# ENGG1003 - Lab Week 5

Brenton Schulz

# 1 Introduction

Project: ENGG1003 - Lab Week 5, March 28, 2019

These lab tasks include some reasonably non-trivial mathematics. I have received feedback from both demonstrators and students that the mathematics so far has, for some, been difficult to follow. Unfortunately, I can't do much about this. Engineering is *very* mathematics heavy. You can't get away from it. The mathematics in 2nd year only gets *much* more advanced.

If you find the mathematics here difficult to understand please take some time to learn it in your own time. You can ask the ENGG1003 PASS leader for help and there are PASS sessions for MATH1110 (or MATH1002) you can attend. You can also ask ENGG1003 demonstrators or your MATH\* tutors and lecturers for help.

The 2019 PASS timetable can be found here.

I (Brenton) speak from bitter personal experience here. If you do not finish 1st year with solid foundational knowledge in mathematics you will have immense struggles continuing. In the mid-2000s I failed *over half* of my 2nd year subjects the first time through engineering for this reason.

If mathematical understanding is getting in the way of learning programming I strongly recommend that you attempt the Sieve of Eratosthenes task as a priority. It only requires basic arithmetic but the algorithm is non-trivial to implement.

Page 1 of 20 Brenton Schulz

# 2 New Content

## 2.1 Functions

A C function is a block of code which can be called from anywhere in your program. A C function is defined by:

- A unique name
  - The name must be unique among all functions within your program, the libraries which are #include'ed, and variables within the scope of where the function is called
- Zero or more *arguments*. Each argument is separated by a comma, has a fixed data type, and name unique to that function's scope
  - eg: (float x, int num, char a)
  - Functions which don't take arguments must list void in place of arguments in their prototype and definition
- A return value data type
  - Functions with no return value have a return data type of void

A function prototype summarises the above information with the syntax:

```
return_datatype function_name(arguments);
```

for example, the sin() function in the mathematics library returns a double and accepts a single double as an argument. It therefore has the following prototype:

```
double sin(double x);
```

A function definition is a repeat of the function prototype followed by the code which gets executed when the function is called.

A function body is just the code which gets executed. It is a subset of the function definition.

Example: the following code listing includes a function called printResult which takes a single float argument and prints a human-readable message including that number:

```
#include <stdio.h>
 // This line is the function prototype
 // "float x" indicates that it takes a single argument of type float.
 // The return type is void because it does not return a value
6 void printResult(float x);
 int main() {
    float a = 2.0;
    printResult(a); // Test the function by calling it
12
13
 // The lines below are the function definition
void printResult(float x) {
     // This printf() statement is the only code in the function body
     // The argument "x" is a pre-initialised variable within this scope
    printf("The final calculation result was: f^n, x);
19
```

## 2.2 Static Variables

A static variable is one which retains its value between function calls. Normally, all variables declared in functions (including arguments) are lost when the function returns. Any variable declared in a function with the static keyword is kept safe and retains its value between function calls.

For example, the following code prints the numbers 1 to 5 because, within the definition of counter(), x is declared with the static keyword:

```
#include <stdio.h>
  // Takes no arguments, so void argument list
 // Returns an int equal to the number of times it has been called
5 int counter(void);
  int main() {
     // Call 5 times just to test its operation
     printf("%d\n", counter() );
    printf("%d\n", counter() );
     printf("%d\n", counter() );
    printf("%d\n", counter() );
12
     printf("%d\n", counter() );
13
14 }
16 // Takes no arguments, so void argument list
_{
m 17} // Returns an int equal to the number of times it has been called
int counter(void) {
     // Declaration of x initialises it to zero on first call only
19
     static int x = 0;
     // Increment x. Initialisation is only done once
21
    x = x + 1;
    return x;
```

# 2.3 Arrays

An array is a collection of variables, all of the same type, arranged in a long list and accessed with an array index. In C, an array is declared with a fixed length, data type, and name with the following syntax:

```
data_type name[size];
```

The data type can be any of the standard C types seen so far (char, int, unsigned long, float, etc). The name must be unique among all variables within its scope. Arrays may be initialised when declared with the following syntax:

```
data_type array_name[] = \{1, 2, 3, 4, 5, 6\};
```

If the above syntax is used the array size (inside the []'s) is calculated from the initialisation and doesn't need to be explicitly listed.

