

		Truth / Reality.	
		H_0 true $\theta = 0$	H_0 false $\theta \neq 0$
Decision / conclusion	Do not reject H_0	✓	Type II error.
	Reject H_0	Type I error α	Power ✓

Family-wise error rate

Level of significance = α .

$$\text{FWER} = P(\text{falsely rejecting at least one } H_{0i} \text{ in a set of } m \text{ tests})$$

$$= P(V \geq 1)$$

$$= 1 - P(V = 0)$$

$$= 1 - P(\text{never falsely rejecting any hypotheses in a set of } m \text{ tests})$$

$$= 1 - (1 - \alpha)^m$$

$$P(\text{falsely rejecting one } H_0)$$

$$= P(\text{making one type I error})$$

$$= \alpha$$

$$P(\text{not making a type I error}) = 1 - \alpha.$$

$$P(\text{not making } m \text{ type I errors (out of } m \text{ trials)}) = (1 - \alpha)^m$$

Case study 2

$$H_0: \mu_1 - \mu_2 = 0$$
$$H_1: \mu_1 - \mu_2 \neq 0$$

Uncorrected p-values

	Truth	
	H_0 true	H_0 false
do not reject H_0	479	0
reject H_0	21	500

$$\left(\frac{21}{\cancel{479}} \approx \cancel{0.042} \right)$$
$$\frac{21}{500} = 0.042$$

Bonferroni p-values

	Truth	
	H_0 true	H_0 false
do not reject H_0	500	26
reject H_0	0	474.

BH p-values

	Truth	
	H_0 true	H_0 false
do not reject H_0	491	0
reject H_0	9	500.