ENGG1003 - Tuesday Week 4

Loose Ends
Functions

Brenton Schulz

University of Newcastle

March 16, 2019

Subscript Notation

- Last chance to learn that we use:

$$x_1, x_2, x_3, ..., x_n \tag{1}$$

and

$$x_n = x_{n-1} + x_{n-2} \tag{2}$$

notation because it is the simplest method that gets the point across.

Subscript Notation

- x_n means that x is "some number" and n is an *integer* value
- n implies *uniqueness* (ie: x_1 and x_2 can differ)
- n implies an *order* to the x's
- A formal mathematical statement of the above would be something like:

$$x_n : \ x \in \mathbb{R} \text{ and } n \in \mathbb{Z} \tag{3}$$

- $\mathbb{R}$ is the set of real numbers
- $\mathbb{Z}$ is the set of all integers

Subscript Notation

- Without this notation it is *really* hard to write things like:

$$x_n = x_{n-1} + x_{n-2} \tag{4}$$

Subscript Notation

- Without this notation it is *really* hard to write things like:

$$x_n = x_{n-1} + x_{n-2} \tag{4}$$

- If you instead wrote:
  "Calculate a sequence of numbers, $a, b, c, d, ...$"
  how would you write the equation?

FOR Loops in C

- The C FOR loop syntax is:

```
1 for( initial ; condition ; increment ) {
2   // Loop block
3 }
```

- Where:
  - `initial` is a statement executed *once*
  - `condition` is a statement executed and tested *before* every loop iteration
  - `increment` is a statement executed *after* every loop iteration, but *before* the `condition` is tested

FOR Loops in C

```
1 for( x = 0 ; x < 10 ; x++ ) {
2   printf("%d\n", x);
3 }
```

- Run this code
- Observe that:
  - 0 is printed
  - 10 is **not** printed
  - `x` increments automatically

FOR Example 1 - Factorials

- Use FOR to count from 2 to our input number
- Keep a running product as we go

```
BEGIN
  INPUT x
  result = 1
  FOR k = 2 TO x
    result = result * k
  ENDFOR
END
```

- Is this algorithm robust? What happens if:
  - x = -1
  - x = 1
  - x = 0 (**NB:** 0! = 1 because *maths*)

BREAK Statements

- Sometimes you want to exit a loop *before* the condition is re-tested
- The flow-control mechanism for this is a BREAK statement
- If executed, the loop quits
- BREAKs typically go inside an IF
- It adds an extra condition on loop exit placed at any point in the loop

FOR Example 2

- Two equivalent ways to implement the $\cos()$ series from before are:

NB: |tmp| means "absolute value of tmp".

```
BEGIN
  INPUT x
  sum = 0
  FOR k = 0 to 10
    tmp = (-1)^k x^2k / (2k)!
    sum = sum + tmp
    IF |tmp| < 1e-6
      BREAK
    ENDIF
  ENDWHILE
END
```

```
BEGIN
  INPUT x
  tmp = 1
  k = 0
  sum = 0
  WHILE (k<10)AND(|tmp|>1e-6)
    tmp = (-1)^k x^2k / (2k)!
    sum = sum + tmp
    k = k + 1
  ENDWHILE
END
```

`break` Statements

- The example is mildly pointless
  - In C, the $|tmp| < 1e-6$ condition can go in the `for()` statement. In pseudocode it *sort of* can't.
- It is there to illustrate what `break` does, not explain how to use it
- As the "experienced engineer' that's up to you

FOR Loops in C (Advanced)

- `for()` syntax allows multiple expressions in the `inital` / `condition` /`increment` sections
- Separate expressions with commas
- eg:

```
1 int x, y=10;
2 for( x = 0 ; x < 10 ; x++, y++ ) {
3   printf("x: %d y: %d\n", x, y);
4 }
```

- This increments both `x` and `y` but only `x` is used in the condition

Loop `continue` Statements

- A `continue` causes execution to jump back to the loop start
- The *condition* is tested before reentry
- eg, run this in the Che debugger:

```
1 int x;
2 for(x = 0; x < 10; x++) {
3   if(x%2 == 0)
4     continue;
5   printf("%d is odd\n");
6 }
```

- (Not the best example but gets the point across)

`break` and `continue`

- Some programmers claim that `break` and `continue` are "naughty"
- Well, yes, but actually no
- They *can* make your code needlessly complicated
- They might make it simpler
- It is up to you to judge
- As engineers you shouldn't follow strict rules
- Always try to choose the best tool for the job

GOTO

- There exists a GOTO flow control mechanism
  - Sometimes also called a *branch*
- It "jumps" from one line to a different line
  - An ability some consider to be unnatural
- It exists for a purpose
- That purpose does not (typically) exist when writing C code
  - C *supports* a `goto` statement
  - It results in "spaghetti code" which is hard to read
  - Don't use it in ENGG1003
- You *must* use branch instructions in ELEC1710

Loose End: Increment Example

```c
#include <stdio.h>
int main() {
  int x = 0;
  int y = 0;
  int z = 0;
  y = ++x + 10;
  printf("Pre-increment: %d\n", y);
  y = z++ + 10;
  printf("Post-increment: %d\n", y);
  return 0;
}
```

Pre/post-inc/decrements have many applications, more details in coming weeks.