The size must be an integer but does not need to be known at compile time. For example, the following code snippet declares an array with a size given by the user at runtime:

```
int length;
printf("Enter an array length: ");
scanf("%d", &length);

float numbers[length];
```

A single variable stored inside an array is known as an array *element*. Each element is accessed with a unique *index*. The index is an integer ranging from zero to length-1. Array elements are accessed with the following syntax:

```
arrayName[index]
```

Arrays can be used anywhere that other variables can and their index can be an integer variable or literal.

### Examples:

```
x = array[2]; // Simple arithmetic example y = 2.0*x[12] + y[0]; // Non-trivial arithmetic n[i] = sin(x); // As lvalues (NB: array can't be declared "const") printf("%f\n", nums[12]); // As an argument to a function
```

## 2.4 switch-case Statements

A switch-case statement is a flow control construct which provides a neat way to choose one of multiple options. It replaces a long string of if()-else-if() statements.

The following two code blocks are equivalent:

```
switch(x) {
if(x == 0) {
                                            case 0: // stuff
  // stuff
} else if(x == 1) {
                                               break;
  // stuff
                                            case 1: // stuff
} else if(x == 2) {
                                               break;
  // stuff
                                            case 2: // stuff
} else if(x == 3) {
                                               break;
  //stuff
                                            case 3: // stuff
} else {
                                               break;
  // If nothing else matches, do this
                                            default: // If nothing else matches, do this
```

## Notes:

- x must be an **integer** data type (int, char, unsigned long, etc)
- The break statements are optional
- The program execution will jump from the switch () line to the first matching case line and continue from there
- If a break is not found the program will continue to execute other case's listed below the matching one
- The default case is jumped to if none of the other cases match

# 3 Tasks

## Task 1: (Simple Function): Arithmetic

Project: ENGG1003 - Lab Week 5, March 28, 2019

Write a C function, arithmetic () which takes two float arguments, a and b, and returns their sum.

Sub-tasks:

- 1. Write the function prototype.
- 2. Write the function definition.
- 3. Place the prototype and definition inside the test code below. It includes test variables x and y, declared within main(). Compile, run, and compare your program's output with a manual calculation of x + y:

```
#include <stdio.h>

// Place prototype here

int main() {
    float x = 1, y = 5;
    float result;

    result = arithmetic(x, y);
    printf("%f plus %f is %f\n", x, y, result);

// Place definition here

// Place definition here
```

#### Task 2: (Switch Statements): Arithmetic Function

Extend your function from the previous task to accept a third integer argument, operation. Use a switch() statement inside the function definition so that it exhibits the following behaviour:

- If operation is zero, return a+b
- If operation is one, return a-b
- If operation is two, return a\*b
- If operation is three, return a/b
- If operation is anything else, print an error message (eg: printf("Illegal operation %d", operation)) and return zero.

This task can be broken down into the following sub-tasks:

- 1. Modify the function prototype to include the third argument operation of type int
- 2. Modify the first line of the function definition to include the third argument
- 3. Draw the rest of the owl Write the switch statement which makes a choice between the four arithmetic operations based on the value of operation.

**NB:** You may write return at any point inside a function. As such, your switch() statement may either:

- (a) Allocate the arithmetic result to a temporary variable (of type float) followed by a break statement, return'ing the temporary variable at the end of the function, OR
- (b) have return statements inside the switch () statement, directly after each case.

## Task 3: (Arrays) Maximum Number Search

Write a C program which searches an array for its maximum (most positive) element. The data will be provided as an initialised array of type float. The program's output should include the maximum value and the array index at which it was found.

Your program should implement the following algorithm:

```
BEGIN
  float data[N]
  float maximum = -1e30 // Initialise to a large negative number
  float maxIndex
  FOR i = 0 to N-1 // C array indexing from 0 to N-1
    IF data[i] > maximum
      maximum = data[i]
      maxIndex = i
    ENDIF
  ENDFOR
  PRINT ("The maximum value was %f, found at index %d", maximum, maxIndex)
You may use this (very incomplete) template:
#include <stdio.h>
int main() {
   float data[] = \{1.2, 8.4, 10.8, -0.4, -8.234, 3.1\};
   // Declare other variables
   // Implement search
   // Print result
```

## Task 4: Functions: Prime Number Testing

Write a C function, isPrime () which tests if an integer argument is prime.

