ENGG1003 - Monday Week 6

Interpolation, Assignment 1 and Mid-term quiz

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Lecture overview

1. Interpolation
2. Assignment 1
3. Mid-term quiz

The story so far

- variables and data types
- arrays (using `numpy`)
- plotting (using `matplotlib`)
- flow control
  - `if`
  - `while`
  - `for`
- functions

Most of ENGG1003 from here uses these elements of Python to solve Engineering problems

1) Interpolation

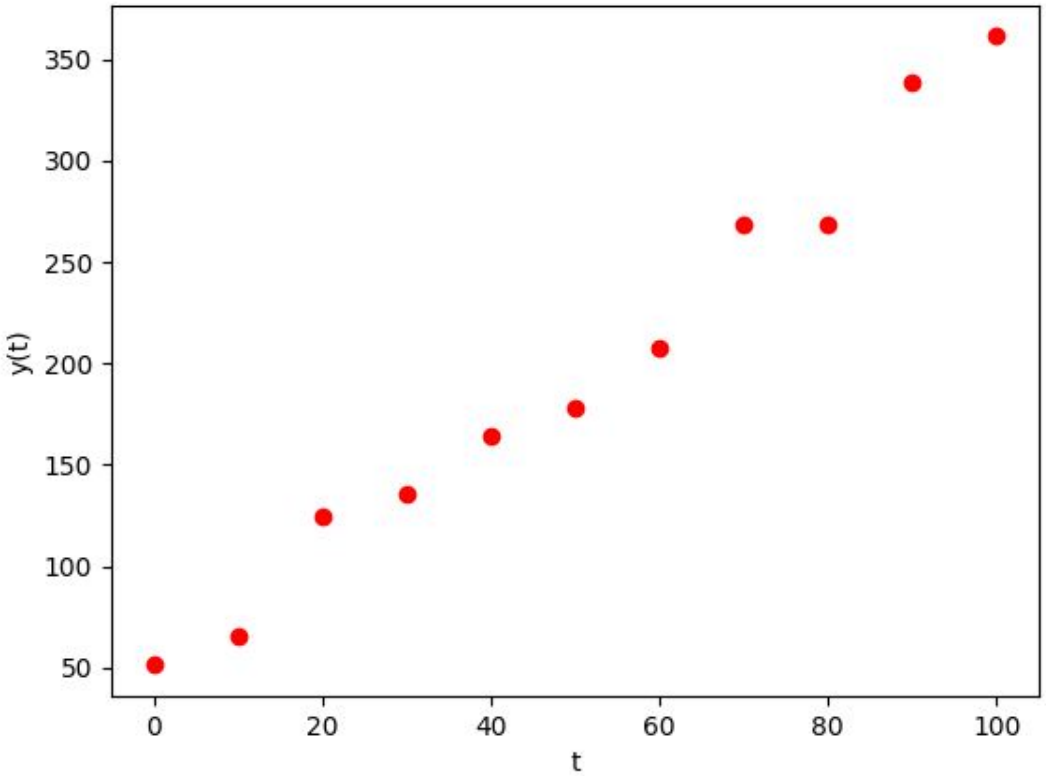
Two common forms of *curve-fitting* in Engineering applications:

1. *interpolation*
   - today's lecture
2. *regression*
   - considered in detail later in ENGG1003

