ENGG1003 - Friday Week 1

Algorithms and Pseudocode

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March 4, 2019



Lab feedback? Yell it out to me.

Algorithms

- Informally, an algorithm is a series of steps which accomplishes a task
- More accurately, the steps (instructions) must:
 - Have a strict order
 - Be unambiguous
 - Be executable
- "Executable" means that the target platform is capable of performing that task.
 - eg: An industrial welding robot can execute "move welding tip 1 cm left". A mobile phone can't.



Algorithms

- An algorithm exists purely as an abstract concept until it is communicated
- ► We will use:
 - Pseudocode to communicate algorithms to ourselves and other people
 - The languages C and MATLAB to communicate algorithms to computers
- Pseudocode can be very formal, but as engineers we will only use formal rules if required
 - eg: When documenting algorithms for other people
 - Your own "working out" can be anything that helps you



Algorithm Example 1

Name: Algorithm given to mum to start my car (2015 Tarago)

Result: The vehicle's engine is idling

Initialisation: stand next to the vehicle, key fob in hand

- 1. Depress the unlock button on the key fob, car will beep twice
- 2. Place key fob in your pocket
- 3. Enter the vehicle, sit in the driver's seat
- 4. Ensure that the gear selector has P engaged
- 5. Depress the brake pedal
- 6. Press the engine start button
- 7. Wait 5 seconds
- 8. If engine is not idling
 - Call me



Example Discussion

- Algorithms typically need to feel over-explained
 - Computers are really stupid; get in the habit of over-thinking everything
- ► The algorithm contained *flow control* in the form of an "if" statement
 - ► The final step ("call me") was conditional on the car not starting
- We will discuss conditional logical statements later, but first...



Algorithm Example 2

A wife asks her husband, a programmer, "Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?

A short time later the husband comes back with 6 cartons of milk and his wife asks, "Why did you buy 6 cartons of milk?

He replies, They had eggs.

Algorithm Example 2a

Lets make this more realistic.

A wife asks her robot helper, "Could you please go shopping for me and buy one carton of milk, and if they have eggs, get 6?

The robot replies: "Unknown instruction: 'get 6'."

Flow Control

- Instructions in an algorithm execute in an ordered list
 - ie: top to bottom
- Flow Control is any algorithmic mechanism which changes the default "top to bottom" execution behaviour
- We will discuss IF statements and loops
- Flow control (almost) always requires a condition



Conditions

- Computers don't understand "maybe"
- A condition must be absolutely true or false
- Human examples:
 - ▶ I am within the boundary of the Callaghan campus
 - ▶ I am alive
 - My net worth is below AU\$100M
- Computer examples:
 - ▶ i is less than 184
 - x plus y is not equal to zero
 - Input data has been given to the program
 - A division by zero has occurred



Code Blocks

- A block is a set of instructions which are, for some reason, grouped together
- If a single condition controls multiple instructions they can go together in a block
- A block is typically indicated via indentation
- Eg:

```
IF it is raining
Pack an umbrella
Drive to campus instead of walking
Leave home 40mins early to find parking
ENDIF
```

IF Variants

- ▶ There are several versions of IF flow control:
 - ► IF ... ENDIF
 - ▶ IF ... ELSE ... ENDIF
 - ► IF ... ELSEIF ... ENDIF
- The IF and ELSEIF keywords indicate conditions
- The ELSE keyword is unconditional
- Which one you choose depends on need
 - Is there one thing which is conditional?
 - Do I need to make a choice between two or more options?
 - Could nothing be executed?



IF Statement Syntax

► The IF ... ENDIF syntax is:

```
IF condition
do some things
```

Likewise: IF ... ELSEIF ... ENDIF syntax is:

```
IF condition1
  do some things
ELSEIF condition2
  do other things
ENDIF
```

► And finally:

```
IF condition
do some things
ELSE
do some things
ENDIF
```

IF ... ELSEIF

- ► The IF ... ELSEIF construct can have multiple ELSEIF sections
- A crucial point:
 - Conditions are only tested if the previous ones fail
 - Once a condition is TRUE the others are ignored
 - ie: IF ELSE implements a choice priority

Algorithm Example 3 - Quadratic Root Finding

From high school you should know that the equation

$$ax^2 + bx + c = 0 \tag{1}$$

has solutions given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \tag{2}$$

lets write an algorithm which provides real valued solutions to a quadratic equation.