The return value and argument should both be int data types. If the argument is prime the function returns 1 and returns 0 otherwise.

For the purposes of this task you should perform a "brute force" search for any integer factor of the argument. ie: for an integer x test if it is divisible by all integers between 2 and x/2+1. If any factors are found the function should return zero.

**Revision:** An integer, x, is prime if it is not divisible by any other integer, k. In C, x is divisible by k if x + k = 0.

You may use the template below. It has the function prototype, function definition, and main() "test code" pre-written:

```
#include <stdio.h>

// Returns 1 if x is prime, zero otherwise
int isPrime(int x);

// main function for testing isPrime()

// Only modify if I made a mistake or you want to play around
int main() {
   int testNum;
   for(testNum = 0; testNum < 20; testNum++) {
      if(isPrime(testNum)) {
        printf("%d is prime\n", testNum);
      }
   }
   return 0;
}

// Returns 1 if x is prime, zero otherwise
// EDIT THIS BIT
int isPrime(int x) {
   return 0;
}</pre>
```

#### Task 5: (Arrays): Sieve of Eratosthenes

This task is mathematically simple but algorithmically complex. It is an excellent programming task if you find the mathematics of other tasks overwhelming.

The Sieve of Eratosthenes is an algorithm for generating prime numbers. The method is attributed to the ancient Greek scholar Eratosthenes of Cyrene (276-194 BC).

If implemented by hand, the algorithm requires the following steps:

- 1. Write a list of integers from 2 to some "large" number, N
- 2. Observe that 2 is prime and that any multiple of 2 would not be prime
- 3. Moving down the list, cross out every multiple of 2
- 4. Choosing the next highest number which is not crossed out, 3, move down the list and cross out every multiple of 3
- 5. Choosing the next highest number which is not crossed out, 5, move down the list and cross out every multiple of 5
- 6. Repeat until you reach the end of the list
- 7. All numbers which were not crossed out are prime

#### Example:

```
Listing integers from 2 to 16:
2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
```

```
Crossing out every multiple of 2:
2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
```

```
Crossing out every multiple of 3:
2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
```

Crossing out every multiple of 5 (ok, they're all crossed out by now already so we can stop):  $2\ 3\ 4\ 5\ 6\ 7\ 8\ 9\ 10\ 11\ 12\ 13\ 14\ 15\ 16$ 

All the numbers left over are prime: 2 3 5 7 11 13

**Task:** Write a C program which uses this method to find all prime numbers strictly less than 100.

Since we need to remember a "long" list of numbers (and whether or not they are "crossed out") this is a perfect application for an array.

To complete this task, declare an array of type char with 100 elements:

```
char numbers[100]; // Index ranges from 0 to 99
```

The list of indices (plural of index) will form the list of integers. The array elements (the numbers stored at each index) indicate whether that index has been "crossed out" or not.

The array includes indices 0 and 1 which are integers not considered by the original algorithm. Your code may either ignore them or treat them as special cases when printing the result (ie: have explicit if (index  $== 0 \mid \mid \text{index} == 1$ ) statements).

The array should be initialised to all 1's to indicate that, at the start of the algorithm, nothing has been crossed out. As elements are "crossed out" they should be set to zero.

Your program should implement the following pseudocode: BEGIN numbers[MAX+1] is an array of char's Set every element of numbers[] to 1 FOR index = 1, 2, 3, ..., MAX IF numbers[index] is 1 FOR j = 2\*index, 3\*index, 4\*index, ... MAX numbers[j] = 0**ENDFOR** ENDIF ENDFOR Print every index for which numbers[index] is 1 You may use the following template: #include <stdio.h> int main() { // Maximum integer to test. Declared constant // This is declared so that the maximum integer // can easily be changed const int MAX = 100;char numbers[MAX+1]; int index; int j; // Initialised numbers[] for(index = 0; index <= MAX; index++) {</pre> numbers[index] = 1;// DO THE SIEVE ALGORITHM HERE // for (index = 2; ...etc // Print results printf("The following numbers are prime:\n"); for(index = 2; index <= MAX; index++) {</pre> if(numbers[index] == 1) { printf("%d\n", index); } return 0; **HINT:** The inner FOR loop in the pseudocode can be implemented with the C for () statement: for  $(j = 2 \times index; j < MAX; j = j + index)$  { // Do stuff **Extension:** The Wikipedia article covering the Sieve of Eratosthenes describes several optimisations.