- we now demonstrate both curve-fitting methods applied to the same dataset

Curve-fitting dataset

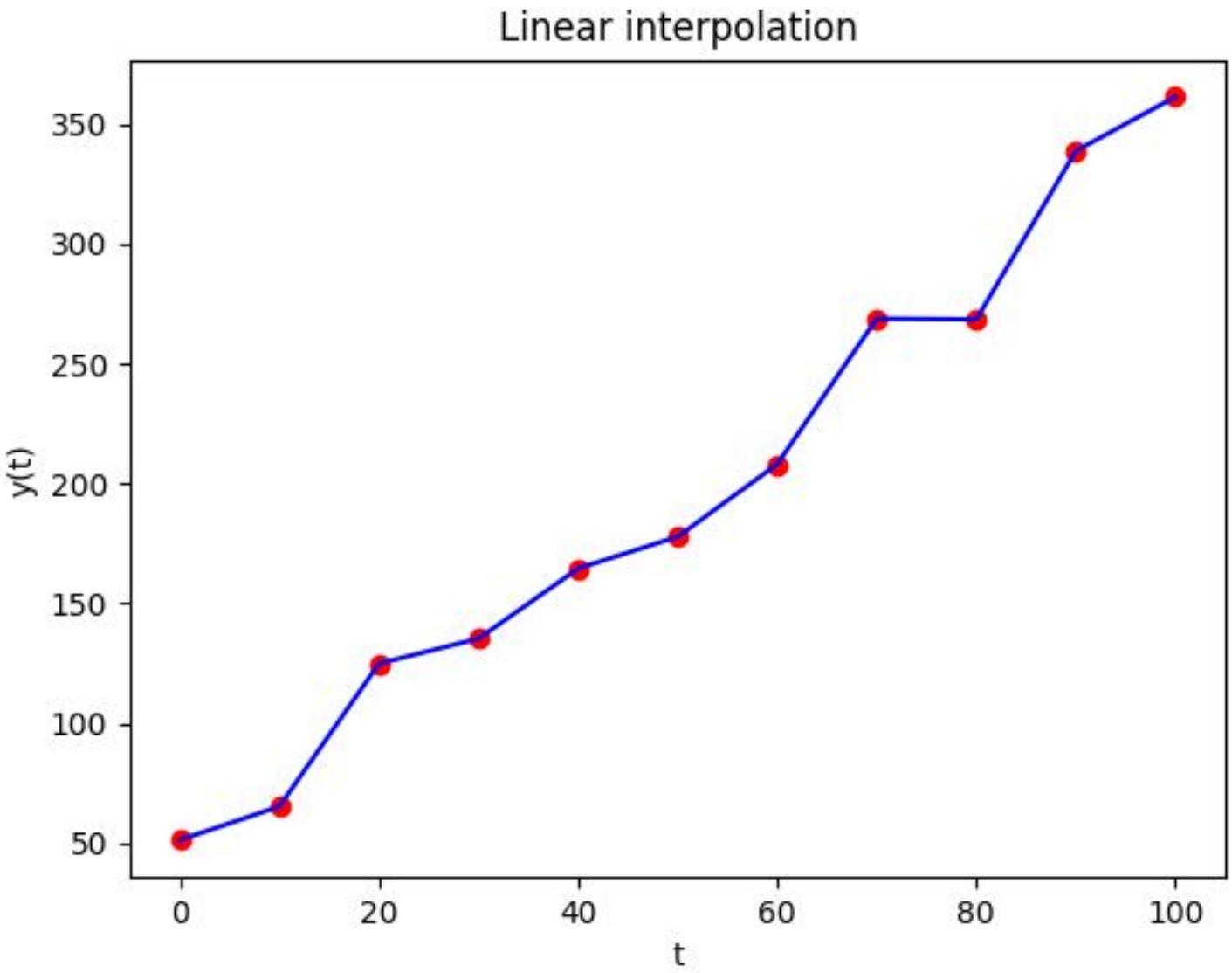
`Week6Mon.py`



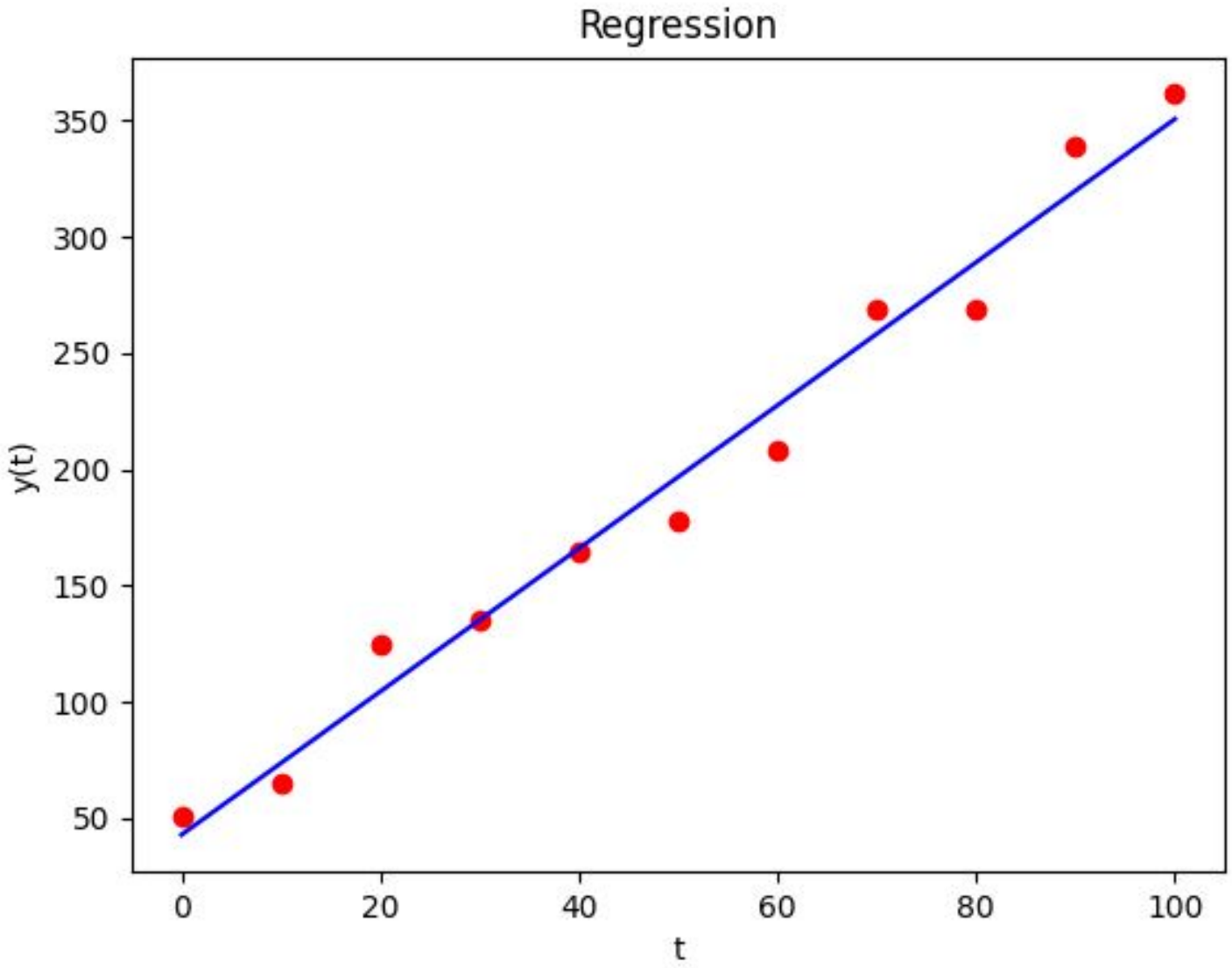
- 11 pairs of data points $(t_i, y_i), i = 0, 1, 2, \ldots, 10$

  $(0, 51.29), (10, 65.24), (20, 124.89), \ldots, (100, 361.32)$

Interpolation



Regression



Interpolation vs. regression

- **interpolation:** joining the dots
  - obtain value of y at some intermediate point
- **regression:** fitting a straight line
  - when there's "too much data", simplify
  - here, simplifying to a straight line
  - we return to choosing "best" straight line later in ENGG1003
  - no more regression in this lecture
- both interpolation & regression involve creating a function (blue line) from data (red dots)