Algorithm Example 3 - Quadratic Root Finding

Input: Real numbers a, b, and c **Output:** Three numbers:

- 1. The number of solutions, N
- 2. One of the roots, x_1
- 3. The other root, x_2

Behaviour:

- ▶ If N is 2 then x_1 and x_2 are different real numbers
- ▶ If N is 1 then x_1 is the unique solution and x_2 is undefined
- ▶ If N is 0 then x_1 and x_2 are undefined



Algorithm Example 3 - Quadratic Root Finding

```
BEGIN

INPUT: a, b, c

D = b^2 - 4ac

IF D < 0

N = 0

ELSEIF D == 0

N = 1

x1 = -b/(2a)

ELSEIF D > 0

N = 2

x1 = (-b + sqrt(D))/(2a)

ENDIF
```

- Reasonably formal pseudocode
- The IF ... ELSE IF flow control construct forces exclusive execution of only one block
 - ► The first condition that is true causes execution of that block
 - Subsequent blocks ignored
 - Contains 3 conditions

END

Boolean Algebra Basics

- What if we want more complicated conditions? Boolean algebra is needed!
- Boolean algebra (or Boolean logic) is a field of mathematics which evaluates combinations of logical variables as either true or false
- Boolean variables can only take the values true (or 1) or false (or 0)
- Boolean algebra defines three operators:
 - ► OR
 - AND
 - ► NOT



Boolean Algebra Basics

- Boolean variables can be allocated any symbols (just like in "normal" algebra)
 - ► Typically get upper-case letters
 - ightharpoonup eg: X = A OR B
- Various symbols can be used for OR/AND/NOT, we will only use the words here
 - Write them in capitals to remove ambiguity
 - C and MATLAB have their own symbols for Boolean algebra
 - Other courses (eg: ELE17100) will use different symbols again



Boolean Operators

- An operand is a value on which a mathematical operation takes place
 - ightharpoonup eg: In "1 + 2" the 1 and 2 are operands and + is the operator
- OR Evaluates true if either operand is true
 - \triangleright X = A OR B
 - X is true if A or B is true
- AND- Evaluates true only when both operands are true
 - \triangleright X = A AND B
 - X is true only if both A and B is true



Boolean Operators

- OR and AND are binary operators
 - ► They operate on two operands
 - ► From Latin "bini" meaning "two together"
- The NOT operator is unary
 - It only operates on one operand
 - NB: The operand could be a single variable or complex expression
- NOT performs a logical inversion
 - ► NOT true = false
 - NOT false = true



Boolean Condition Examples

- My car needs a service if, since the last service, (more than 6 months has past) OR (more than 15000km have been travelled)
- ➤ You will pass this course if (you score 40% or more in the final exam) AND (the weighted sum of all assessments is more than 50%)
- ➤ A computer program repeats an algorithm if (there is still data to process) AND (errors have not occurred) AND (NOT (the user has terminated the program))



Algorithm Example 4 - Boolean Conditions

Problem: How can trigonometric functions be calculated by a computer?

One Solution: Series expansion! (Seen in MATH1120).

The function cos(x) can be evaluated with arithmetic as:

$$\cos(x) = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} = 1 + \frac{-x^2}{2!} + \frac{x^4}{4!} + \frac{-x^6}{6!} + \frac{x^8}{8!} \dots$$
 (3)

Evaluation of this series needs two things:

- 1. The *loop* flow control concept
- 2. Some kind of stop condition



Factorial

- Do we know what factorials are?
- ► The product of an integer and all the integers between it and 1
- Notation in mathematics is the ! symbol
 - eg: $4! = 4 \times 3 \times 2 \times 1 = 24$
- ▶ NB: C uses! for Boolean NOT
 - C does not have a factorial operator

