1 Understand Functor and Applicative Functor

1.1 Functor and Applicative

What is Applicative Functor in Haskell? Applicative Functor is almost like Functor

Functor - it takes the value inside a box and compute it, then wrap the result into a box.

```
class Functor f where
    fmap::(a -> b) -> f a -> f b

-- Functor needs to satisfy two laws:
-- fmap id = id
-- fmap(f . g) = (fmap f)(fmap g)

instance Functor Maybe where
    fmap:: (a -> b) -> Maybe a -> Maybe b
    fmap _ Nothing = Nothing
    fmap f (Just x) = (Just f x)

class (Functor f)=> Applicative f where
    pure:: a -> f a
    <%> :: f (a -> b) -> f a -> f b
```

From the definition of Applicative Functor, If you want to be a Applicative Functor, you have to be a Functor first. In other words, Applicative is also a Functor and you need to implement two functions:

```
pure:: a -> f a
<%> :: f (a -> b) -> f a -> f b
```

Maybe is a Applicative Functor, and we know Maybe is also a Functor too, let's implement the two functions.

```
instance Applicative Maybe where
   pure a = (Just a) -- pure = Just
```

For Applicative Maybe, If you pass anything to pure, then pure just wraps it with Just.

```
Nothing <%> _ = Nothing
_ <%> Nothing = Nothing
(Just f) <%> (Just a) = (Just f a)
```

<%> either side is Nothing then Nothing comes out <%> if f is inside Just, <%> extracts f out and applies fmap f (Just x) = (Just f x) How to implement <%> with fmap?

Functor contains a function $(a \to b)$, fmap applies the function $(a \to b)$ to a functor and wrap the result inside a functor, The difference between Functor and Applicative Functor:

```
Functor: \langle \$ \rangle applies (a \to b) inside fa
```

Applicative Functor: <%> extracts $(a\rightarrow b)$ out from functor and applies it inside fa

```
(+ 3) <$> (Just 2) => Just 5 -- Functor
(Just (+ 3)) <*> (Just 2) => Just 5 -- Applicative Functor
(++) <$> getLine <*> getLine = ((++) <$> getLine) <*> getLine => "a" ++ "b"
```