Functions

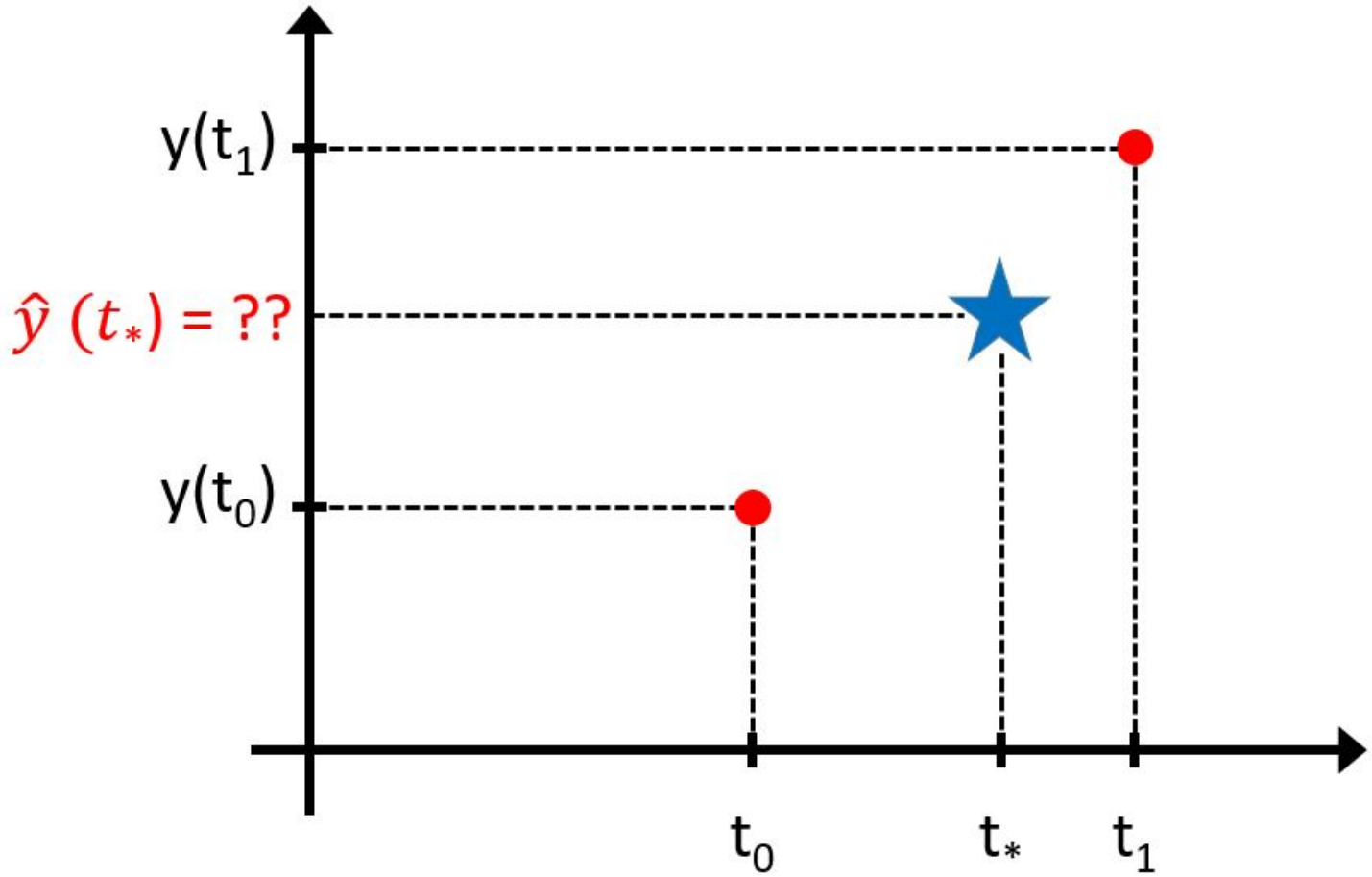
- in maths, you've seen functions written as follows:

