

ENGG1003 - Tuesday Week 2

Calculating Pi
C Arithmetic
Datatypes

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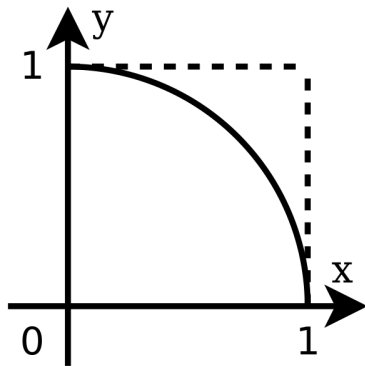
Case Study: Calculating π

- ▶ Computers are *really* good at repetitive things
- ▶ Lets use this fact to calculate π using a “monte-carlo” method
 - ▶ Informally, these are methods which solve problems by trying the same thing with different inputs until patterns emerge
 - ▶ It could repeat millions or billions of times
 - ▶ Name comes from the Monaco Principality's high concentration of casinos
- ▶ Algorithm pseudocode will be written before an implementation in C

Case Study: Calculating π

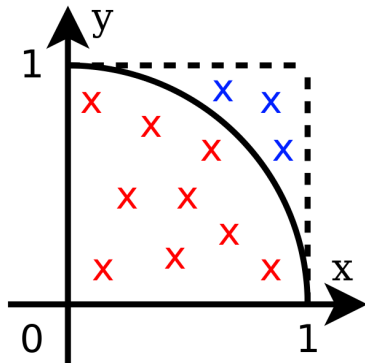
Consider a quadrant of a unit circle ($r = 1$) with a square around it:

- ▶ Area of the square
 $A_1 = 1$
- ▶ Area of the circle quadrant $A_2 = \frac{\pi r^2}{4} = \frac{\pi}{4}$
- ▶ Ratio of areas $\frac{A_2}{A_1} = \frac{\pi}{4}$
- ▶ Therefore $\pi = 4 \times \frac{A_2}{A_1}$



Case Study: Calculating π

- ▶ We can't calculate the area ratio without knowing π
- ▶ Estimate it by:
 - ▶ Randomly picking many points inside the square
 - ▶ Test if the point is inside the circle with $x^2 + y^2 < 1$



- ▶
$$\pi \approx 4 \times \frac{\text{Number of points which land inside circle}}{\text{Total number of points tested}} = 4 \times \frac{9}{12} = 3$$

Algorithm for Calculating π

- ▶ How can the above *mathematics* be turned into an *algorithm*?
- ▶ The algorithm needs to repeat the *same thing* multiple times
 - ▶ This implies use of a loop
- ▶ As the loop repeats, we need to keep track of the following *variables*:
 - ▶ The number of points tested
 - ▶ The number of points inside the circle
 - ▶ The (x, y) coordinates of the point under test
- ▶ The incrementation of the “inside circle” count is *conditional* on the values of x and y
 - ▶ This implies an IF...ENDIF flow control structure

Algorithm for Calculating π

- ▶ The number of points tested will be an *integer*, we will call it countTotal
- ▶ The number of points found to be inside the circle is also an integer, we will call it countInside
- ▶ The point under test needs two “real” variables: x and y
 - ▶ “Real” is the generic term for a number with integer and fractional components. Eg: 1.45
- ▶ The condition on incrementing countInside will be $x^2 + y^2 < 1$

Algorithm for Calculating π

```
BEGIN
  integer countTotal = 0
  integer countInside = 0
  WHILE countTotal < A large number
    x = random number between 0 and 1
    y = random number between 0 and 1
    countTotal = countTotal + 1
    IF  $x^2 + y^2 < 1$ 
      countInside = countInside + 1
    ENDIF
  ENDWHILE
  pi = 4*countInside/countTotal
  PRINT pi
END
```

Missing Knowledge for C Implementation

- ▶ More information about arithmetic
 - ▶ Relational operators look useful
 - ▶ Is there a neat way to do `count=count+1`?
 - ▶ `countInside` and `countTotal` are both integers.
What happens when we divide?
- ▶ Datatypes and how they are handled in arithmetic statements
- ▶ How do we generate random numbers?
- ▶ Syntax for WHILE loops and IF statements

C Arithmetic

- ▶ Basic arithmetic was seen in the lab
 - ▶ You all did the lab, right?

Operation	C Symbol
Addition	+
Subtraction	-
Multiplication	*
Division	/

Table: Basic arithmetic operators in C

- ▶ Complex expressions can be built from these operators and parentheses

C Arithmetic

Examples:

$$\begin{array}{ll} z = x^2 + 5(y + b) & z = x*x + 5*(y + b); \\ u = \frac{x+1}{x-1} & u = (x + 1)/(x - 1); \\ v = z^3 + \frac{5(y+b)}{2} & v = z*z*z + (5*(y + b))/2; \end{array}$$

- ▶ Multiplication is not assumed. If you write $5(y+b)$ the compiler will generate a syntax error.
- ▶ To be valid C expressions the semicolon is required.

