ENGG1003 - Monday Week 2

Calculating Pi Arithmetic Datatypes

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Before we start...

- Today's lecture is information overload
 - ▶ It is a long list of "stuff" to rote learn
 - ► Half of programming is just "playing with Lego" with this "stuff"
 - There is a lot to learn before we can solve interesting problems
- It will probably push you out of your comfort zone
- Lab experience will rebuild your confidence
 - Much of this content will be used in every lab
- But first, a problem for motivation...

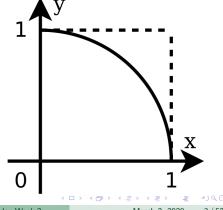
Case Study: Calculating π

- Computers are really good at repetitive things
- Lets use this fact to calculate π using a "monte-carlo" method
 - Informally, these are methods which solve problems by repeating the same thing with different inputs until patterns emerge
 - It could repeat millions or billions of times
 - Name comes from the Monaco Principality's high concentration of casinos
- Algorithm pseudocode will be written before an implementation in C

Case Study: Calculating π

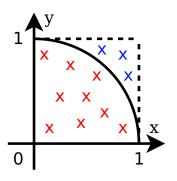
Consider a quadrant of a unit circle (r = 1) with a square around it:

- Area of the square $A_1 = 1$
- Area of the circle quadrant $A_2 = \frac{\pi r^2}{4} = \frac{\pi}{4}$
- Ratio of areas $\frac{A_2}{A_1} = \frac{\pi}{4}$
- Therefore $\pi = 4 \times \frac{A2}{A1}$



Case Study: Calculating π

- We can't calculate the area ratio without knowing π
- Estimate it by:
 - Randomly picking many points inside the square
 - Test if the point is inside the circle with $x^2 + y^2 < 1$



• $\pi \approx 4 \times \frac{\text{Number of points which land inside circle}}{\text{Total number of points tested}} = 4 \times \frac{9}{12} = 3$

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- The algorithm needs to repeat the same thing multiple times
 - This implies use of a loop
 - The loop's exit condition needs to be defined
- As the loop repeats, we need to keep track of the following variables:
 - The number of points tested
 - The number of points which landed inside the circle
 - ▶ The (x, y) coordinates of the point under test



- The number of points tested will be an integer, we will call it countTotal
- The number of points found to be inside the circle is also an integer, we will call it countInside
- Before these variables are used they should be initialised
 - ie: The algorithm will explicitly include countTotal =
 0 and countInside = 0
 - So-called uninitialised variables have undefined (or random) values

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- The condition on incrementing countInside is $x^2 + y^2 < 1$
- Incrementing a variable in pseudocode takes the form:
 - variable = variable + 1
 - ► This can be read as "variable becomes variable plus 1"
 - Maths people would write: $x_{n+1} = x_n + 1$



- \bullet The point under test needs two "real" variables: x and y
 - "Real" comes from mathematics: any number with integer and fractional components. Eg: 1.45
- These values take new random values each loop
- The pseudocode doesn't need to describe how a random number is generated
 - ➤ Stating: "x = a random number between 0 and 1" is totally acceptable
- At the end of the algorithm the final step will be $\pi = 4 \times \frac{\text{countInside}}{\text{countTotal}}$

```
BEGIN
  integer countTotal = 0
  integer countInside = 0
  WHILE countTotal < A large number
    x = random number between 0 and 1
    v = random number between 0 and 1
    countTotal = countTotal + 1
    IF x*x + y*y < 1
      countInside = countInside + 1
    ENDIF
  ENDWHILE
  pi = 4*countInside/countTotal
  PRINT pi
END
```

Missing Knowledge for C Implementation

- More information about arithmetic
 - ► Relational operators (less/greater-than) look useful
 - Is there a neat way to do count=count+1?
 - countInside and countTotal are both integers. What happens when we divide?
- Datatypes and how they are handled in arithmetic statements
- How do we generate random numbers?
- Syntax for WHILE loops and IF statements

Basic arithmetic was seen in the lab

Operation	C Symbol
Addition	+
Subtraction	_
Multiplication	*
Division	/

Table: Basic arithmetic operators in C

 Complex expressions can be built from these operators and parentheses

Examples:

$$z=x^2+5(y+b)$$
 $z=x*x+5*(y+b);$ $u=\frac{x+1}{x-1}$ $u=(x+1)/(x-1);$ $v=z^3+\frac{5(y+b)}{2}$ $v=z*z*z+(5*(y+b))/2;$

- Multiplication is not assumed. If you write 5 (y+b) the compiler will generate a syntax error.
- To be valid C statements the semicolon is required.