$$y = f(t)$$

- function f, takes *argument* t and returns a *value* which is assigned to y

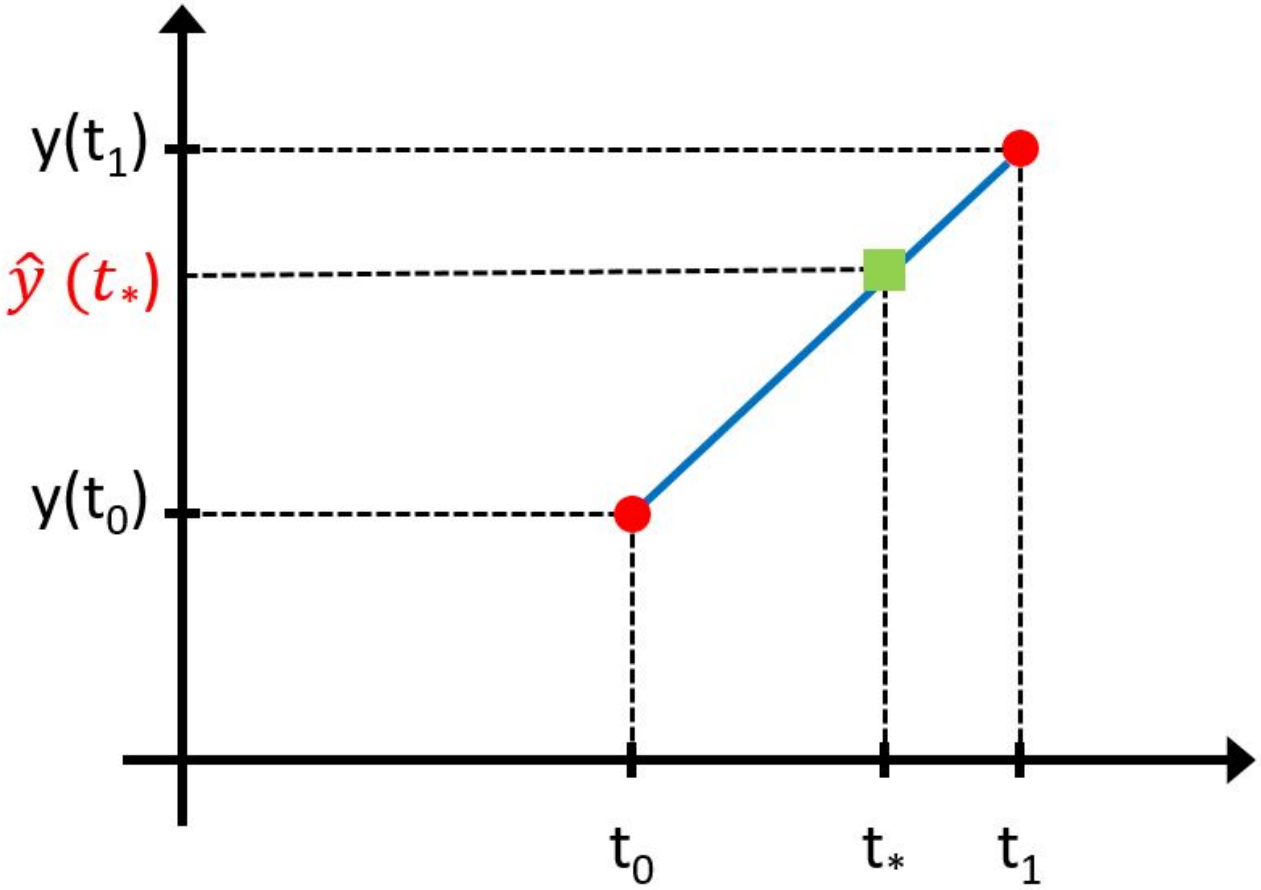
- . . . and last week we saw Python uses the same terminology with functions

The interpolation problem



Given: data points $(t_0, y(t_0))$ & $(t_1, y(t_1))$ and $t_\star$
Calculate: interpolated value $\hat{y}(t_\star)$

Linear interpolation



- interpolated value $\hat{y}(t_\star)$ lies on straight line connecting $(t_0, y(t_0))$ & $(t_1, y(t_1))$

Linear interpolation using `interp1d`

- `interp1d` function from `scipy.interpolate`
  - `pip install scipy` at terminal before using `scipy` for the first time

- `t` and `y` are arrays of values used to approximate some function: $y = f(t)$

```
1 f = interp1d(t, y)
```

