Newton's Iteration Method

First method to derive Newton's iteratino method

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h} \quad \text{def. of limit}$$

$$f'(x) \approx \frac{f(x+h) - f(x)}{h} \quad \text{where h is sufficient small}$$

$$f'(x_0) \approx \frac{f(x_0 + h) - f(x_0)}{h}$$

$$f'(x_0) = \frac{y - y_0}{x - x_0} \qquad (1)$$

$$h = \frac{f(x_0 + h) - f(x_0)}{f'(x_0)}$$

$$h = \frac{0 - f(x_0)}{f'(x_0)} \quad \text{where line } f(x_0 + h) = 0 \text{ intercepts x-axis}$$

$$x_1 = x_0 + h \quad \text{second root}$$

Method 2 to derive Newton's iteration method

$$y - y_0 = f'(x_0)(x - x_0)$$

$$y = f'(x_0)(x - x_0) + y_0$$

$$y - y_0 = f'(x_0)(x - x_0)$$

$$x = \frac{-y_0}{f'(x_0)} + x_0 \quad \text{where } y = 0$$

$$x = x_0 - \frac{y_0}{f'(x_0)}$$

$$x_1 = x_0 - \frac{y_0}{f'(x_0)}$$
(2)