- C supports two time-saving *unary* operators:
 - Very useful in loops.

Operation	ration C Syntax Replaces		
Increment	x++; or ++x;	x = x + 1;	
Decrement	x; orx;	x = x - 1;	

• It also supports the following shorthand syntax:

What's the difference between x++ and ++x?

- x++ is a post-increment
- ++x is a pre-increment
- If they appear in an arithmetic expression, pre-increment is processed before the variable is used and post-increment is processed after it is used.
- In isolation there is no difference.

Modulus

- Integer division ignores (truncates) any fractional component
- The modulus operator provides the remainder after division
 - C uses the % character
 - ▶ "a % b" means "remainder of a / b"
- Example:
 - **▶** 10 / 3 = 3
 - ▶ 10 % 3 = 1

Modulus Example - Printing Every *nth* Number

```
1 #include <stdio.h>
2 int main() {
   int x = 0;
  while (x < 1000)
      x++; // Increment x
      if(x%100 == 0) // if(x is divisible by 100)
       printf("%d\n", x);
    return 0;
10
11 }
```

Relational Operators

• C supports six *relational* operators:

Operation	C Symbol
Less than	<
Less than or equal to	<=
Greater than	>
Greater than or equal to	>=
Equal to	==
Not equal to	! =

Relational Operators

- The result of a relational operation is 0 or 1
 - C treats 0 as Boolean FALSE and non-zero as TRUE
- They are typically used as flow control conditions
 - ▶ if(condition) {statements}
 - while(condition) {statements}
- While we're here: the above is the correct syntax for IF and WHILE flow control in C

if() and while()

Syntax for your "cheat sheet":

```
1 if (condition) {
2 // Do stuff
3
1 if (condition) {
2 // Do stuff
3 } else {
4 // Do other stuff
5 }
while (condition) {
2 // Do stuff
3
```

• If there is a single statement inside an if() or while() the { and } are optional

if() and while()

Example:

```
1 #include <stdio.h>
3 main() {
   int x = 1;
  while (x != 0) {
    printf("Enter an integer: ");
      scanf("%d\n", &x);
      if(x % 2 == 0)
        printf("%d is even\n", x);
      else
10
        printf("%d is odd\n", x);
11
12
13 }
```

Boolean Operators

- We discussed Boolean algebra last week
- It has three operators: AND, OR, NOT
- In C, these are implemented with:

Operator	C Characters
AND	& &
OR	
NOT	!

- I know the | character as a "pipe" symbol or "vertical slash"
 - Ask your demonstrator to find it on the keyboard

Conditions

- We have seen that if() and while() statements need conditions
- A condition can be any combination of variables, operators, and literals (numbers, defined later)
- The following are all valid:
 - \rightarrow if(x > 29)
 - \triangleright if (x == 2)
 - \triangleright if(!(x == y))
 - \triangleright if ((x > 5) && (x < 20))
 - \triangleright if (x = y + z)
 - Evaluates (y + z), assigns to x, uses result as if()
 condition

C Arithmetic Operator Precedence

- C has an "order of operations"
- eg: 1+5*2 evaluates to 11
 - You remember BODMAS / PEDMAS, right?
- Multiplication and division first
- Addition and subtraction second
- Relational operators somewhere below that
- If in doubt: force order with parentheses
 - This makes the code more readable
 - It doesn't cost you anything
 - C compilers understand algebra and will optimise inefficient expressions automatically



Variable Declaration

- In C, all variables are declared before use
- Declaration specifies the variable's:
 - Datatype
 - Name
 - An initialisation value (optional)
 - Always assume uninitialised variables have random values!
 Behaviour varies between compilers and target platforms.
 - eg: int counter = 0;
 - Type is int
 - Name is counter
 - Initial value is 0 (optional)
- C is a "strongly-typed" language
 - ► A variable's type doesn't change



Variable Declaration

• You can declare multiple variables in one line:

```
1 int a, b, c, d;
```

You can mix initialised and uninitialised variables:

```
1 \text{ float } q, r = 1.0, s = 12e3, t;
```