- call to `interp1d` returns a function
  - first time we've seen a *function* returned by a function
- live demo

Linear interpolation in Python

Week6MonLinear.py

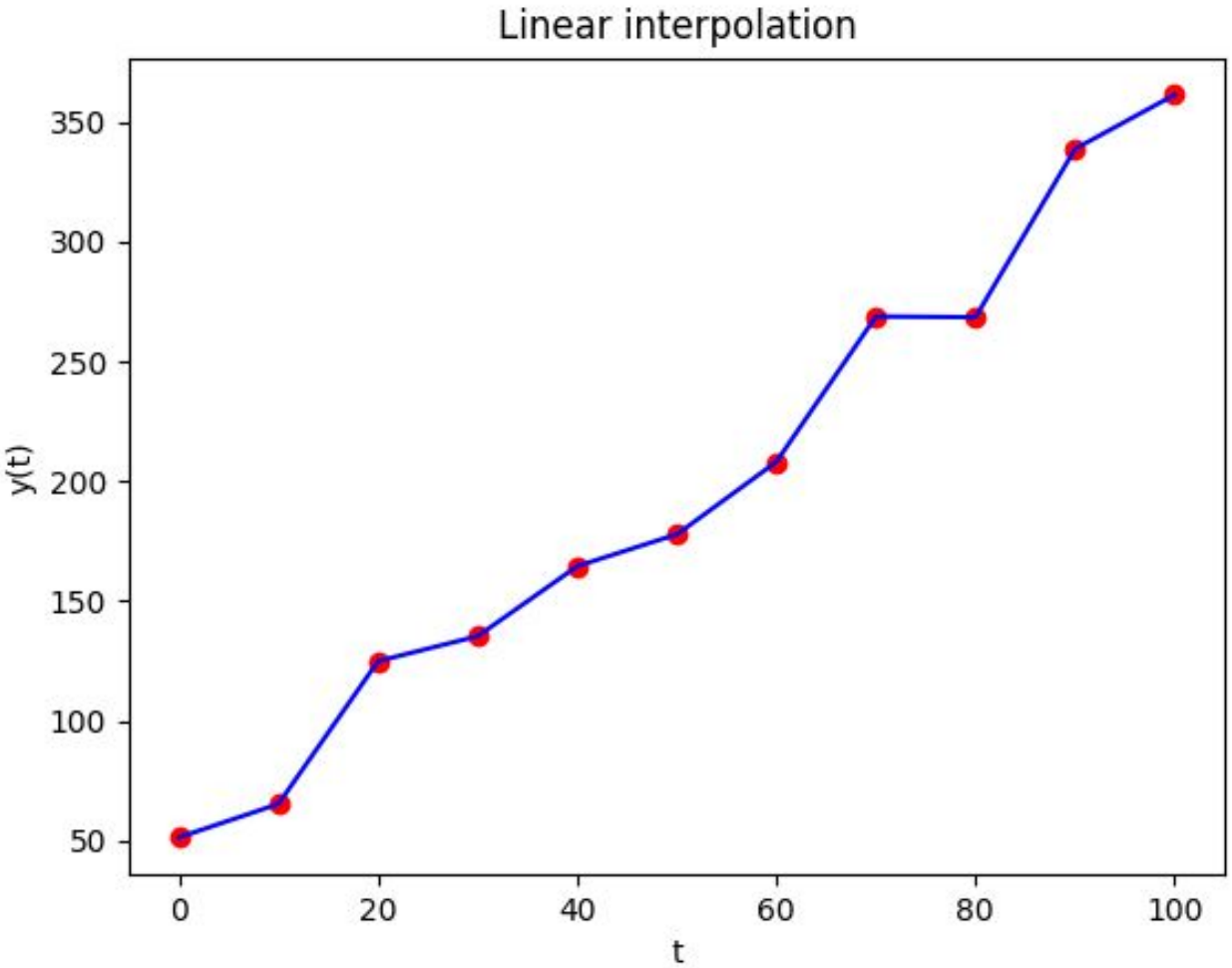
```
1  import numpy as np
2  import matplotlib.pyplot as plt
3  from scipy.interpolate import interp1d
4
5  # seed random number generator to reproduce lecture results
6  np.random.seed(27101967)
7
8  N = 11
9  t = np.linspace(0,100,11)              # 0,10,20,...,100
10 tnew = np.linspace(0,100,100*N)        # 0,0.1,0.2,...,100
11 n = np.random.uniform(-25,25,N)        # noise on linear function
12
13 m = 3                                  # gradient
14 b = 50                                 # intercept
15 y = m*t + b + n                    # dataset is straight line + noise
```

