ENGG1003 - Tuesday Week 1

Algorithms and Pseudocode

Brenton Schulz

University of Newcastle

March 2, 2020



Algorithms

- Informally, an algorithm is a series of steps which accomplishes a task
- More accurately, the steps (instructions) must:
 - Have a strict order
 - Be unambiguous
 - Be executable
- "Executable" means that the target platform is capable of performing that task.
 - eg: An industrial welding robot can execute "move welding tip 1 cm left". A mobile phone can't.

Algorithms

- An algorithm exists purely as an abstract concept until it is communicated
- We will use:
 - Pseudocode to communicate algorithms to ourselves and other people
 - The languages C and MATLAB to communicate algorithms to computers
- Pseudocode can be very formal, but as engineers we will only use formal rules if required
 - eg: When documenting algorithms for other people
 - Your own "working out" can be anything that helps *you*

Algorithm Example 1

Name: Algorithm given to mum to start my car (2015 Tarago)

Result: The vehicle's engine is idling

Initialisation: stand next to the vehicle, key fob in hand

- Depress the unlock button on the key fob, car will beep twice
- Place key fob in your pocket
- Enter the vehicle, sit in the driver's seat
- Ensure that the gear selector has P engaged
- Depress the brake pedal
- Press the engine start button
- Wait 5 seconds
- If engine is not idling
 - Call me

Example Discussion

- Algorithms typically need to feel over-explained
 - Computers are really stupid; get in the habit of over-thinking everything
- The algorithm contained flow control in the form of an "if" statement
 - ► The final step ("call me") was conditional on the car not starting
- We will discuss conditional logical statements later, but first...

Algorithm Example 2

A wife asks her husband, a programmer, "Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?

A short time later the husband comes back with 6 cartons of milk and his wife asks, "Why did you buy 6 cartons of milk?

He replies, They had eggs.

Algorithm Example 2a

Lets make this more realistic.

A wife asks her robot helper, "Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?

The robot replies: "Unknown instruction: 'get 6'."

Flow Control

- Instructions in an algorithm execute in an ordered list
 - ie: top to bottom
- Flow Control is any algorithmic mechanism which changes the default "top to bottom" execution behaviour
- We will discuss IF statements and loops
- Flow control (almost) always requires a condition

Conditions

- Computers don't understand "maybe"
- A condition must be absolutely true or false
- Human examples:
 - I am within the boundary of the Callaghan campus
 - I am alive
 - My net worth is below AU\$100M
- Computer examples:
 - i is less than 184
 - x plus y is not equal to zero
 - Input data has been given to the program
 - A division by zero has occurred



Code Blocks

- A block is a set of instructions which are grouped together
- If a single condition controls multiple instructions they can go together in a block
- A block is typically indicated via indentation
- Eg:

```
IF it is raining
Pack an umbrella
Drive to campus instead of walking
Leave home 40mins early to find parking
ENDIF
```

IF Variants

- There are several versions of IF flow control:
 - ► IF ... ENDIF
 - ▶ IF ... ELSE ... ENDIF
 - ▶ IF ... ELSEIF ... ENDIF
- The IF and ELSEIF keywords indicate conditions
- The ELSE keyword is unconditional
- Which one you choose depends on need
 - Is there one thing which is conditional?
 - Do I need to make a choice between two or more options?
 - Could nothing be executed?



IF Statement Syntax

The IF ... ENDIF syntax is:

IF condition
do some things
ENDIF

Likewise: IF ... ELSEIF ... ENDIF syntax is:

IF condition1
do some things
ELSEIF condition2
do other things
ENDIF

And finally:

IF condition
do some things
ELSE
do some things
ENDIF

IF ... ELSEIF

- The IF ... ELSEIF construct can have multiple ELSEIF sections
- A crucial point:
 - Conditions are only tested if the previous ones fail
 - Once a condition is TRUE the others are ignored
 - ie: IF ELSE implements a choice priority

Algorithm Example 3 - Quadratic Root Finding

From high school you should know that the equation

$$ax^2 + bx + c = 0 (1)$$

has solutions given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \tag{2}$$

lets write an algorithm which provides real valued solutions to a quadratic equation.

(□) (□) (□) (□) (□) (□) (□)

Algorithm Example 3 - Quadratic Root Finding

Input: Real numbers a, b, and c

Output: Three numbers:

- 1 The number of solutions, N
- 2 One of the roots, x_1
- \bigcirc The other root, x_2

Behaviour:

- If N is 2 then x_1 and x_2 are different real numbers
- If N is 1 then x_1 is the unique solution and x_2 is undefined
- If N is 0 then x_1 and x_2 are undefined



Algorithm Example 3 - Quadratic Root Finding

```
BEGIN
INPUT: a, b, c
D = b^2 - 4ac
IF D < 0
N = 0

ELSEIF D == 0
N = 1
x1 = -b/(2a)

ELSEIF D > 0
N = 2
x1 = (-b + sqrt(D))/(2a)

ENDIF
```

- Reasonably formal pseudocode
- The IF ... ELSE IF flow control construct forces exclusive execution of only one block
- The first condition that is true causes execution of that block
- Subsequent blocks ignored
- Contains 3 conditions