Implement the one which only crosses out index values starting at  $index^2$  (instead of  $2 \times index$ )

and the algorithm exit condition of not attempting to cross out values larger than  $\sqrt{MAX}$ .

#### Task 6: Arrays: Statistics Calculations

Write a C program which accepts a "large" number of real numbers and calculates their sample mean and sample variance.

**Revision:** From statistics, the *sample variance*,  $s^2$ , of N samples,  $X_1, X_2, ..., X_N$ , can be calculated as:

$$s^{2} = \frac{1}{N-1} \sum_{k=1}^{N} (X_{k} - mean(X))^{2}.$$
 (1)

There are  $\underline{\text{many algorithms}}$  for calculating a data set's variance. For this task you should implement the reasonably robust two-pass algorithm which calculates the sample mean and uses this value to calculate the variance as follows:

```
integer n = 0
float sum1 = 0
float sum2 = 0

FOR each data point Xn
    n = n + 1
    sum1 = sum1 + Xn

ENDFOR

mean = sum1 / n

FOR each data point Xn
    sum2 = sum2 + (Xn - mean) * (Xn - mean)
ENDFOR

variance = sum2 / (n-1)
```

Your program should "input" the data via an array initialisation. This is to avoid having to manually repeatedly type test data into scanf() while debugging.

You may use the following template:

```
#include <stdio.h>
int main() {
   // The mean of x[] is 5.000000
   // The variance of x[] is 7.500000
   // x[] has 9 elements
   float x[9] = \{1, 2, 3, 4, 5, 6, 7, 8, 9\};
   float variance, mean;
   float sum1 = 0, sum2 = 0;
   int n; // Counter variable
   // Calculate the sample mean (NB: we are assuming N=9)
   for (n = 0; n < 9; n++) {
      // Write your calculation here
   // Calculate the sample variance
   // Write your own for() loop
   printf("Mean: %f\nVariance: %f\n", mean, variance);
   return 0;
```

#### Task 7: Functions: Numerical Integration

**NB:** I belive the mathematics of this task is much more difficult to understand than the C implementation. Read the linked Wikipedia page and ask a demonstrator for an explanation if you don't follow it.

Write a C program which implements the following equation:

$$f(x) = e^{x^2}$$

as a C function and uses the trapezoidal rule to numerically calculate its integral between two given points:  $x_1$  and  $x_2$  (assume  $x_1 < x_2$ ). You should use the expf() function from the C maths library; be sure to #include <math.h>.

The function  $e^{x^2}$  is impossible to integrate by hand (ie: there is no "closed form" solution for  $\int e^{x^2} dx$ ) so we are *forced* to use numerical methods such as the trapezoidal rule (or Riemann integrals, Simpson's Rule, etc.) to evaluate it.

For the purposes of this task, the trapezoidal rule requires the interval,  $[x_1, x_2]$  to be broken up into several smaller "chunks" of trapezoidal shape. The area of each of these trapezoids is easy to calculate and sum together.

Graphical illustration of the method can be found on Wikipedia. This task implements the method described under numerical implementation on a uniform grid.

To implement this, your program needs a number, N, equal to the number of trapezoids the  $[x_1, x_2]$  interval is broken into. For this task, you may "hard code" a value of int N=5. You are encouraged to vary this value and observe how the accuracy of the result changes.

