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#### Calculus on Manifolds

A modern approach to classical theorems of advanced calculus

#### 1965

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