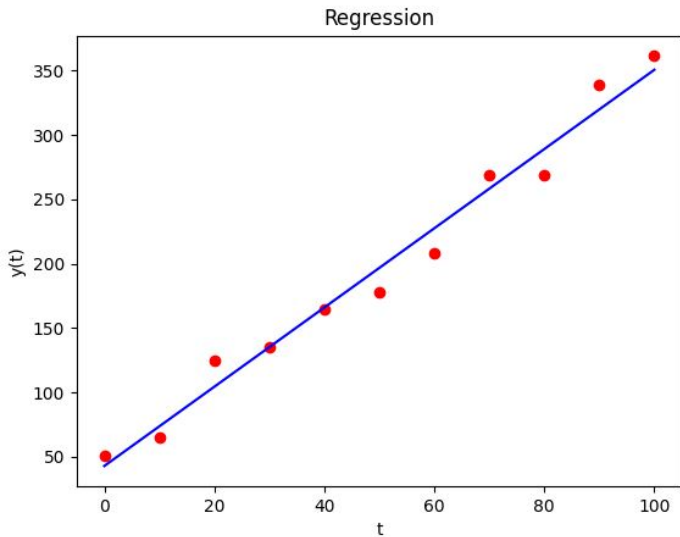
Curve-fitting dataset

`Week6Monday.py`

- 11 pairs of data points $(t_i, y_i), i = 0, 1, 2, \ldots, 10$
  $(0, 51.29), (10, 65.24), (20, 124.89), \ldots, (100, 361.32)$

Interpolation

Linear interpolation

Regression

Interpolation vs. regression

- **interpolation:** joining the dots
  - ▶ obtain value of y at some intermediate point

- **regression:** fitting a straight line
  - ▶ when there's "too much data", simplify
  - ▶ here, simplifying to a straight line
  - ▶ we return to choosing "best" straight line later in ENGG1003
  - ▶ no more regression in this lecture

- both interpolation & regression involve creating a function (blue line) from data (red dots)
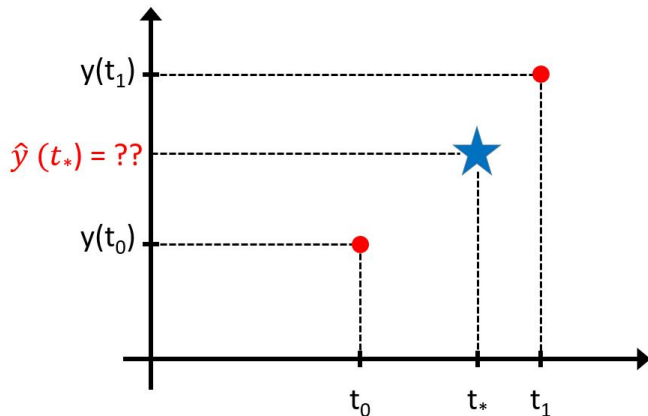
Functions

- in maths, you've seen functions written as follows:

$$y = f(t)$$

- function f, takes *argument* t and returns a *value* which is assigned to y

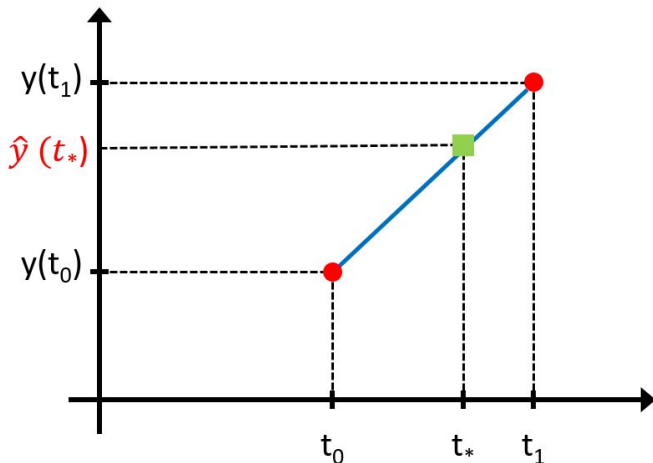- ...and last week we saw Python uses the same terminology with functions

The interpolation problem

Given: data points $(t_0, y(t_0))$ & $(t_1, y(t_1))$ and $t_\star$
Calculate: interpolated value $\hat{y}(t_\star)$

Linear interpolation

- interpolated value $\hat{y}(t_\star)$ lies on straight line connecting $(t_0, y(t_0))$ & $(t_1, y(t_1))$

Linear interpolation using `interp1d`

- `interp1d` function from `scipy.interpolate`
  - ▶ `pip install scipy` at terminal before using `scipy` for the first time

- `t` and `y` are arrays of values used to approximate some function: $y = f(t)$

```
f = interp1d(t, y)
```

- call to `interp1d` returns a function
  - ▶ first time we've seen a *function* returned by a function
- live demo

Linear interpolation in Python

Week6MonLinear.py

```python
import numpy as np
import matplotlib.pyplot as plt
from scipy.interpolate import interp1d

# seed random number generator to reproduce lecture results
np.random.seed(27101967)

N = 11
t = np.linspace(0,100,N)               # 0,10,20,...,100
tnew = np.linspace(0,100,100*N)        # 0,0.1,0.2,...,100
n = np.random.uniform(-25,25,N)        # noise on linear function

m = 3                                  # gradient
b = 50                                 # intercept
y = m*t + b + n                        # dataset is straight line + noise
```