Given the interval,  $[x_1, x_2]$ , and trapezoid count, N, the horizontal width of each trapezoid,  $\Delta x$ , can be calculated as:

$$\Delta x = \frac{x_2 - x_1}{N}.\tag{2}$$

The integral of an arbitrary function, f(x), may then be calculated with the following equation:

$$\int_{T_{i}}^{x_{2}} f(x)dx = \Delta x \left( \frac{1}{2} f(x_{1}) + \sum_{k=1}^{N-1} f(x_{k}) + \frac{1}{2} f(x_{2}) \right)$$
 (3)

where  $x_1$  is given and the  $x_k$ 's inside the sum can be calculated as:

$$x_k = x_1 + k\Delta x$$
.

In your C program, evaluation of f(x) is simply written as f(x) so long as you have declared the variable float x; and have written a function with the prototype float f(f(x)).

The evaluation of  $\sum_{k=1}^{N-1} f(x_k)$  implies the use of a for () loop with the following form:

```
int N = 50;
int k; // Loop counter

float x1 = 0, x2 = 2;

float dx = (x2 - x1) / N;

// ... other code

float sum = 0;

for (k = 1; k < N; k++) {

    float x;
    x = x1 + k*dx;
    sum = sum + f(x)

}</pre>
```

With the values for x1 and x2 above the final answer should be  $\approx 16.4526$ .

#### Task 8: Functions: Numerical Differentiation

In pure mathematics, the following formula is used to differentiate the function f(x) at a point  $x_0$  from first principles:

$$\frac{df(x_0)}{dx} = \lim_{h \to 0} \left[ \frac{f(x_0 + h) - f(x_0)}{h} \right] \tag{4}$$

On a computer it is not possible to implement Equation (4) exactly because a division by zero causes numerical errors and is mathematically a little bit naughty.

Instead, we can *estimate* the differential (ie: gradient of  $f(x_0)$ ) by choosing a small, but non-zero, value for h and acknowledging that the answer is not exact. Thankfully engineering never requires exact values so the approximation can still be very useful.

Explicitly, we calculate an estimate for the gradient as:

$$\frac{df(x_0)}{dx} \approx \left\lceil \frac{f(x_0 + h) - f(x_0)}{h} \right\rceil \tag{5}$$

for a "small" but non-zero value of h.

**Task:** Write a C program which calculates the gradient of  $f(x) = x^2 + 2x - 1$  at a given point  $x_0$ .

#### **Procedure:**

- 1. Write a C function which takes a single argument of type float and returns a float equal to x\*x + 2\*x 1. The function prototype should be:
- float f(float x);
- 2. Using the above function, write a second function which takes two float arguments, x0 and h, and returns an estimate of the gradient of  $x^2+2x-1$  at x0 using Equation (5). The function prototype should be:
- float diff(float x, float h);
- 3. Test your program given that:

$$f'(x) = 2x + 2$$
$$f'(0) = 2$$
$$f'(1) = 4$$
$$f'(-1) = 0$$

You may use the following template:

```
#include <stdio.h>
float diff(float x);
float f(float x);
int main() {
    float h = 0.0001;
    printf("%f\n", diff(0, h));
    printf("%f\n", diff(1, h));
    printf("%f\n", diff(-1, h);
}
float diff(float x) {
    float d; // Differentiation result variable d = ; // Fill in this line return d;
}
// Write the function definition of f(float x) below here
```

## Task 9: Functions and Static Variables: Fibonacci Sequence Generator

**Review:** The Fibonacci Sequence is a sequence of integers:

 $x_1, x_2, x_3, ...,$ 

where:

$$\begin{aligned} x_1 &= 1 \\ x_2 &= 1 \\ x_n &= x_{n-1} + x_{n-2} \end{aligned}$$

**Task:** Write a C function which, each time it is called, returns the next value of the Fibonacci sequence. This will require the use of static variables within the function. Use the following function prototype:

```
unsigned int fib (void);
```

You can use the following template:

```
#include <stdio.h>

unsigned int fib(void);

int main () {
   int n;

for(n = 0; n < 10; n++)
     printf("%d %x\n", n, fib() ); //%x formats an unsigned int
}</pre>
```

After correctly implementing the function definition for fib() your program output should be:

- 1 1
- 2 1
- 3 2
- 4 3
- 5 5
- 6 8
- 7 13 8 21
- 9 34

#### Task 10: Mandelbrot Images - Advanced

Starting from a completed solution to the Week 3 Mandelbrot problem modify your code to generate an ASCII netpbm "portable PixMap" (PPM) formatted image.