Binary Nomenclature

- A data type's value range is a result of the underlying binary storage mechanism
- A single binary digit is called a *bit*
- There are 8 bits in a *byte*
- In programming we use the "power of two" definitions of kB, MB, etc:
  - 1 kilobyte is $2^{10} = 1024$ bytes
  - 1 Megabyte is $2^{20} = 1048576$ bytes
  - 1 Gigabyte is $2^{30} = 1073741824$ bytes
  - (Advanced) These numbers look better in hex: `0x3FF`, `0xFFFFF`, etc.

Binary Nomenclature

- Observe that kilobyte, Megabyte, Gigabyte, etc use scientific prefixes
- These *normally* mean a power of 10:
  - kilo- $= 10^3$
  - Mega- $= 10^6$
  - Giga- $= 10^9$
  - ...etc (see the inside cover of a physics text)
- Computer science stole these terms and re-defined them

Binary Nomenclature

- This has made some people *illogically angry*
- Instead, we can use a more modern standard:
  - 2^{10} bytes $= 1$ kibiByte (KiB)
  - 2^{20} bytes $= 1$ Mebibyte (MiB)
  - 2^{30} bytes $= 1$ Gibibyte (GiB)
  - ...etc
- Generally speaking, KB (etc) implies:
  - powers of two to *engineers*
  - powers of ten to *marketing*
    - The number is smaller
    - Hard drive manufacturers, ISPs, etc like this

Unambiguous Integer Data Types

- Because the standard `int` and `long` data types don't have fixed size unambiguous types exist
- Under OnlineGDB (ie: Linux with `gcc`) these are defined in `stdint.h` (`#include` it)
- You will see them used commonly in embedded systems programming (eg: Arduino code)
- The types are:
  - `int8_t`
  - `uint8_t`
  - `int16_t`
  - ...etc

Code Blocks in C

- Semi-revision:
- The curly braces { } encompass a *block*
- You have used these with `if()` and `while()`
- They define the set of lines executed inside the `if()` or `while()`

Code Blocks in C

- You can place blocks anywhere you like
- Nothing wrong with:

```
1 int main() {
2   int x;
3   {
4     printf("%d\n", x);
5   }
6   return 0;
7 }
```

- This just places the `printf();` inside a block
- It doesn't do anything useful, but...

Variable Scope

- A variable's "existence" is limited to the block where it is declared
  - Plus any blocks within that one
- Example this code won't compile:

```
1  #include <stdio.h>
2  int main() {
3    int x = 2;
4    if(x == 2) {
5      int k;
6      k = 2*x;
7    }
8    printf("%d\n", k);
9    return 0;
10 }
```

Variable Scope

- Note that `k` was declared inside the `if()`
- That means that it no longer exists when the `if()` has finished
- This generates a compiler error
- It frees up some RAM
- It also lets the variable's name be reused elsewhere
  - This can be *really* confusing. Be careful.

Functions

- A *function* is a block of code which can be *called* multiple times, from multiple places
- They are used when you want the same block of code to execute in many places throughout your code
- A function requires:
  - A name
  - (optional) A *return value*
  - (optional) One or more *arguments*

Functions in Mathematics

- In mathematics you saw functions written as:

$$y = f(x)$$

- Here, the function is called f, takes an argument of x and returns a value which is given to y
- C and pure mathematics have these general ideas in common

Functions in Mathematics

- In mathematics you saw functions written as:

$$y = f(x)$$

- Here, the function is called f, takes an argument of x and returns a value which is given to y
- C and pure mathematics have these general ideas in common
- The similarities stop there

Function Examples

- So far, some of you have used *library functions*
- These are functions which are pre-existing within the compiler (and its libraries)
- I have shown you:
  - `scanf();`
  - `printf();`
  - `rand();`

Function Syntax

- Writing `rand();` in you code is *calling* the function
- The program execution "jumps" into the function's code, executes it, then jumps back
- Function call syntax is:

```
[return value] = name( [arguments] )
```

- Not all functions take arguments
- You may ignore the return value

Function Examples

- Example 1:

```
1 x = rand();
```

  - `rand` is the function name
  - It returns a "random" number
  - The return value is allocated to `x`
  - It doesn't take an argument

Function Examples

- Example 1:

```
1 x = rand();
```

  - `rand` is the function name
  - It returns a "random" number
  - The return value is allocated to `x`
  - It doesn't take an argument

- Example 2:

```
1 y = sqrtf(x);
```

  - `sqrtf` is the function name
  - `x` is the argument
  - It returns the square root of `x`
  - The return value is allocated to `y`

Functions

- Function arguments and return values have pre-defined data types

Functions

- Function arguments and return values have pre-defined data types
- Example from documentation
  - `int rand(void);`
    - The return value is an `int`
    - The argument is type `void`
    - This just means there aren't any