 All variables declared in this way must be of the same type

Variable Naming Rules

- Variable names:
 - Are case sensitive
 - Must not be a C keyword (eg: int, char, while, etc)
 - Must not contain special characters (⋆-+/, etc)
 - Must begin with a letter
 - Can contain numbers
 - Can contain underscores
- What you do with those rules is up to you
- Modern practice encourages:
 - camelCaseVariableNames
 - names_with_underscores



Integer Data Types

- There are several integer data types
- They vary by their:
 - Size
 - Support for negative numbers
- C integer types can be 1, 2, 4, or 8 bytes long
 - int and long sizes vary by platform
 - Larger sizes store larger numbers, use more RAM
- Each type can be signed or unsigned
 - Unsigned numbers are always positive but you get double the value range

Integer Data Types

- The integer data type ranges can be calculated from the data type's size in bits
- For unsigned numbers of bit length *n*:

$$\max = 2^n - 1 \tag{1}$$

• For signed numbers of bit length n:

$$\max = 2^{(n-1)} - 1 \tag{2}$$

$$\min = -2^{(n-1)} \tag{3}$$

• Signed numbers are stored in *two's complement* format, covered in ELEC1710

Integer Data Types

- C includes the sizeof() expression so that a program can discover the size of a data type on a given platform
- On a modern 64-bit Linux desktop machine:

Type	Bytes	Bits	Value Range
char	1	8	-128, +127
short	2	16	-32768, 32767
int	4	32	-2147483648, 2147483647
long	8	64	-9223372036854775808,

Unsigned Integers

- Unsigned integers are always positive
- They are the same size as their signed counterparts
- The unsigned keyword placed before the data type makes that variable unsigned
- eg: unsigned char is 1 byte and has a value range of 0 to 255

Overflow

- Overflow occurs when the result of a calculation is too big to fit into the target type
- Example: 127 + 1 = -128

```
1 #include <stdio.h>
2 int main() {
3    char x = 127;
4    printf("%d\n", x);
5    x++;
6    printf("%d\n", x);
7    return 0;
8 }
```

Overflow

- Message: make variables as small you can, but no smaller
 - Or just use long everywhere and cop the performance hit
- Quite often you need to take a guess at how big a variable needs to be
- Typically a good idea to document software limits due to variable choice

Why Care About Data Types?

- You may be thinking "why not make everything a long?"
- Answer: speed and memory
- Smaller types use less RAM
- Arithmetic on a type larger than the target platform's native size is slow
- Matters if you store millions of the same type
- Makes a huge difference on embedded targets
 - Don't declare 32-bit variables on an 8-bit AVR microcontroller unless you have to

Floating Point Data Types

- To store real numbers C has several floating point data types
- As with integers, try to use the smallest you can get away with
- long double is supported in gcc but...complicated

Type	Size	Range	Precision
float	4	$1.2 \times 10^{-38} \text{ to } 3.4 \times 10^{38}$	6 dp
double	8	2.3×10^{-308} to 1.7×10^{308}	15 dp

How good is 15 decimal places?

Paraphrasing NASA:

Calculating the circumference of Earth using 15 decimal places for π results in a truncation error about the size of a molecule.

39 digits of π calculates the circumference of the *visible* universe to within the width of a hydrogen atom ($\approx 10^{-10}$ m).

Floating Point Problems

- Q: Why not always use float or double instead of int?
- A: Floating point arithmetic is **NOT** exact
- Example 1: Does this code exit?

```
#include <stdio.h>
int main() {
  float x = 16000000.0;

while(x < 17000000.0) {
    x = x + 1.0;
    printf("%f\n", x);
}

</pre>
```

Floating Point Problems

- Example 2: $\tan\left(\frac{\pi}{2}\right)$ is undefined
- But using floating point π can't be represented exactly, so C produces a result anyway

```
#include <stdio.h>
#include <math.h>
int main() {
   double pi = 3.141592653589793238;
   printf("%f\n", tan(pi/2.0));
   printf("%f\n", ftanf((float)pi/2.0));
}
```

Literals

- A literal is any number written in the code
- Why not "constant"?
 - ► That word means something different
- Examples:
 - \triangleright x = 5; // 5 is a literal int
 - \triangleright y = 2.0 / z; // 2.0 is a literal double
- By default:
 - ► An integer literal is stored as an int data type
 - \bullet ie: has the value range and arithmetic limits of ${\tt int}$
 - ▶ A floating point literal is stored as double