# **PPM Image Format**

The PPM format specification allows images to be written to files using only plain text (ASCII) data. This results in a *very* simple file format which is easy to create with basic programs.

The file header has the following format:

```
P3 
<x resolution> <y resolution> 
<max value>
```

#### where:

- P3 is a "magic number" identifying the format
- <x resolution> is the number of pixels horizontally
- <y resolution> is the number of pixels vertically
- <max value> is the pixel value corresponding to maximum brightness. Typically 255.

An example header for a 100x100 pixel image would be:

```
P3
100 100
255
```

After the header comes the *body*. This is a list of **integer** RGB triplet numbers, separated by whitespace. The exact format is not critical, but I recommend the following:

```
R G B
R G B
R G B
```

The pixel data scans left-to-right top-to-bottom (ie: top left pixel is first, bottom right pixel is last). This is the same order in which the Week 3 task calculated pixel values.

#### Colouring Fractal Images

In order to colour a fractal image a mapping is used which converts each pixel's *iteration count* to a colour. There are a near-infinite number of choices for this and I strongly recommend you research so-called "colorbar" creation. For this task I recommend the following two options:

1. For debugging, use a grayscale mapping which uses the following formula for a pixel brightness, p, given the number of iters a pixel took to escape:

$$p = 255 \times \frac{\mathrm{iters}}{\mathrm{MAX\_ITERS}}$$

To create greyscale images the RGB values of a pixel must be equal. This means that after you calculate p you can just use

```
R = p;

G = p;

B = p;
```

to make R, G and B equal. **NB:** The PPM format requires the output numbers to be **integers!** 

2. More interesting colour mappings can be built with the use of the HSL (Hue-Saturation-Luminance) colourspace. This is a set of 3 numbers (H, S and L) which define a unique colour based on their hue (base colour from the rainbow), saturation ("colourfull-ness") and

luminance (brightness).

You can then slightly tweak the previous formula to provide a H value and fix S and L at 1.0:

$$H = 360 imes rac{ exttt{iters}}{ exttt{MAX\_ITERS}} \ S = 1.0 \ L = 1.0$$

Because the PPM image format only supports RGB pixel formats you will need to implement formulas which convert HSV triplets to RGB values. Wikipedia lists the set of formulas. Implement them in code, either as three functions or just as "inline" code.

You can attempt to write a single function which accepts a pointer to an array of 3 floats but we won't cover the details of this for a couple of weeks.

After RGB values have been calculated the output file data can be written.

# **Creating Files**

For this task we have two options for creating a file:

- 1. Use command line output redirection
- 2. Use the C file I/O library

The first option keeps your program simpler but requires the use of a command line when running the program. If your code simply uses printf() to output the PPM data (and *nothing* else) it can be written to a file with:

```
# ./a.out > image.ppm
```

The file image.ppm can then be downloaded (if you're using Che etc) or directly opened with an image editor. I know eog, gimp, etc open PPM on Linux and am naively hoping that something on Windows supports it.

The alternative, which will work with C development environments which don't have command lines like OnlineGDB, is to use the C file I/O library. To do this you need several lines of code and an extra function:

```
FILE *output; // A pointer variable of type FILE*
output = fopen("image.ppm", "w"); // To open the file image.ppm
fprintf(output, "%d %d %d\n", r, g, b);
```

The FILE \*output line is a variable declaration, only do this once. Likewise, output = fopen... opens the file image.ppm for writing. Only do this once as well.

The fprintf() function is almost exactly the same as printf() except it takes an extra argument: the file to write to. In this case passing output (the FILE \* variable declared earlier) will write the formatted text to that file.

Lets see if somebody gets this to work given the above plus your own independent research. We will formally cover file I/O in a few weeks (check the course outline for a planned week).

# 4 C Summary

This section will be included in all future lab documents and lists a summary of C language features taught prior to the lab session. It will grow each week.

Not everything listed in this section is required to complete a particular lab.