C Arithmetic

- ▶ C supports two time-saving *unary* operators:
 - ▶ Very useful in loops.

Operation	C Syntax	Replaces
Increment	<code>x++</code> ; or <code>++x</code> ;	<code>x = x + 1</code> ;
Decrement	<code>x--</code> ; or <code>--x</code> ;	<code>x = x - 1</code> ;

- ▶ It also supports the following shorthand syntax:

<code>x = x + y</code> ;	<code>x += y</code> ;
<code>x = x - y</code> ;	<code>x -= y</code> ;
<code>x = x * y</code> ;	<code>x *= y</code> ;
<code>x = x / y</code> ;	<code>x /= y</code> ;

C Arithmetic

What's the difference between $x++$ and $++x$?

- ▶ $x++$ is a *post-increment*
- ▶ $++x$ is a *pre-increment*
- ▶ If they appear in an arithmetic expression, pre-increment is processed *before* the variable is used and post-increment is processed *after* it is used.
- ▶ In isolation there is no difference.

Increment Example

```
1 #include <stdio.h>
2 int main() {
3     int x = 0;
4     int y = 0;
5     int z = 0;
6     y = ++x + 10;
7     printf("Pre-increment: %d\n", y);
8     y = z++ + 10;
9     printf("Post-increment: %d\n", y);
10    return 0;
11 }
```

Pre/post-inc/decrements will be used when working with *arrays*, more details in coming weeks.

Modulus

- ▶ Computers frequently only deal with integers
- ▶ Integer division in C ignores (truncates) any fractional component
- ▶ The *modulus* operator provides the remainder after division
 - ▶ Implemented with the `%` character
 - ▶ $a \% b = \text{remainder of } a / b$
 - ▶ Very useful for tasks performed every *nth* loop
- ▶ Example:
 - ▶ $10 / 3 = 3$
 - ▶ $10 \% 3 = 1$

Relational Operators

- C supports six *relational* operators:

Operation	C Symbol
Less than	<
Less than or equal to	<=
Greater than	>
Greater than or equal to	>=
Equal to	==
Not equal to	!=

Table: Relational operators in C

Relational Operators

- ▶ The result of a relational operation is 0 or 1
 - ▶ C treats 0 as Boolean FALSE and non-zero as TRUE
- ▶ They are typically used as flow control conditions
 - ▶ `if(condition) {statements}`
 - ▶ `while(condition) {statements}`
- ▶ While we're here: the above is the correct syntax for IF and WHILE flow control in C

Modulus Example 1 - Printing Every *nth* Loop

```
1 #include <stdio.h>
2 int main() {
3     int x = 0;
4     while(x < 1000)
5     {
6         // Presumably something useful is done with x
7         // inside this loop
8         if(x%100 == 0)
9             printf("%d\n", x);
10    }
11    return 0;
12 }
```

Modulus Example 2 - Finding Factors

```
1 #include <stdio.h>
2 int main() {
3     int input;
4     int x;
5     printf("Enter an integer to factorise: ");
6     scanf("%d", &input);
7     x = input;
8     while(x > 0) {
9         if(input % x == 0) // ie: if the remainder is zero
10             printf("%d is a factor of %d\n", x, input);
11         x--;
12     }
13     return 0;
14 }
```

Observe that the while() loop loops over every value of x from input to 1. We will discuss a flow control method designed for this (the for loop) later.

C Arithmetic Operator Precedence

- ▶ C has an “order of operations”
- ▶ eg: $1+5*2$ evaluates to 11
- ▶ Multiplication and division first
- ▶ Addition and subtraction second
- ▶ Relational operators somewhere below that
- ▶ If in doubt: force order with parentheses
 - ▶ This makes the code more readable
 - ▶ It doesn't cost you anything
 - ▶ C compilers understand algebra and will optimise inefficient expressions automatically

Data types

- ▶ You have hopefully noticed that all variables are *declared* before use
- ▶ Declaration specifies the variable's:
 - ▶ Datatype
 - ▶ Name
 - ▶ An *initialisation value* (optional)
 - ▶ Always assume uninitialised variables have random values! Behaviour varies between compilers and target platforms.
- ▶ C is a “strongly-typed” language
 - ▶ Every variable has a fixed type

Integer Data types

- ▶ Integer data types vary by their:
 - ▶ Size
 - ▶ Support for negative numbers
- ▶ C integer types can be 1, 2, 4, or 8 bytes long
- ▶ Each type can be *signed* or *unsigned*
 - ▶ Unsigned numbers are never negative but you get double the value range

TODO: Keep hacking until we've implemented π .