

Derived circle parametic equation line equation from (0,r) to (t, 0)

line equatin

$$\frac{y-0}{x-t} = \frac{y-r}{x-0}$$

$$\Rightarrow xy = (y-r)(x-t)$$

$$\Rightarrow xy = xy - rx - yt + rt$$

$$\Rightarrow rx = rt - yt = t(r-y)$$

$$\Rightarrow rx = t(r-y)$$

$$\Rightarrow x = \frac{t}{r}(r-y)$$
(1)

Let the circle equation to be

$$x^{2} + y^{2} = r^{2}$$

$$\Rightarrow \left(\frac{t}{r}(r-y)\right)^{2} + y^{2} = r^{2}$$

$$\Rightarrow \left(\frac{t}{r}\right)^{2}(r-y)^{2} + y^{2} = r^{2}$$

$$\Rightarrow t^{2}(r^{2} + y^{2} - 2ry) + r^{2}y^{2} = r^{4}$$

$$\Rightarrow t^{2}r^{2} + t^{2}y^{2} - 2rt^{2}y + r^{2}y^{2} = r^{4}$$

$$\Rightarrow (t^{2} + r^{2})y^{2} - 2rt^{2}y + t^{2}r^{2} - r^{4} = 0$$

$$\Rightarrow a = (t^{2} + r^{2}) \quad b = -2rt^{2} \quad c = t^{2}r^{2} - r^{4}$$

$$y = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$$

$$\Rightarrow y = \frac{2rt^2 \pm \sqrt{4r^2t^4 - 4(t^2 + r^2)(t^2r^2 - r^4)}}{2(t^2 + r^2)}$$

$$\Rightarrow y = \frac{rt^2 \pm \sqrt{r^2t^4 - (t^4r^2 - t^2r^4 + t^2r^4 - r^6)}}{(t^2 + r^2)}$$

$$\Rightarrow y = \frac{rt^2 \pm \sqrt{r^2t^4 - t^4r^2 + t^2r^4 - t^2r^4 + r^6}}{(t^2 + r^2)}$$

$$\Rightarrow y = \frac{rt^2 \pm \sqrt{t^2r^4 - t^2r^4 + r^6}}{(t^2 + r^2)}$$

$$\Rightarrow y = \frac{r(t^2 \pm r^2)}{(t^2 + r^2)}$$

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$$\Rightarrow y = r$$

$$\Rightarrow \begin{cases} x = \frac{t}{r}(r - y) & (3) \\ y = r & (3) \end{cases}$$

$$\Rightarrow \begin{cases} x = \frac{t}{r}(r - y) & (3) \\ y = \frac{r(t^2 - r^2)}{(t^2 + r^2)} & (4) \end{cases}$$

$$\Rightarrow \text{Sub}(2) \text{ into } (1)$$

$$\Rightarrow \frac{t^2}{r^2}(r - y)^2 + y^2 = r^2$$

$$\Rightarrow \frac{t^2}{r^2}(r^2 + y^2 - 2ry) + y^2 = r^2$$