Literals

- Integer literals can be in:
 - ▶ Decimal: 123
 - ► Hexadecimal: 0xA34 // Zero-x
 - Octal: 0125 // Capital letter 0
 - ► (Hex and octal are covered in ELEC1710)
- Integer literals can be specified as unsigned with the u suffix:
 - ▶ 938u
- They can also be declared long with the l suffix:
 - **37264841**
 - The compiler will issue a warning if a literal is too big for int

Literals

- Floating point literals can be written in many ways:
 - ▶ 1.0f // f suffix forces float
 - ▶ (float)2.3 // Forces float
 - ▶ 1.0 // Default to double
 - ▶ 1e2 // Double, 1 times 10^2
- 1e2 is known as "e-notation"
 - \triangleright XeY = X × 10^{Y}
 - ▶ I will use it all the time
- Forcing literals to float is frequently necessary in embedded systems which lack double precision hardware

Mixing Data Types

- C supports arithmetic between different types
- Type conversion is called casting
- When types are mixed two things can happen:
 - Types get upgraded automatically (implicit type casting)
 - Upgrade path is roughly: short/char int long
 long long float double
 - Types get specified manually by the programmer (explicit type casting)

Explicit Type Casting

- The data type of a variable (or literal) can be forced to change using type casting
- Write the desired type in parentheses before the variable or constant
- Examples:

```
x = (float)y / k;
```

 \triangleright y = (unsigned int)y + 32;

Format Specifiers

- A format specifier controls how printf();
 converts numerical (or textual) data to a series of ASCII characters
- Full details are complex, for now just use:
 - %d for integer types
 - %f for "fixed decimal place" floating point
 - %e for e-notation floating point
 - Cast inside printf() to suppress compiler warnings

Format Specifiers

Casting example:

```
long i;
// ...
printf("%d\n", (int)i); //Breaks when i>2^31
```

• %.df produces d decimal places of precision

```
eg:
```

```
float x = 1.23456;
printf("%.2f", x); // Prints 1.23
```

 Format specifiers can appear anywhere in the output text, eg:

```
printf("%f was the result\n", x);
printf("The result %f was calculated\n", x);
```

Format Specifiers

- You can print several numbers at once
- Separate variables with commas
- They are printed in the same order as variables are written
- You can put maths inside printf();

```
1 printf("%f plus %f is %f\n", x, y, x+y);
```

Integer Division Example

With all that out of the way, what is the output of each printf() statement?

```
#include <stdio.h>
int main() {
  printf("%d\n", 9/10);
  printf("%f\n", 9/10);
  printf("%f\n", 9.0/10);
  printf("%f\n", 9.0/10);
  printf("%f\n", 9/10.0);
  printf("%f\n", (float) 9/10);
  return 0;
}
```

Listing 1: intdiv.c

- In C there is a standard library function which generates random numbers
- We will study functions in more detail later
- To use a library function:
 - Read the function's documentation
 - #include the correct header file
 - Take note of the return value data type
 - Add any compiler flags (beyond ENGG1003)
 - Use the function in your code
- Demonstration: read the rand() man page
 - Click here



Observe that rand(); requires

```
#include <stdlib.h>
```

- Observe that it returns an int between 0 and RAND_MAX which, in gcc, is $2^{31}-1$
- Note that is has <u>limits</u> (advanced discussion, beyond ENGG1003)
- For us, using the % operator:

```
x = rand() % (RANGE+1);
```

produces a *good enough* random number between zero and RANGE

As above, zero to RANGE is produced with:

```
x = rand() % (RANGE+1);
```

• To generate numbers from 1 to RANGE:

```
x = (rand() % RANGE) + 1;
```

• These work because:

```
1 x = x % y;
```

is an integer between zero and y for any x

 Using the above information, we can roll a standard die with:

```
int dieRoll;
dieRoll = (rand() % 6) + 1;
```

Or, if you're a D&D fan, roll a D20 with:

```
int D20Roll;
2 D20Roll = (rand() % 20) + 1;
```

- RAND_MAX is a constant defined in stdlib.h
- We can try to generate a floating point number from 0 to 1 with a division:

```
float num;
num = rand()/RAND_MAX; // This is broken
```

- Problem: rand() is an integer, RAND_MAX is a (large) integer
 - ► The integer division result will always be zero!
- Solution: use an explicit cast so that a floating point division occurs:

```
double num;
num = (double)rand()/RAND_MAX;
```

Probably out of time by now, lets implement a π calculator in the lab... *In theory* you have enough information by now.