Boolean Algebra Basics

- What if we want more complicated conditions?
 Boolean algebra is needed!
- Boolean algebra (or Boolean logic) is a field of mathematics which evaluates combinations of logical variables as either true or false
- Boolean variables can only take the values true (or 1) or false (or 0)
- Boolean algebra defines three *operators*:
 - OR
 - AND
 - NOT



Boolean Algebra Basics

- Boolean variables can be allocated any symbols (just like in "normal" algebra)
 - Typically get upper-case letters
 - ightharpoonup eg: X = A OR B
- Various symbols can be used for OR/AND/NOT, we will only use the words here
 - Write them in capitals to remove ambiguity
 - C and MATLAB have their own symbols for Boolean algebra
 - Other courses (eg: ELE17100) will use different symbols again

Boolean Operators

- An operand is a value on which a mathematical operation takes place
 - ightharpoonup eg: In "1 + 2" the 1 and 2 are operands and + is the operator
- OR Evaluates true if either operand is true
 - \triangleright X = A OR B
 - X is true if either one of A or B is true
- AND- Evaluates true only when both operands are true
 - \triangleright X = A AND B
 - X is true only if both A and B are true

Boolean Operators

- OR and AND are binary operators
 - They operate on two operands
 - From Latin "bini" meaning "two together"
- The NOT operator is unary
 - It only operates on one operand
 - ▶ NB: The operand could be a single variable or complex expression
- NOT performs a logical inversion
 - ► NOT true = false
 - NOT false = true

Boolean Condition Examples

- My car needs a service if, since the last service, (more than 6 months has past) OR (more than 15000km have been travelled)
- You will pass this course if (you score 40% or more in the final exam) AND (the weighted sum of all assessments is more than 50%)
- A computer program repeats an algorithm if (there is still data to process) AND (errors have not occurred) AND (NOT (the user has terminated the program))

Algorithm Example 4 - Boolean Conditions

Problem: How can square roots be calculated by a computer?

One Solution: The Babylonian Method.

The square root of a, \sqrt{a} , can be found by *iterating*:

$$x_{n+1} = \frac{1}{2} \left(x_n + \frac{a}{x_n} \right) \tag{3}$$

until x_n is "close enough" to the true value of \sqrt{a} for our liking. Execution of this algorithm can use two things:

- The loop flow control concept
- 2 Some kind of stop condition



Iteration

- In this context iteration is the process of repeatedly applying a formula to the same variables
- Iteration typically creates a sequence of numbers: $x_0, x_1, ..., x_n$
 - ▶ Eg: The equation $x_n = x_{n-1} + 1$ with a choice of $x_0 = 0$ just counts 1, 2, 3, 4...
- We will study a lot of equations like this in the coming weeks

Square Root By Hand

- Lets find $\sqrt{2}$ "manually"
- In our notation, a=2
- The choice of x_n doesn't *really* matter, lets go with $x_0=2$
- Applying the formula $x_{n+1} = \frac{1}{2} \left(x_n + \frac{a}{x_n} \right)$:

$$x_1 = \frac{1}{2} \left(2 + \frac{2}{2} \right) = 1.5$$

$$x_2 = \frac{1}{2} \left(1.5 + \frac{2}{1.5} \right) = 1.4167$$

$$x_3 = \frac{1}{2} \left(1.4167 + \frac{2}{1.4167} \right) = 1.4142$$

Square Root By Spreadsheet

Well that's tedious. Lets try it on a spreadsheet

Questions: When do we stop calculating? How would be write a *stop condition* in computer language terms?

Note that the "difference" is always negative.

Algorithm Example 4 - Boolean Conditions

- For this example we will choose two exit conditions:
 - An acceptable precision is reached
 - An iteration limit is reached
- The resulting Boolean expression is something like:

"If the change between x_n and x_{n+1} is greater than some precision value AND the number of iterations is less than maximum then continue iterating"

Loops

- A loop causes an algorithm to execute a given block of instructions multiple times
- Loops typically require an exit condition
 - Without an exit condition they are called infinite loops
 - Yes, these have a purpose
- Multiple types of loops
 - WHILE condition...ENDWHILE
 - DO...WHILE condition
 - ► FOR counter FROM 1 TO something

Algorithm Example 4 - Boolean Conditions

- Implementing the square root algorithm:
 - ► Choose max iterations as 10 and precision as 0.001

```
BEGIN
    INPUT a
    x = a
    xOld = 0 // Why do we do this?
    n = 0
    WHILE (n<10) AND ( (x-xOld) > -0.0001 )
        xOld = x
        x = 1/2*(x + a/x)
        n = n + 1
    ENDWHILE
END
```

• It loops until 10 *iterations* have occurred OR a precision limit is reached

Loop Details

- WHILE conditions are tested before "entering"
- The condition is tested before every repeat
- Variables in the condition should change inside the loop
 - Try to avoid infinite loops unless you want one
- What if we want to force the loop to execute *at least once*?
 - ► There exists a DO ... WHILE loop for this purpose