Algorithm Example 4 - Boolean Conditions

- Computers can't count to infinity, we need to know when to stop
- Computers have limited precision, 16 significant figures is typical
- Observe that as k increases in Equation 4 the denominator increases really fast (4!=24, 10!=3628800)
- ▶ This implies that the value of $\frac{(-1)^k x^{2k}}{(2k)!}$ tends to drop as k increases
- ▶ Therefore, we can add terms until they are "too small"
- \triangleright A maximum value of k can also be specified for safety

$$\cos(x) = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} \tag{4}$$



Loops

- ➤ A loop causes an algorithm to execute a given block of instruction multiple times
- Loops typically require an exit condition
 - Without an exit condition they are called infinite loops
 - Yes, these have a purpose
- Multiple types of loops
 - WHILE condition...ENDWHILE
 - ▶ DO...WHILE condition
 - ► FOR counter FROM 1 TO something



Algorithm Example 4 - Boolean Conditions

The while loop repeats a block of steps until the *condition* becomes false.

```
BEGIN
  TNPIIT x
  tmp = 1
  k = 0
  sum = 0
  WHILE (k<10) AND ((tmp>-1e-6) AND (tmp<1e-6))
    tmp = \frac{(-1)^k x^{2k}}{(2k)!}
    sum = sum + tmp
    k = k + 1
  ENDWHILE
END
```

Here it loops until 10 iterations have occurred OR a precision limit is reached

This is where we left off... Updates:

- Changed = to == in "D == 0" quadratic algorithm. == means "is equal to".
- Added "1+" to the series expansion
- Changed series expansion loop condition to be (absolute value(tmp) < 1e-6)
 - ► Implemented with tmp greater than -1e-6 AND less than 1e-6 (ie: within the interval (-1e-6, 1e-6))

Loop Details

- WHILE conditions are tested before "entering"
- The condition is tested before every repeat
- Variables in the condition should change inside the loop
 - Try to avoid infinite loops unless you want one
- What if we want to force the loop to execute at least once?

DO ... WHILE

- ► Same as WHILE except executes at least once
- The condition is tested at the end
- Loops repeats if condition is TRUE
- Syntax:

```
DO stuff WHILE condition
```

FOR Loops

- ► A FOR loop executes a given number of times
- Used when the number of loop repeats is known before entering the loop
 - Repeat count could be "hard coded" as a number
 - Could also be a variable
- Can be easier to read than WHILE
- Example pseudocode syntax:

```
FOR x = 1 to 10
  Do something ten times
ENDFOR
```

► The *loop variable* is automatically incremented



BREAK Statements

- Sometimes you want to exit a loop before the condition is re-tested
- The flow-control mechanism for this is a BREAK statement
- If executed, the loop quits
- BREAKs typically go inside an IF to control their execution

FOR Example 1

► Two equivalent ways to implement the cos() series from before are:

NB: |tmp| means "absolute value of tmp".

```
BEGIN

INPUT x

sum = 0

FOR k = 0 to 10

tmp = \frac{(-1)^k x^{2k}}{(2k)!}

sum = sum + tmp

IF |tmp| < 1e-6

BREAK

ENDIF

ENDWHILE
```

```
BEGIN

INPUT x

tmp = 1

k = 0

sum = 0

WHILE (k<10) AND(|tmp|>1e-6)

tmp = \frac{(-1)^k x^{2k}}{(2k)!}

sum = sum + tmp

k = k + 1

ENDWHILE

END
```

FOR Example 2 - Factorials

- Use FOR to count from 2 to our input number
- Keep a running product as we go

```
BEGIN
   INPUT x
   result = 1
   FOR k = 2 TO x
     result = result * k
   ENDFOR
END
```

Is this algorithm robust? What happens if:

```
x = -1
x = 1
```

 \rightarrow x = 0 (**NB**: 0! = 1 because *maths*)



GOTO

- There exists a GOTO flow control mechanism
 - Sometimes also called a branch
- ▶ It "jumps" from one line to a different line
- It exists for a purpose
- That purpose does not (typically) exist when writing C code
 - C supports a goto statement
 - It results in "spaghetti code" which is hard to read
 - Don't use it in ENGG1003
- You can use GOTO in ELEC1710



Lets end with a joke