Functions

- Function arguments and return values have pre-defined data types
- Example from documentation
  - `int rand(void);`
    - The return value is an `int`
    - The argument is type `void`
    - This just means there aren't any
  - `float sqrtf(float x);`
    - The return value is a `float`
    - The argument is a `float`
    - Argument is called `x` in documentation but that is irrelevant

Return Values (an Engineer's View)

- The function's *return value* is the number a function gets "replaced with" in a line of code

Return Values (an Engineer's View)

- The function's *return value* is the number a function gets "replaced with" in a line of code
- Function return values, variables, and literals can all be used in the same places:
  - In arithmetic
  - In conditions
  - As arguments to other functions

Return Values (an Engineer's View)

- The function's *return value* is the number a function gets "replaced with" in a line of code
- Function return values, variables, and literals can all be used in the same places:
  - In arithmetic
  - In conditions
  - As arguments to other functions
- The C standard is *very* specific about what return values are but I will be informal for now
  - Technically, for example, an expression like `x=y+5.0;` also has a "return value" equal to the value allocated to `x`

Return Values

- I use functions from `math.h` in these examples, we'll cover them in a few mins

Return Values

- I use functions from `math.h` in these examples, we'll cover them in a few mins
- The following are all valid:
  - `x = rand();`
  - `printf("%f\n", sin(y));`
  - `if( (rand()%6) < 2)`
  - `while( sin(x) < 0 )`

Return Values

- I use functions from `math.h` in these examples, we'll cover them in a few mins
- The following are all valid:
  - `x = rand();`
  - `printf("%f\n", sin(y));`
  - `if( (rand()%6) < 2)`
  - `while( sin(x) < 0 )`
  - This next one is complicated...

Return Values

- I use functions from `math.h` in these examples, we'll cover them in a few mins
- The following are all valid:
  - `x = rand();`
  - `printf("%f\n", sin(y));`
  - `if( (rand()%6) < 2)`
  - `while( sin(x) < 0 )`
  - This next one is complicated...
  - `x = sin((double)rand());`

Return Values

- I use functions from `math.h` in these examples, we'll cover them in a few mins
- The following are all valid:
  - `x = rand();`
  - `printf("%f\n", sin(y));`
  - `if( (rand()%6) < 2)`
  - `while( sin(x) < 0 )`
  - This next one is complicated...
  - `x = sin((double)rand());`
    - Generates a random integer, casts to `double`, uses that number as an argument to the `sin()` function

Using Functions

- (semi-revision)
- Before you use a function you must:
  - Read the documentation
  - `#include` the correct header file
  - Add the correct library to the compiler options
    - In Che I've done this for the maths library
    - `stdio` and `stdlib` are always there
  - Be aware of the data types
    - Do you need any type casting?
    - Are you using the correct function?

Maths Functions

- Since some of you have already used them, lets learn about the maths library...
- It includes functions for:
  - Trigonometry
  - Exponentials (base e) & logarithms (base e and 10)
  - Exponents
  - Rounding (`floor();` & `ceil();`)
  - Floating point modulus (`fmod();`)
  - Square roots
  - Maybe others?

Maths Functions

- There are typically *different* functions for `float` and `double`
- This can have a huge speed impact
- Get in the habit of using the right ones!
- `float` maths functions typically end in `'f'`
  - `cosf();`
  - `sqrtf();`
  - `atanf();`
  - ...etc
- `double` maths functions don't end in `'f'`
  - `cos();`
  - `log();`

Maths Functions

- Math functions are written by mathematicians
  - All angles are in radians

Maths Functions

- Math functions are written by mathematicians
  - All angles are in radians
  - `log();` is $\log_e$
    - `log10();` is $\log_{10}$
    - `log2();` is $\log_2$

Maths Functions

- Math functions are written by mathematicians
  - All angles are in radians
  - `log();` is $\log_e$
    - `log10();` is $\log_{10}$
    - `log2();` is $\log_2$
  - Inverse trig functions are called "arcus functions"
    - $\sin^{-1}$ is `asin();`
    - $\cos^{-1}$ is `acos();`
    - $\tan^{-1}$ is `atan();`

Maths Functions

- Math functions are written by mathematicians
  - All angles are in radians
  - `log();` is $\log_e$
    - `log10();` is $\log_{10}$
    - `log2();` is $\log_2$
  - Inverse trig functions are called "arcus functions"
    - $\sin^{-1}$ is `asin();`
    - $\cos^{-1}$ is `acos();`
    - $\tan^{-1}$ is `atan();`
  - The "4 quadrant" arctan function is `atan2();`
    - `atan(x);` returns $[0, \pi]$
    - `atan2(x,y);` returns $[-\pi, \pi]$ depending on the quadrant of the point `x,y`
    - Very useful for polar to Cartesian coordinate transforms (probably beyond 1st semester 1st year)

Example - Quadratic Equation

Write a C program which uses the standard library function `sqrtf();` as part of the calculations required to produce solutions to a quadratic equation:

$$ax^2 + bx + c = 0 \tag{5}$$

using

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \tag{6}$$

...do it live in Che