Linear interpolation in Python (ctd.)

```
1  # INTERPOLATION
2  f = interp1d(t, y)
3
4  # PLOT RESULTS
5  plt.plot(t, y, 'ro')
6  plt.xlabel('t')
7  plt.ylabel('y(t)')
8  plt.plot(tnew, f(tnew), 'b')
9  plt.title('Linear interpolation')
10 plt.show()
```

- **line 2:** create function `f` to interpolate data in arrays `t` and `y`
- **line 8:** use function `f` using "high resolution" time data in array `tnew`

Linear interpolation



- "stitches together" straight line segments

Beyond linear interpolation: Cubic splines

Problem: slopes of adjacent straight lines change abruptly at data points

- *could* solve by stitching together quadratic polynomials (parabolas) between consecutive point pairs
  - adjacent parabolas pass through data points
  - *and also have slopes that match at data points*

- very common to use degree-3 polynomials (cubics) instead of degree-2 parabolas
  - even smoother fit to data
  - *cubic splines* very popular in computer graphics

Cubic spline in Python code

```
# INTERPOLATION
f3 = interp1d(t, y, 'cubic')

# PLOT RESULTS
plt.plot(t, y, 'ro')
plt.xlabel('t')
plt.ylabel('y(t)')
plt.plot(tnew, f3(tnew), 'b')
plt.title('Cubic spline interpolation')
plt.show()
```

Linear interpolation:

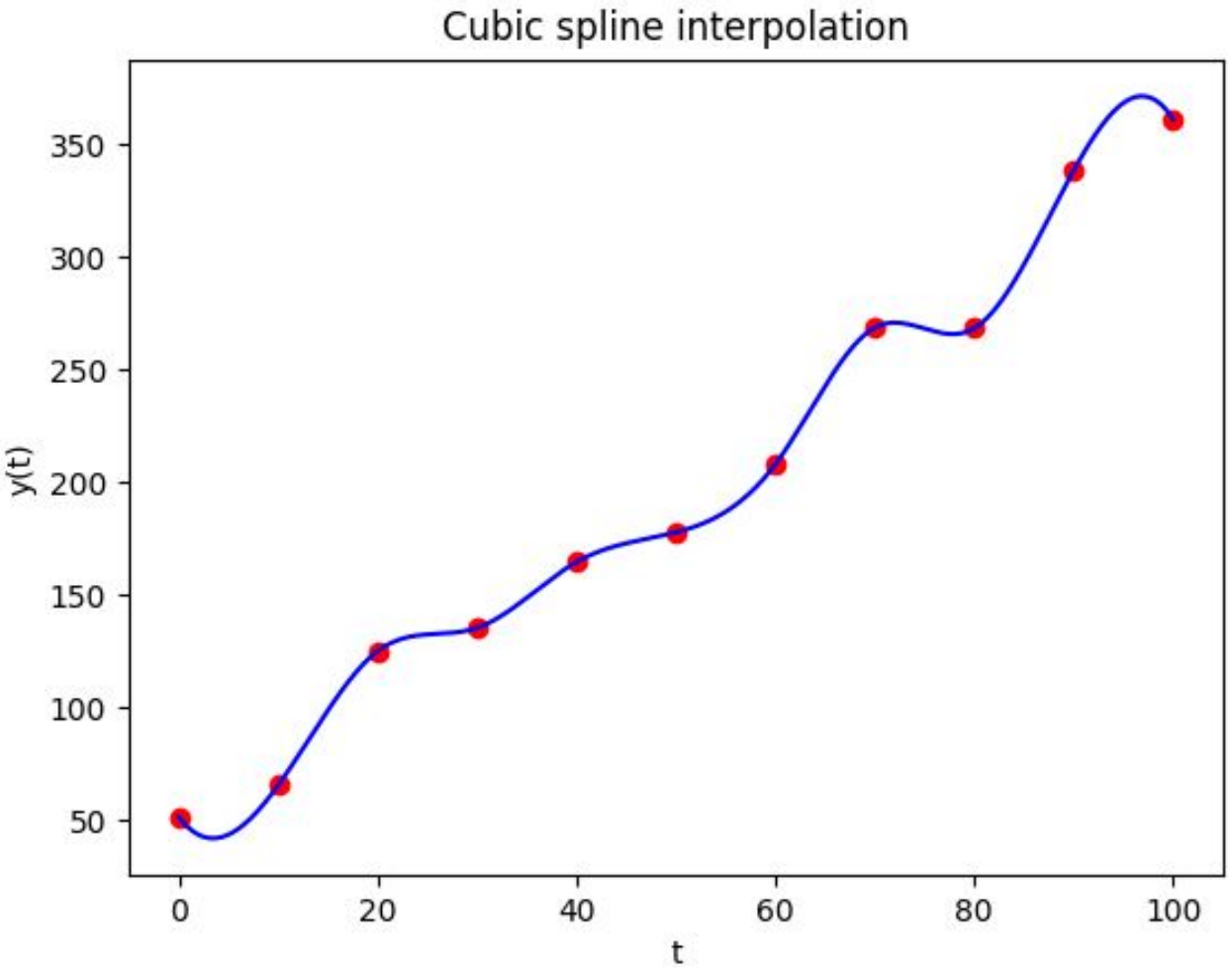
```
f = interp1d(t, y)
```

Cubic spline interpolation:

```
f3 = interp1d(t, y, 'cubic')
```

- Live demo of `Week6MonCubic.py`

Cubic spline interpolation



- "stitches together" *cubic* polynomials

2) Assignment 1

- released today, Monday 29 March 2021
- upload Python file to BB no later than 9:00 am, Monday 19 April
- counts for 20% of course grade
- each student will be assessed by demonstrator in week 7 face-face computer lab (after recess)

2) Assignment 1

- assignment topic: analysis of GPS data
- in more detail:
  - GPS data collected during a mountain bike ride
  - GPS track log is presented in a `csv` file containing timestamps, latitude, longitude, and elevation columns recorded at 1 second intervals
  - project asks you to analyse GPS data, eg: fitness tracker
  - use interpolation where GPS signal was lost
- computer labs this week:
  - there is no week 6 lab sheet
  - get started on assignment in place of lab sheet

3) Mid-term quiz

- Thursday 1 April, 4–5 pm
  - during scheduled lecture time
  - mid-term quiz instead of lecture this week so. . .
  - **NO Zoom or YouTube livestream on 1 April**
- 50-minute quiz
- open-book
- quiz will appear on BB at 4:05 pm
  . . . and will disappear at 4:55 pm
- counts for 15% of course grade

What to expect, and how to prepare

- the quiz will ask you to write Python code to:
  - load a `csv` file
  - perform some calculations on a specified column of the file ie: array processing
    (each student gets assigned a unique column in the file)
- once your program is complete, you do two things:
  1. enter the results of your program into BB
  2. upload your Python code to BB

- **there is a practice quiz NOW on BB**
  - you can practice as many times as you like!
- live demo of how the mid-term quiz will run

Lecture summary

- Interpolation
  - linear interpolation
    - straight line "join the dots"
  - cubic spline interpolation
    - smoothly connects data points

- Assignment 1
  - released today
  - submissions due on BB by 9:00 am, Monday 19 April
  - worth 20%

- Mid-term quiz
  - **there is a practice quiz NOW on BB**
  - done on BB at 4:00 pm, Thursday 1 April
  - worth 15%