Linear interpolation in Python (ctd.)

```python
1  # INTERPOLATION
2  f = interp1d(t, y)
3
4  # PLOT RESULTS
5  plt.plot(t, y, 'ro')
6  plt.xlabel('t')
7  plt.ylabel('y(t)')
8  plt.plot(tnew, f(tnew), 'b')
9  plt.title('Linear interpolation')
10 plt.show()
```

- **line 2:** create function f to interpolate data in arrays t and y
- **line 8:** use function f using "high resolution" time data in array tnew

Linear interpolation

Linear interpolation
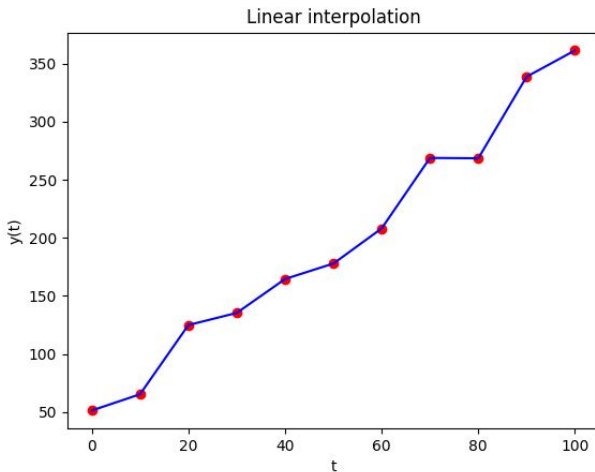
- "stitches together" straight line segments

Beyond linear interpolation: Cubic splines

Problem: slopes of adjacent straight lines change abruptly at data points

- *could* solve by stitching together quadratic polynomials (parabolas) between consecutive point pairs
  - ▶ adjacent parabolas pass through data points
  - ▶ *and also have slopes that match at data points*

- very common to use degree-3 polynomials (cubics) instead of degree-2 parabolas
  - ▶ even smoother fit to data
  - ▶ *cubic splines very popular in computer graphics*

Cubic spline in Python code

```python
1  # INTERPOLATION
2  f3 = interp1d(t, y, 'cubic')
3
4  # PLOT RESULTS
5  plt.plot(t, y, 'ro')
6  plt.xlabel('t')
7  plt.ylabel('y(t)')
8  plt.plot(tnew, f3(tnew), 'b')
9  plt.title('Cubic spline interpolation')
10 plt.show()
```
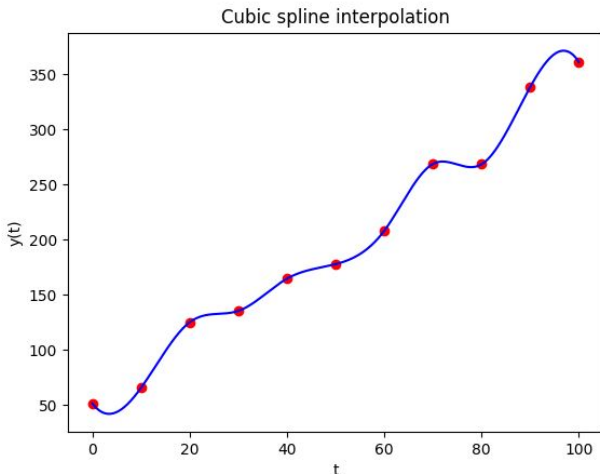
Linear interpolation:

```python
1  f = interp1d(t, y)
```

Cubic spline interpolation:

```python
1  f3 = interp1d(t, y, 'cubic')
```

- Live demo of `Week6MonCubic.py`

Cubic spline interpolation

Cubic spline interpolation

- "stitches together" *cubic* polynomials

2) Assignment 1

- released today, Monday 29 March 2021

- upload Python file to BB no later than 9:00 am, Monday 19 April

- counts for 20% of course grade

- each student will be assessed by demonstrator in week 7 face-face computer lab (after recess)

2) Assignment 1

- assignment topic: analysis of GPS data

- in more detail:
  - ▶ GPS data collected during a mountain bike ride
  - ▶ GPS track log is presented in a $\mathtt{csv}$ file containing timestamps, latitude, longitude, and elevation columns recorded at 1 second intervals
  - ▶ project asks you to analyse GPS data, eg: fitness tracker
  - ▶ use interpolation where GPS signal was lost

- computer labs this week:
  - ▶ there is no week 6 lab sheet
  - ▶ get started on assignment in place of lab sheet

3) Mid-term quiz

- Thursday 1 April, 4–5 pm
  - ▶ during scheduled lecture time
  - ▶ mid-term quiz instead of lecture this week so. . .
  - ▶ **NO Zoom or YouTube livestream on 1 April**

- 50-minute quiz

- open-book

- quiz will appear on BB at 4:05 pm
  . . . and will disappear at 4:55 pm

- counts for 15% of course grade

What to expect, and how to prepare

- the quiz will ask you to write Python code to:
  - ▶ load a `csv` file
  - ▶ perform some calculations on a specified column of the file ie: array processing
    (each student gets assigned a unique column in the file)
- once your program is complete, you do two things:
  1. enter the results of your program into BB
  2. upload your Python code to BB

- **there is a practice quiz NOW on BB**
  - ▶ you can practice as many times as you like!
- live demo of how the mid-term quiz will run

Lecture summary

- Interpolation
  - ▶ linear interpolation
    - straight line "join the dots"
  - ▶ cubic spline interpolation
    - smoothly connects data points

- Assignment 1
  - ▶ released today
  - ▶ submissions due on BB by 9:00 am, Monday 19 April
  - ▶ worth 20%

- Mid-term quiz
  - ▶ **there is a practice quiz NOW on BB**
  - ▶ done on BB at 4:00 pm, Thursday 1 April
  - ▶ worth 15%