

$$\begin{aligned}
&= \sum_{k=0}^{\infty} [(k+1) P_k(k, N-k)] + \frac{k_2}{v} k(N-k) + \frac{k_3}{v^2} k(k-1)(N-k) \\
&\quad + \sum_{k=0}^{\infty} [(k-1) P_k(k, k) + \frac{k_2}{v} k(N-k) + \frac{k_3}{v^2} (k(N-k)(N-k-1))] \\
&\quad - \sum_{k=0}^{\infty} [k P_k(k, N) + \frac{2k_2}{v} k(N-k) + \frac{k_3}{v^2} k(N-k)(N-2)]
\end{aligned}$$

$$\begin{aligned}
&= \sum_{k=0}^{\infty} P_k k, \underbrace{[(k+1)(N-k) + (k-1)k - kN]}_{\text{part 1}} + \underbrace{\sum_{k=0}^{\infty} P_k \frac{k_2}{v} k(N-k)}_0 \underbrace{\frac{(k+1+k-1-2k)}{0}}_0 \\
&\quad + \sum_{k=0}^{\infty} P_k \frac{k_3}{v^2} [(k+1)k(k-1)(N-k) - k^2(N-k)(N-2)] \\
&\quad \underbrace{+ k(N-k)(N-k-1)(k-1)}_{\text{part 2.}}
\end{aligned}$$

$$\begin{aligned}
\text{part 1:} &= \sum_{k=0}^{\infty} P_k k, (kN - k^2 + N - k + k^2 - k - kN) = \\
&\sum_{k=0}^{\infty} P_k k, (N - 2k) = k, (N - 2\langle n \rangle)
\end{aligned}$$

part 2:

$$\begin{aligned}
&= \sum_{k=0}^{\infty} P_k \frac{k_3}{v^2} (k(k-1)(k+1)(N-k) + (k-1)k(N-k)(N-k-1) - k^2(N-k)(N-2)) = \\
&\sum_{k=0}^{\infty} P_k \frac{k_3}{v^2} (k(k^2-1)(N-k) + k(N-k)(k-1)(N-k-1) - k^2(N-k)(N-2)) =
\end{aligned}$$

$$\sum_{k=0}^{\infty} P_k \frac{k_3}{v^2} (k^2 - 1 + Nk - k^2 - k - N + k + 1 - Nk + 2k) =$$

$$\sum_{k=0}^{\infty} P_k \frac{k_3}{v^2} (k(N-k)(2k-N)) = \sum_{k=0}^{\infty} P_k \frac{k_3}{v^2} (Nk - k^2)(2k-N) =$$

$$\sum_{k=0}^{\infty} P_k \frac{k_3}{v^2} (2Nk^2 - N^2k - 2k^3 + k^2N) = \sum_{k=0}^{\infty} P_k \frac{k_3}{v^2} (3Nk^2 - 2k^3 - N^2k)$$

$$= 3N\langle n^2 \rangle - N^2\langle n \rangle - 2\langle n^3 \rangle \Rightarrow \frac{\partial \langle n^2 \rangle}{\partial t} = k, (N - 2\langle n \rangle) +$$

$$\frac{k_3}{v^2} (3N\langle n^2 \rangle - N^2\langle n \rangle - 2\langle n^3 \rangle)$$