## 4.1 Basic Structure

This is the absolute minimum amount of code you need to make a C program compile, run, and interact with the user via a console:

```
#include <stdio.h>
int main() {
    // Your program goes here
    return 0;
}
```

# 4.5 Operator Shorthand

Many arithmetic operators support the following shorthand syntax. The left and right columns present equivalent statements.

# 4.2 Comments

```
1 // This is a comment to end of line

2 
3 /* this is a block comment
4  which could span
5  multiple
6  lines
7  */
```

#### 4.3 Code Blocks

Any section of code encompassed by  $\{\ldots\}$  is a *block*.

# 4.4 Operators

Operation	C Symbol
Addition	+
Subtraction	_
Multiplication	*
Division	/
Modulus	왕
Increment	++
Decrement	
Less than	<
Less than or equal to	<=
Greater than	>
Greater than or equal to	>=
Equal to	==
Not equal to	!=
Boolean AND	& &
Boolean OR	
Boolean NOT	!

Table 1: Arithmetic operators in C

# 4.6 Data Types

Type	Bytes	Value Range
char	1	-128, +127
unsigned char	1	0, 255
short	2	-32768, 32767
unsigned short	2	0, 65535
int	4	$\approx \pm 2.1 \times 10^9$
unsigned int	4	0, 4294967296
long	8	$\approx \pm 9.2 \times 10^{18}$
unsigned long	8	$0, 1.8 \times 10^{19}$
float	4	$1.2 \times 10^{-38} \text{ to } 3.4 \times 10^{38}$
double	8	$2.3 \times 10^{-308}$ to $1.7 \times 10^{308}$

Type	Precision
float	6 sig. figs.
double	15 sig. figs

# 4.7 Standard i/o

Read a single variable from stdin with scanf(); scanf("format specifier", &variable);

Write a single variable to stdout with printf(); printf("format specifier", variable);

You can use printf(); without a newline ( $\n$ ) to create an input prompt:

```
printf("Enter a number: ");
scanf("%d", &variable);
```

This prints:

Enter a number:

where \_ indicates the terminal prompt (ie: where typed characters will appear).

#### Format Specifiers 4.8

The following table is weefully incomplete. The compiler may generate warnings if %d is given something other than int and %f is given something other than float. An attempt will be made to ensure these are sufficient.

Data Type	Format Specifier
Integers	%d
Floating point	%f
Float with n decimal places	%.nf

Table 2: Basic format specifiers

#### 4.9 Type Casting

Placing the syntax (type) before a variable name performs a type cast (ie: data type conversion).

eg: convert float to an int prior to using its value. This forces a rounding-down to the nearest integer.

```
1 float a;
2 // ...
y = (int)a * z;
```

**NB:** This does **not** modify the original variable.

Data type "upgrades" are done automatically by the compiler but sometimes it is desired to downgrade or force esoteric behaviour. Adding it unnecessarily doesn't have any negative impact. Applications in ENGG1003 will be limited but it comes up regularly in embedded systems and nobody else explicitly teaches type casting. I have used it extensively if (condition) { in the low-level art of bit banging: manual manipu-2 lation of binary data. This is, unfortunately, beyond 3 } else { ENGG1003.

#### 4.10 Flow control

Flow control allows selected blocks of code to execute 1 if (condition) { multiple times or only under a specified condition. 2 // Do stuff

#### 4.10.1 if()

The if () statement executes a block of code only if the *condition* is true. The condition is an arithmetic statement which evaluates to either zero (false) or non-zero (true).

```
if () Syntax:
```

```
if(condition) {/* other code */}
```

Full if () example:

```
if(x > 10) {
   // Do stuff
```

Condition Examples:

- if(x) // if(x is not zero)
- if (x+y) //if ((x+y) is not zero)
- if (y >= 5)
- if(1) // Always executes
- if(0) // Never executes
  - Can be used for debugging. Might be easier than a block comment /\* \*/

 $\mathbf{NB}$ : NEVER place a semicolon after an if (), that stops it from having any effect. The block after it will always execute. This bug can take days to find.

If there is only *one* statement after an if () the { } braces are optional:

```
if(x > 10)
  printf("x is greater than 10\n");
```

```
4.10.2 if() ... else if()
```

The C syntax for IF ... ELSE is:

```
// Do stuff
```

IF ... ELSEIF takes the form:

```
3 } else if(condition) {
    // Do stuff
```

Multiple "layers" of else if () can be written. You don't have to stop at two.

**NB:** NEVER place a semicolon directly after the else if (). Semicolons only go after the statements inside the if () block (ie: between the curly braces { }).

#### 4.10.3 while()

The while () flow control statement executes a block of code so long as a condition is true. The condition is checked before the block is executed and before every repeated execution.

The condition rules and examples are the same as for those listed under the if () statement.

#### Syntax:

```
while(condition) {/* other code */}
```

Example:

Evaluate the infinite sum:

$$\sum_{n=0}^{\infty} \frac{1}{n^2} \tag{6}$$

to a precision of  $1 \times 10^{-6}$ 

```
float sum = 0.0;
int x = 0;
while(1/(x*x) > 1e-6) {
    sum = sum + 1.0/(x*x);
    x++
}
```

**NB:** *NEVER* place a semicolon directly after a while () line. Semicolons only go after the statements inside the loop.

# 4.10.4 for(;;)

As of week 2 this has not yet been covered in lectures.

```
The for (;;) loop syntax is:
```

```
for( initial ; condition ; increment )
{
    // Do stuff
}
```

The three sub-parts have the following behaviour:

- **Initial:** Code which is executed *once*, before the loop is entered
- Condition: A condition which is tested *before* every loop iteration
- **Increment:** Code which is executed *after* every iteration

for (;;) Example:

```
int x;
for(x = 0; x < 10; x++) {
  printf("%d ", x);
}</pre>
```

will print:

```
0 1 2 3 4 5 6 7 8 9
```

The for (;;) loop example doesn't print 10 because the condition is "strictly less than 10". When x is incremented to 10 the condition fails and the loop exits. It prints 0 because the increment is only applied *after* the loop has run once.

#### 4.10.5 switch() case:

The switch() case: statement is a flow control mechanism which allows one option from a list of many to be executed. It is a neater replacement from complicated if() else if() blocks.

# (6) Example:

```
switch(x) {
   case 1: // Jumped to if x == 1
        break; // Jump out of switch()
   case 2: // Jumped to if x == 2
        break;
   case 3: // Jumped to if x == 3
        break;
   default: // Jumped to if nothing else matched
}
```

# 4.11 Library Functions

#### 4.11.1 rand()

To generate a random number between 0 and MAX:

```
#include <stdlib.h> // For rand()
// ...
x = rand() % (MAX + 1);
```

For all work in this course you may assume that the above method works well enough.

For more crucial work (eg: cryptography, serious mathematics) this method is considered problematic. Very advanced discussion Here.

# 4.12 Glossary of Terms

I'll sort these alphabetically later, just a brain dump for now. Sorry.

- Compiler: The software package which converts *source code* into a *binary*.
- **Source Code:** The text which you type into a programming environment (eg: OnlineGDB) which is sent to the *compiler*.

- **Binary:** A program data file which can be executed on a computer.
- Variable: A "thing" which remembers a number within your program. In C they have a type, a name, (optionally) an initial value, and (for future reference) a memory address. Variables change when they are on the left side of an assignment.
- **Pseudocode:** Any hand-written or typed notes which document the behaviour of a computer program. Pseudocode is for humans to read, not computers.
- Flow Control: Any algorithmic statement which breaks the "top-to-bottom, line-by-line" execution pattern of a computer program.

- Statement: A line of C code which performs a task and ends with a semicolon. Arithmetic lines, printf();, scanf();, and rand(); are all examples of statements.
- Assignment: The process of changing a variable's value as your program executes. In C, this is typically performed with the = symbol. Eg: x = y + 5 calculates the value of "y + 5" then allocates the result to the variable x.
- Block: A section of code "grouped together" by curly braces { ... }. Typically applies to flow control, where a single, say, if() controls a block of code listed inside { and }.
- Literal: Any numerical constant written in your code. Eg: In x < 2.0 the "2.0" is a literal. Unless otherwise stated, integer literals are treated as int data types (ie: they inherit the int's value range limit) and real valued literals are treated as doubles.